

# Observing Exoplanets

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*Subaru Telescope, National Astronomical Observatory of Japan, National Institutes for Natural Sciences (NINS)*



Nov 29, 2017

# My Background

Astronomer / Optical scientist at University of Arizona and Subaru Telescope (National Astronomical Observatory of Japan, Telescope located in Hawaii)

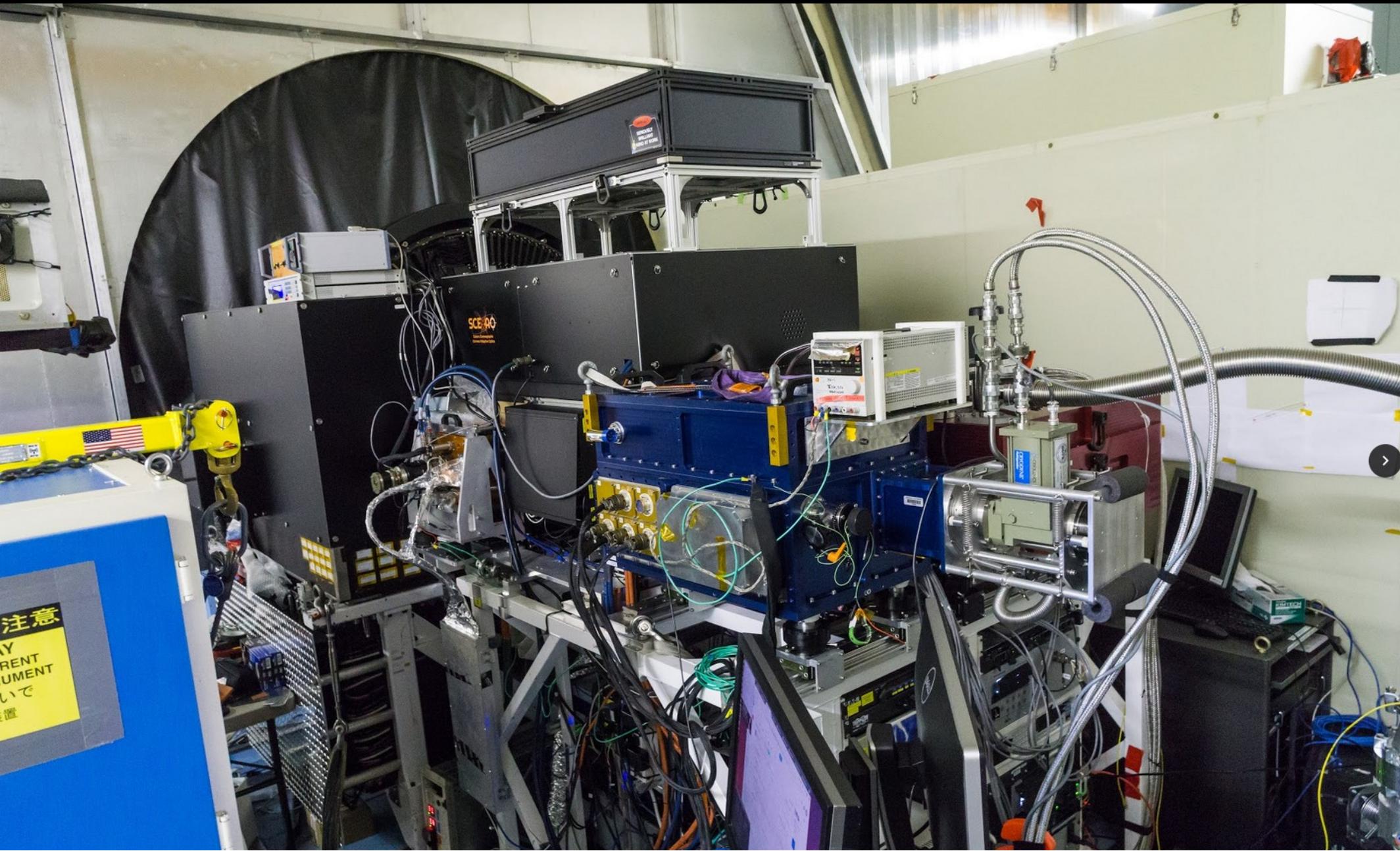
I develop instrumentation to find and study exoplanet, for ground-based telescopes and space missions

My interest is focused on habitable planets and search for life outside our solar system

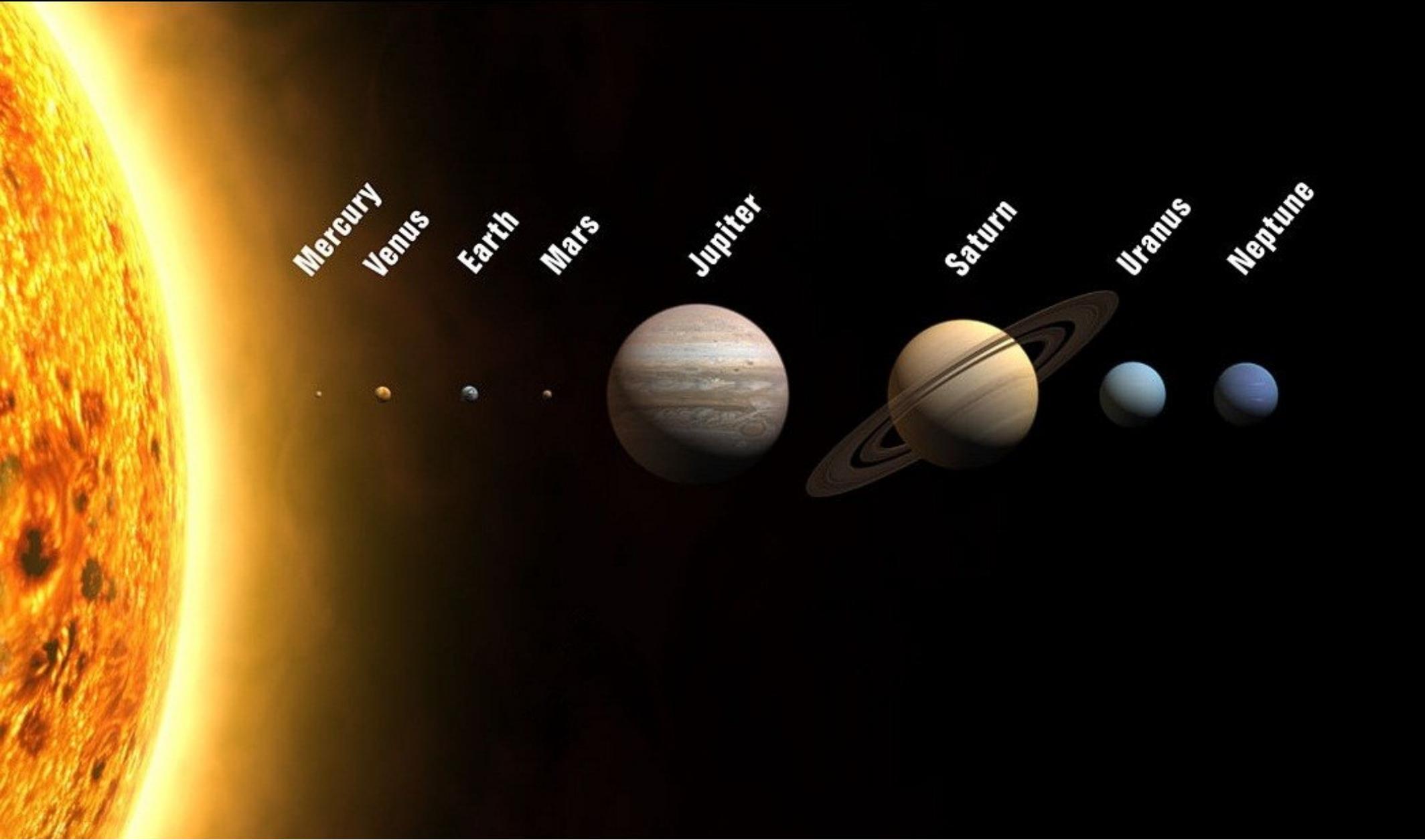
At Subaru Telescope, I lead the Subaru Coronagraphic Extreme Adaptive Optics (SCEXAO) instrument.



# Subaru Coronagraphic Extreme Adaptive Optics



# *ALL known Planets until 1989*



# ***Approximately 10% of stars have a potentially habitable planet***

***200 billion stars in our galaxy***

***→ approximately 20 billion habitable planets***

***Imagine 200 explorers, each spending 20s on each habitable planet, 24hr a day, 7 days a week.***

***It would take >60yr to explore all habitable planets in our galaxy alone.***

***x 100,000,000,000 galaxies in the observable universe***

# Habitable planets

Potentially habitable planet :

- **Planet mass** sufficiently large to retain atmosphere, but sufficiently low to avoid becoming gaseous giant
- **Planet distance to star** allows surface temperature suitable for liquid water (habitable zone)

**Habitable zone = zone within which Earth-like planet could harbor life**

Location of habitable zone is function of star luminosity  $L$ . For constant stellar flux, distance to star scales as  $L^{1/2}$

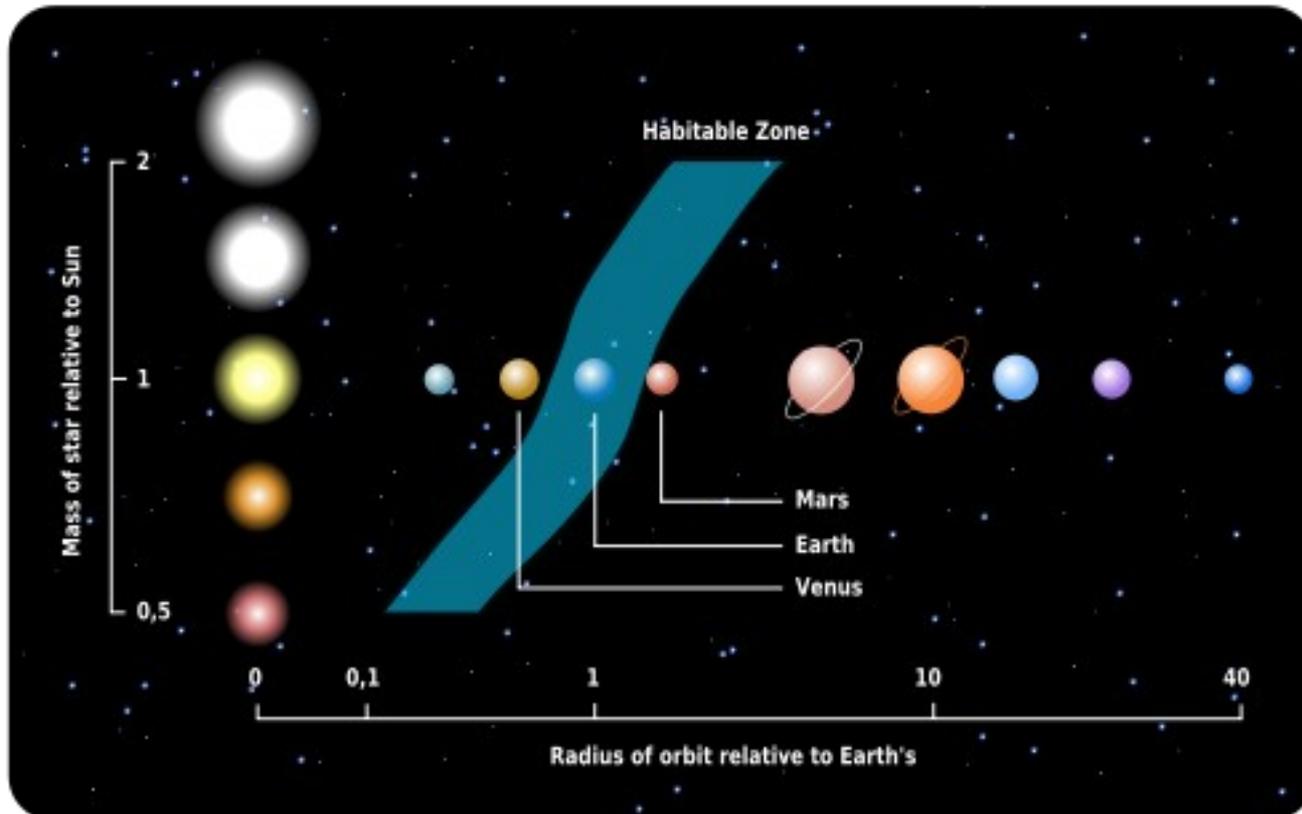
Examples:

Sun

→ habitable zone is at ~1 AU

Rigel (B type star)

Proxima Centauri (M type star)



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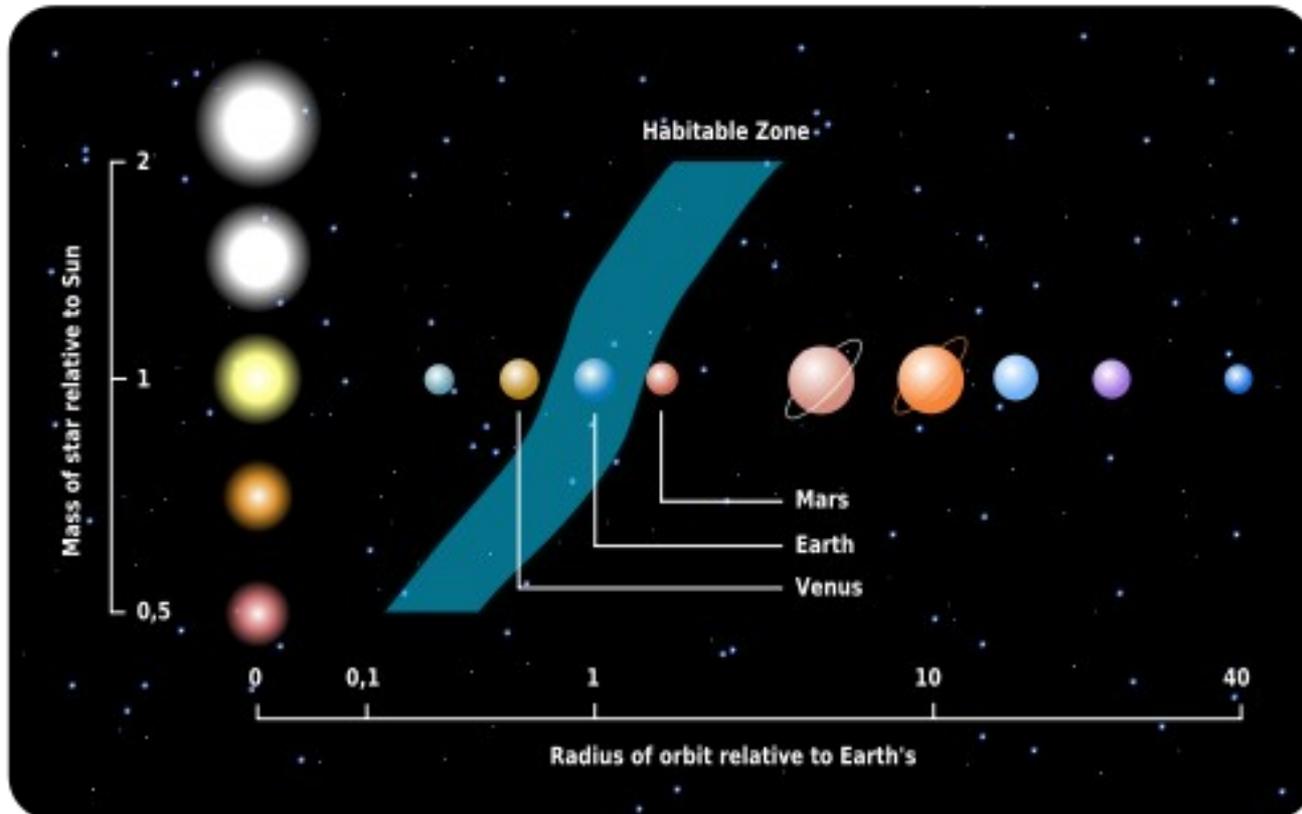
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Rigel (B type star):

18 solar mass

Proxima Centauri (M type star):

0.123 solar mass



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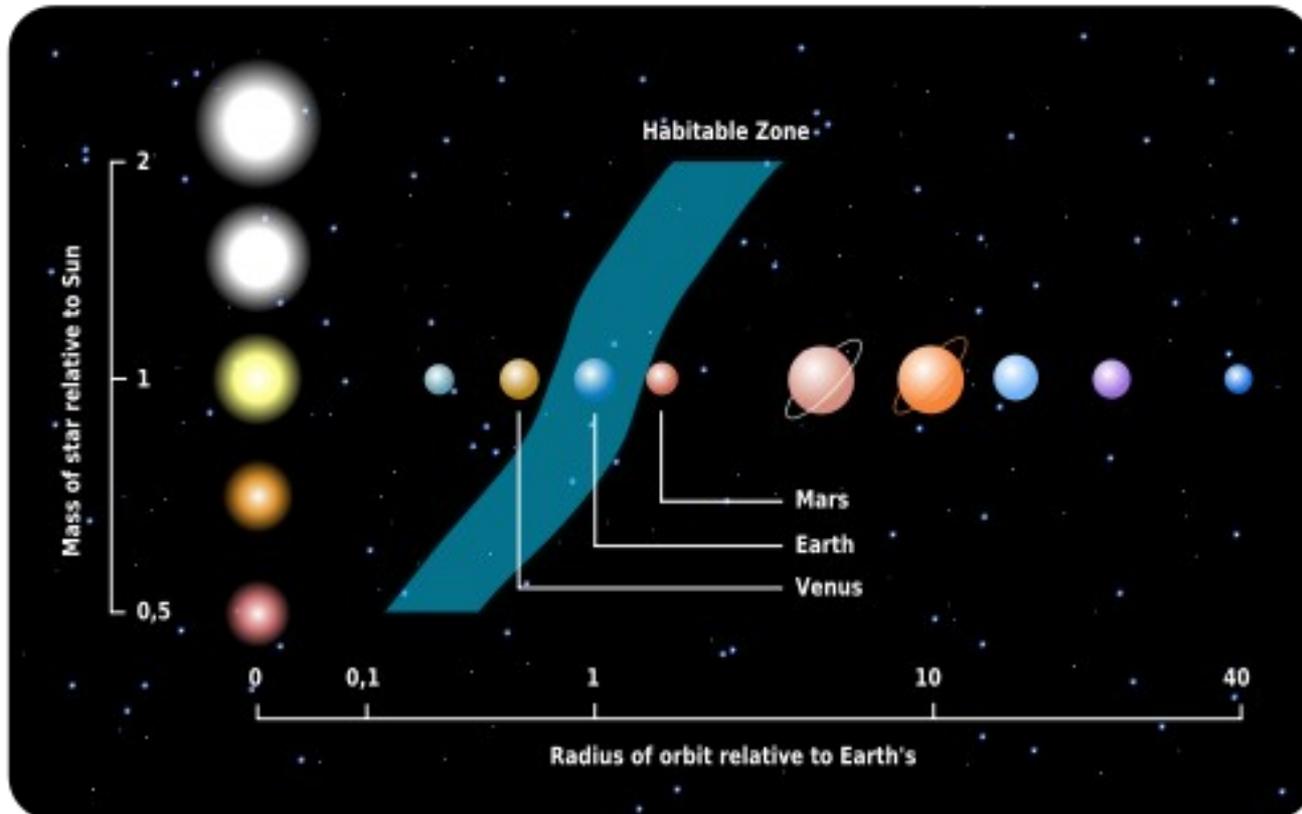
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100000x Sun luminosity

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1/600 Sun luminosity



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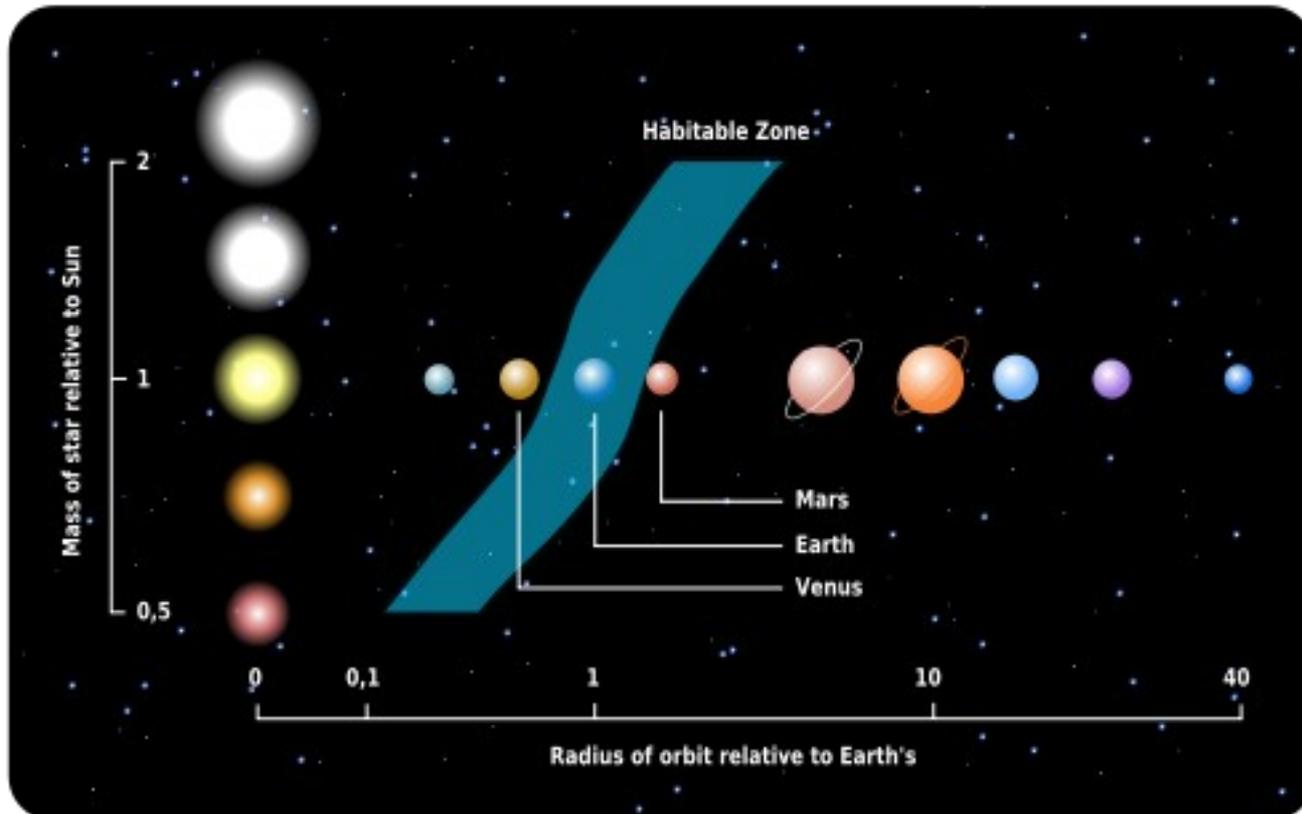
→ habitable zone is at ~300 AU

Proxima Centauri (M type star):

0.123 solar mass

1/600 Sun luminosity

→ habitable zone is at ~0.04 AU



# *How to identify exoplanets ?*

## **HIGH PRECISION OPTICAL MEASUREMENTS OF STARLIGHT (indirect techniques)**

*Earth around Sun at ~30 light year*

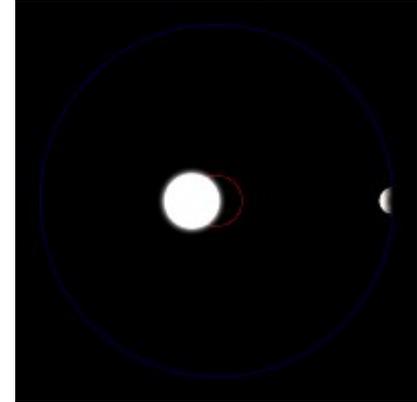
→ **Astrometry**: *measure star position moves by 0.3 micro arcsecond (thickness of a human hair at 20,000 miles)*

→ **Radial velocity**: *measure speed along line of sight Star velocity is modulated by 10cm / sec (changes light frequency by 1 part in 3,000,000,000)*

**Transit**: *measure star brightness*

*If Earth-like planet passes in front of Sun-like star, star dims by 70 parts per million*

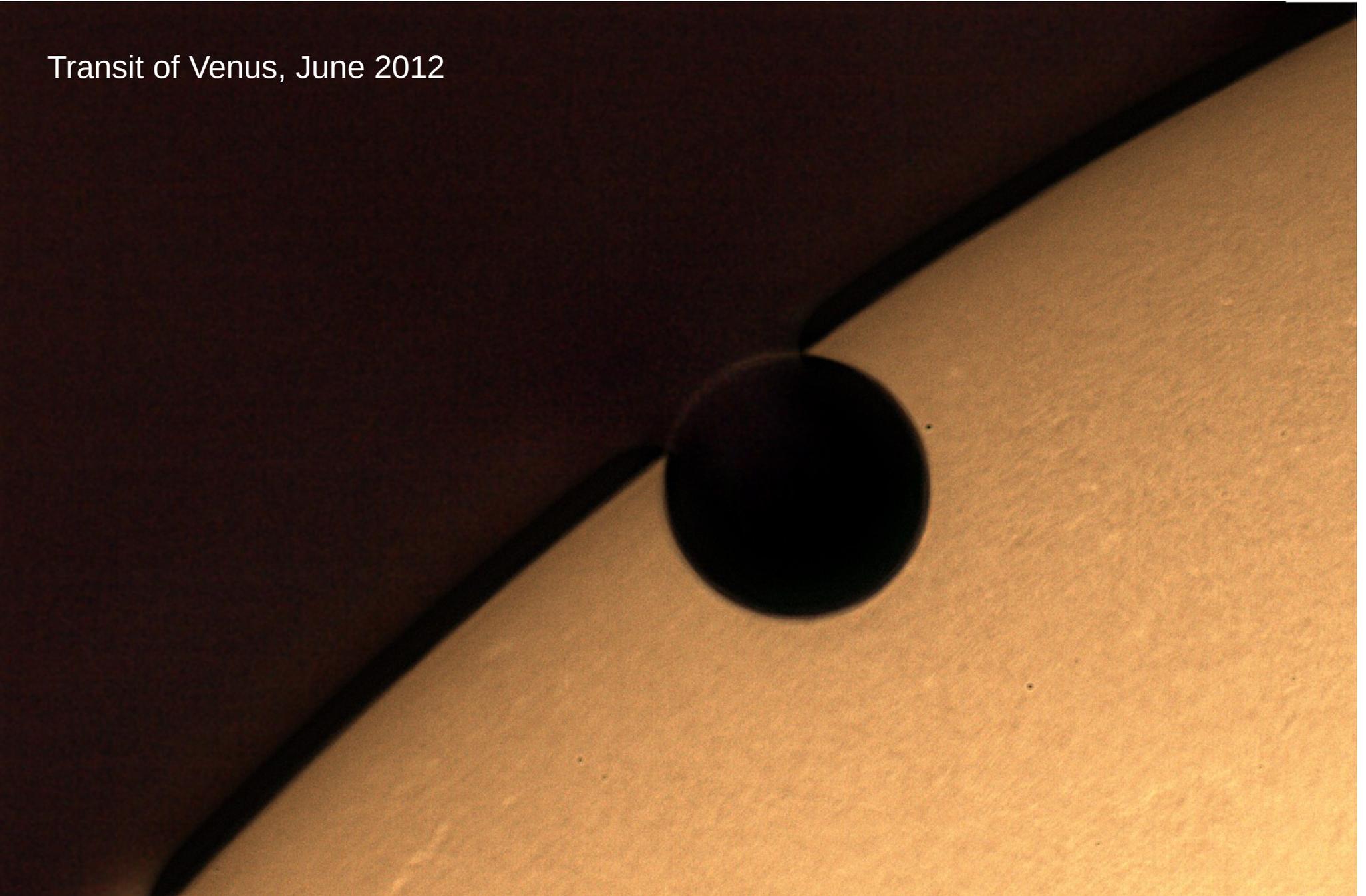
*(12x12 pixel going dark on a HD TV screen 70 miles away)*



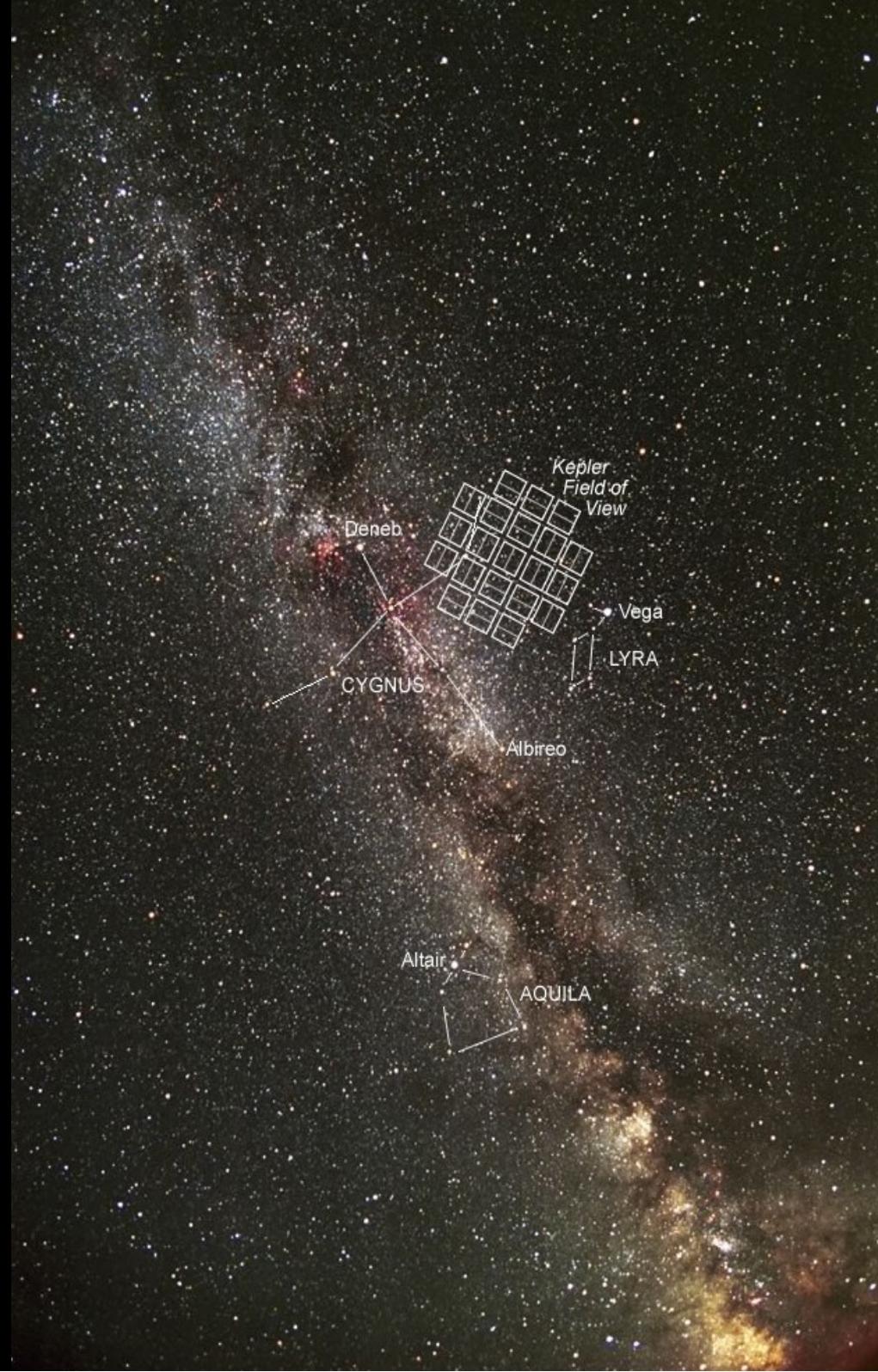
# ***Exoplanet transit***

*If the planet passes in front of its star, we see the star dimming slightly*

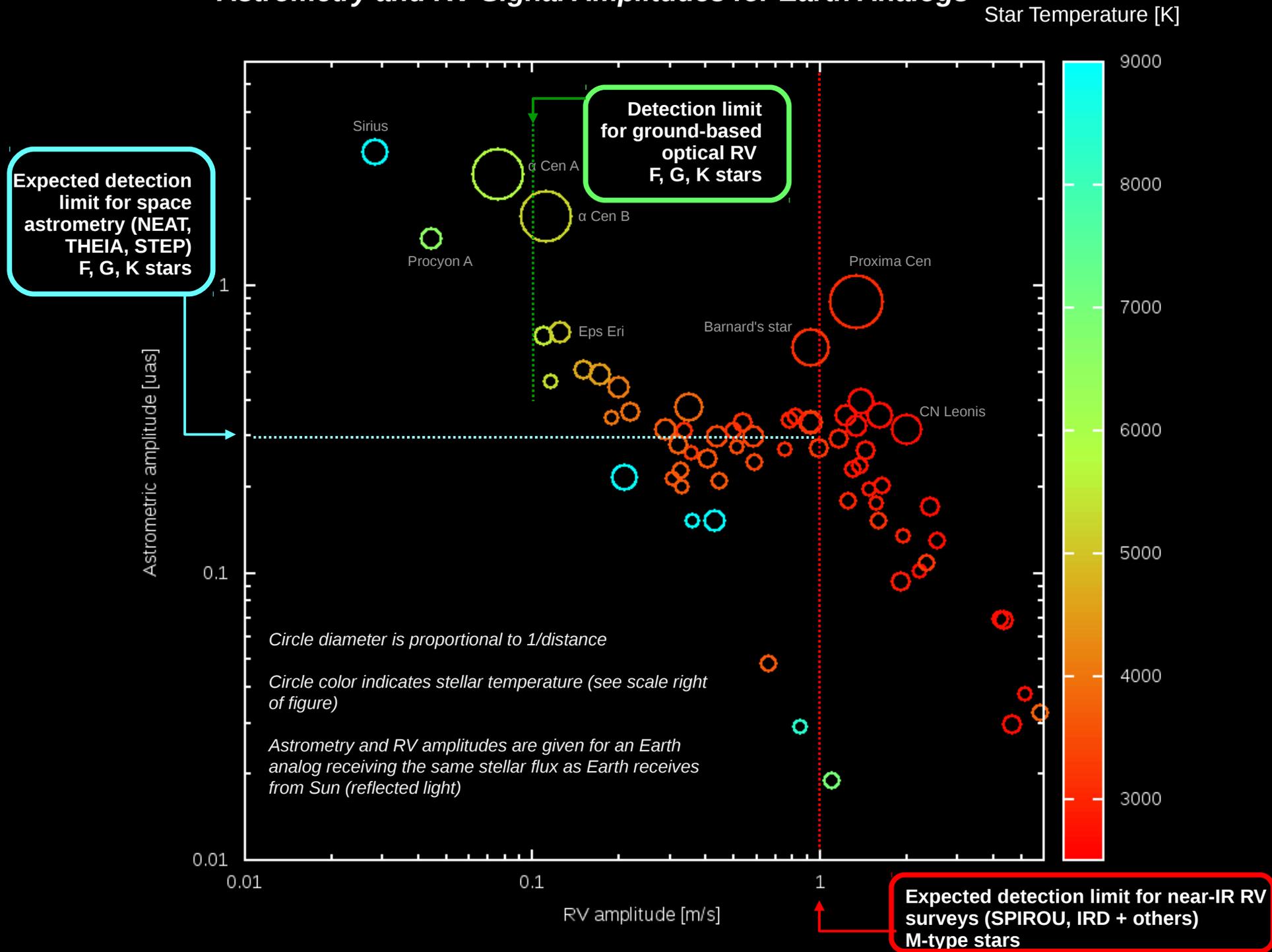
Transit of Venus, June 2012



# Kepler (NASA)



# Habitable Zones within 5 pc (16 ly): Astrometry and RV Signal Amplitudes for Earth Analogs

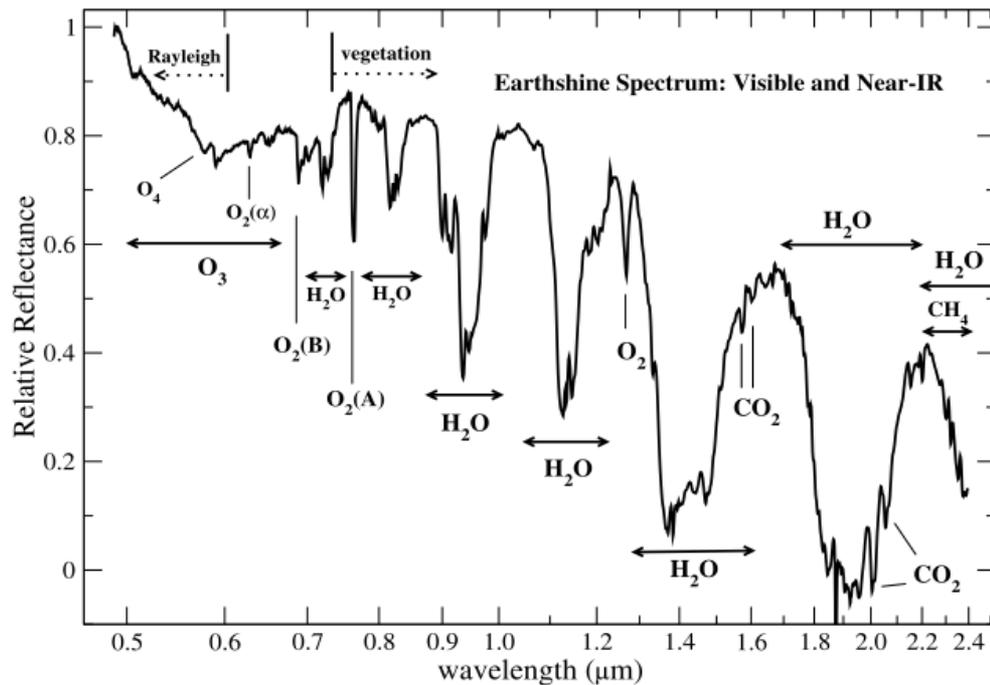


# Spectroscopy of Earth-like planets ... allows detection of biomarkers

Spectroscopy can identify biomarkers: molecular species, or combinations of species that can only be explained by biological activity

On Earth: water + O<sub>2</sub> + O<sub>3</sub> + CH<sub>4</sub>

Spectra of Earth obtained through Earthshine observation also reveals vegetation's red edge !



Turnbull et al. 2006



FIG. 7.—Earth's observed reflectance spectrum, at visible and near-infrared wavelengths, created from a composite of the data in this paper (0.8–2.4 μm) and the data presented in Paper I (0.5–0.8 μm). The strongest molecular signatures are indicated, as are the wavelengths where Rayleigh scattering and vegetation reflection are most significant.

# Direct imaging of Exoplanets (incl. Habitable planets) measures ...

Orbit

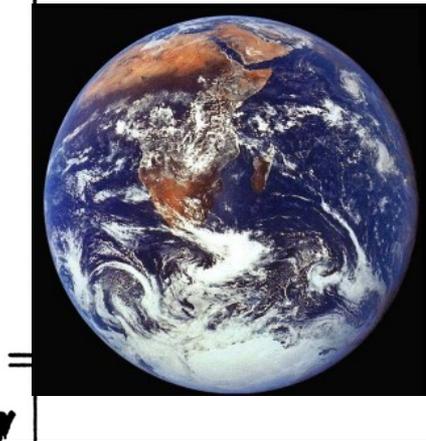
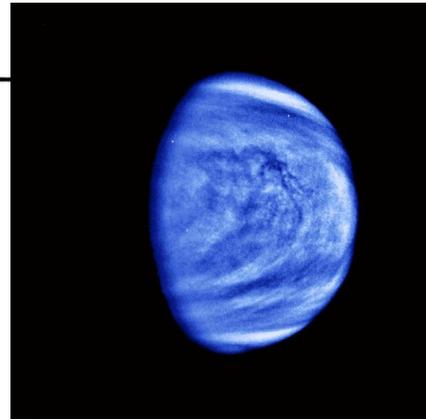
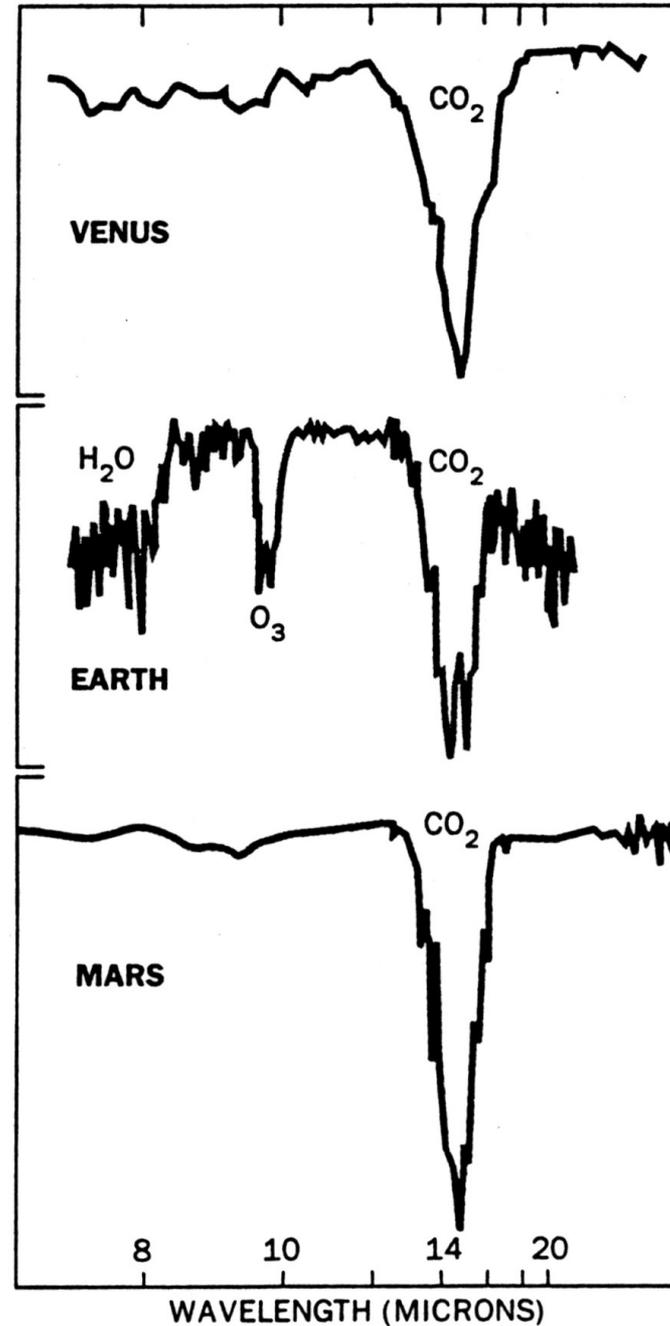
Atmosphere composition

Continents vs. Oceans ?

Rotation period

Weather patterns

Planetary environment :  
Planets + dust



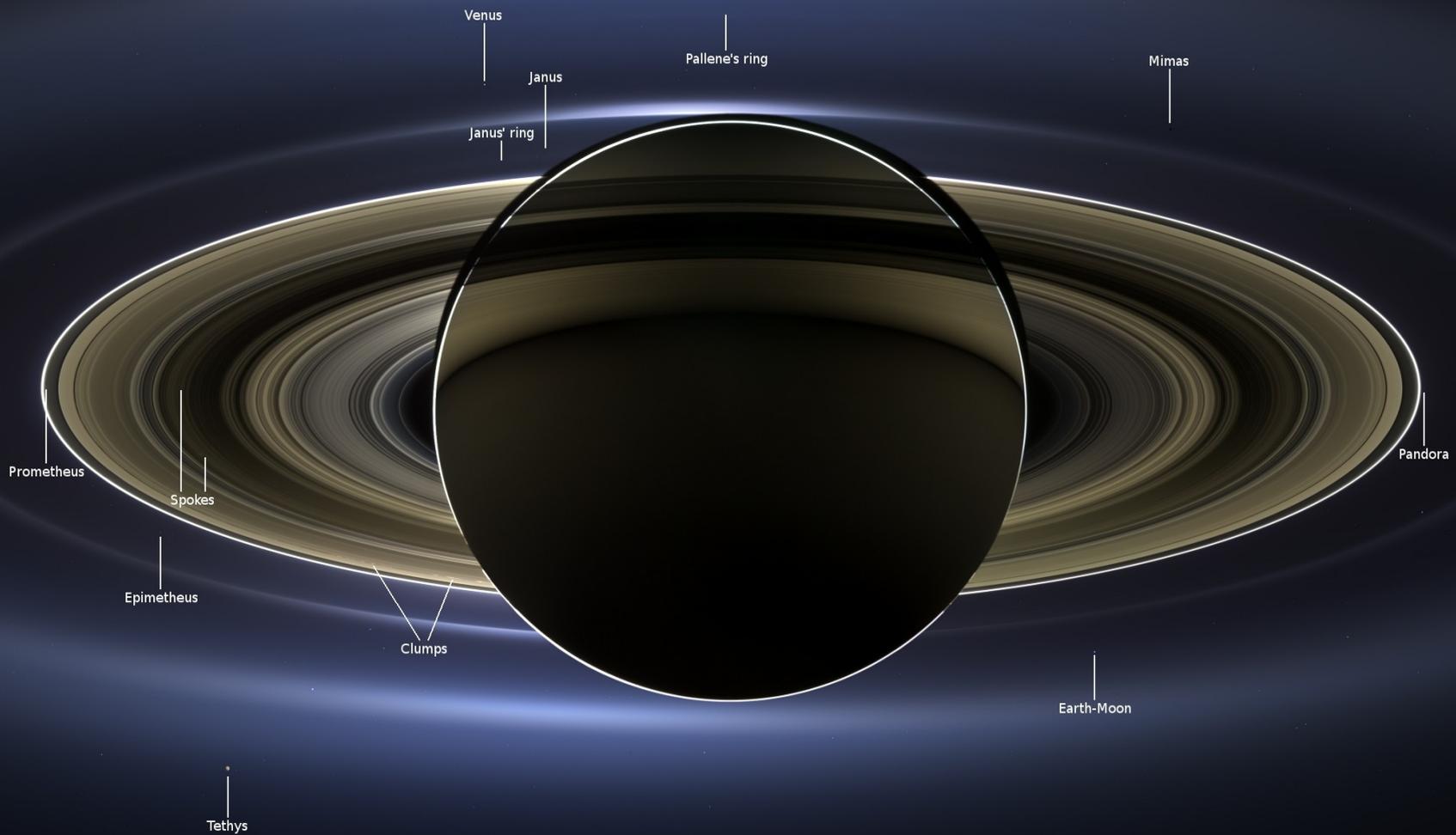
## Exoplanets imaging

### angular separation, contrast: why is it difficult ?

#### *What would our solar system look like from 10pc away ?*

- Sun would be  $m_V = 4.8$  star (faint naked-eye star)
- Sun diameter would be 0.001" (diffraction limit of a 200m telescope in the near-IR)
- Sun-Earth separation would be 0.1" (diffraction limit of a 2-3m telescope in the near-IR)
- Earth diameter = 0.00001" (diffraction limit of a 20km diameter telescope in near-IR)
- In the visible:
  - **Earth at 1e-10 contrast** would be  $m_V \sim 30$  sources (very faint, would be challenging even for Hubble without the host star)
  - Jupiter in the visible would be  $\sim 10x$  brighter than Earth, at 0.5"
  - Zodiacal light would be several 100x brighter than Earth when integrated, and brightest near Sun
- In the near IR ( $\sim 2 \mu\text{m}$ ): similar contrasts
- In the thermal IR ( $\sim 10 \mu\text{m}$ ):
  - Contrasts are much more favorable
  - Earth is brightest planet, at  $\sim 1e-6$  contrast

# Taking images of habitable exoplanets: Why is it hard?



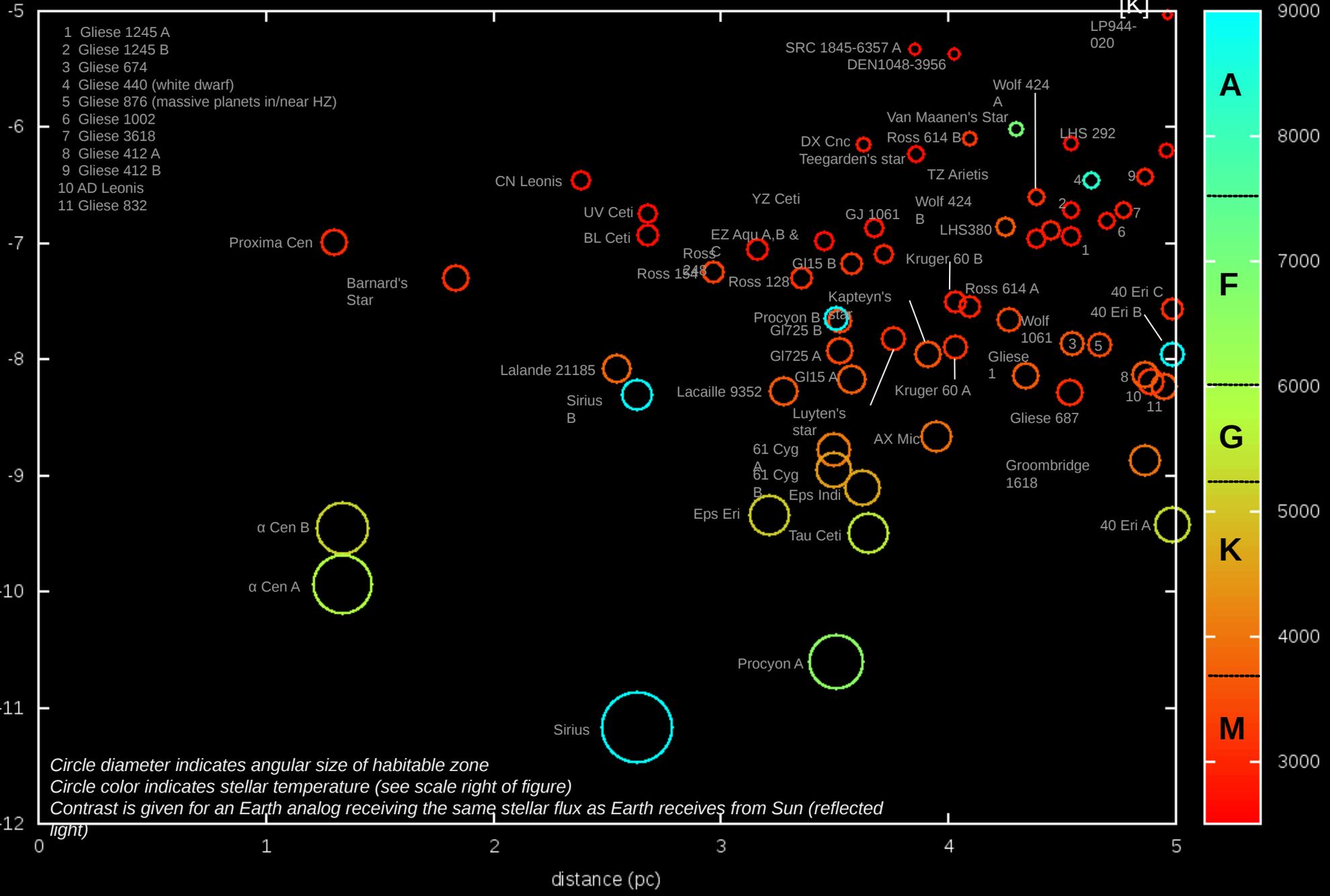


Saturn

↑  
Earth

# Habitable Zones within 5 pc (16 ly)

Star Temperature [K]



# Exoplanets: Contrast ratio, visible vs. infrared

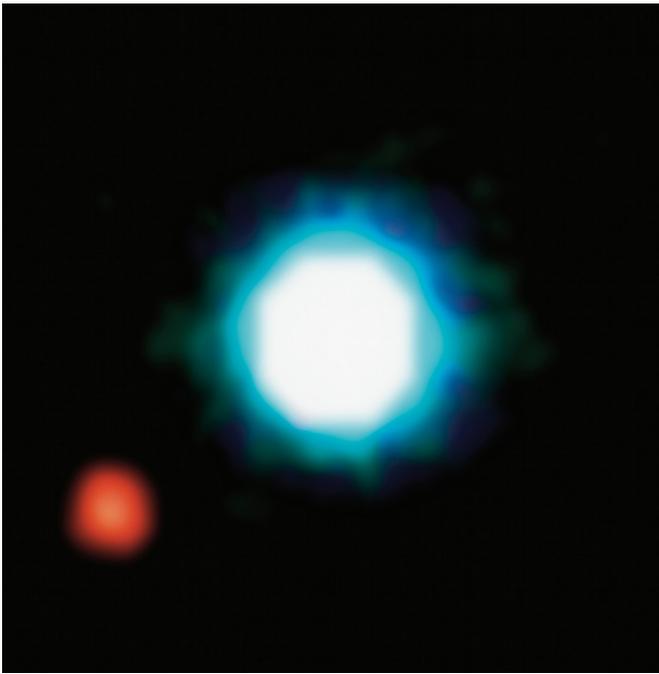
**In the visible**, planets are very faint unless they are very close to their star (luminosity goes as  $d^{-2}$ )

Planets in or near habitable zone cannot be imaged from the ground, and would require dedicated space telescope+instrument.

**In the near-IR**, giant and young planets (“young Jupiters”) can be imaged:

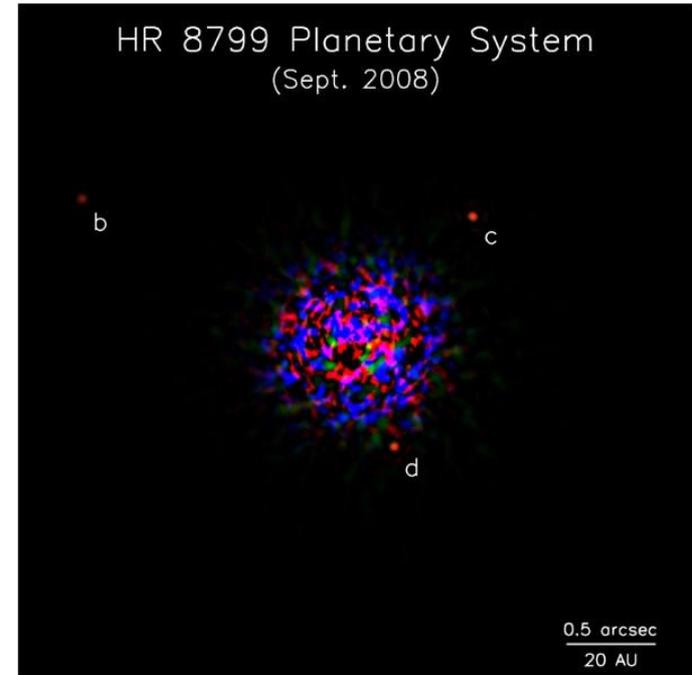
- AO systems work well in the near-IR
- Giant planets emit their own light (thermal emission)
- Young planets are still very hot, and slowly cool after formation

**In the Thermal IR** (~10  $\mu\text{m}$  & longer), contrast is even more favorable, and older giant planets can be imaged (this is one of the key science goals of JWST)



2M1207 exoplanet (Chauvin et al., ESO, 2004)  
Probably the first direct image of an exoplanet

HR8799: first image of exoplanetary system with multiple planets (Marois et al. 2009)



HR 8799 Planetary System (Sept. 2008)

0.5 arcsec  
20 AU

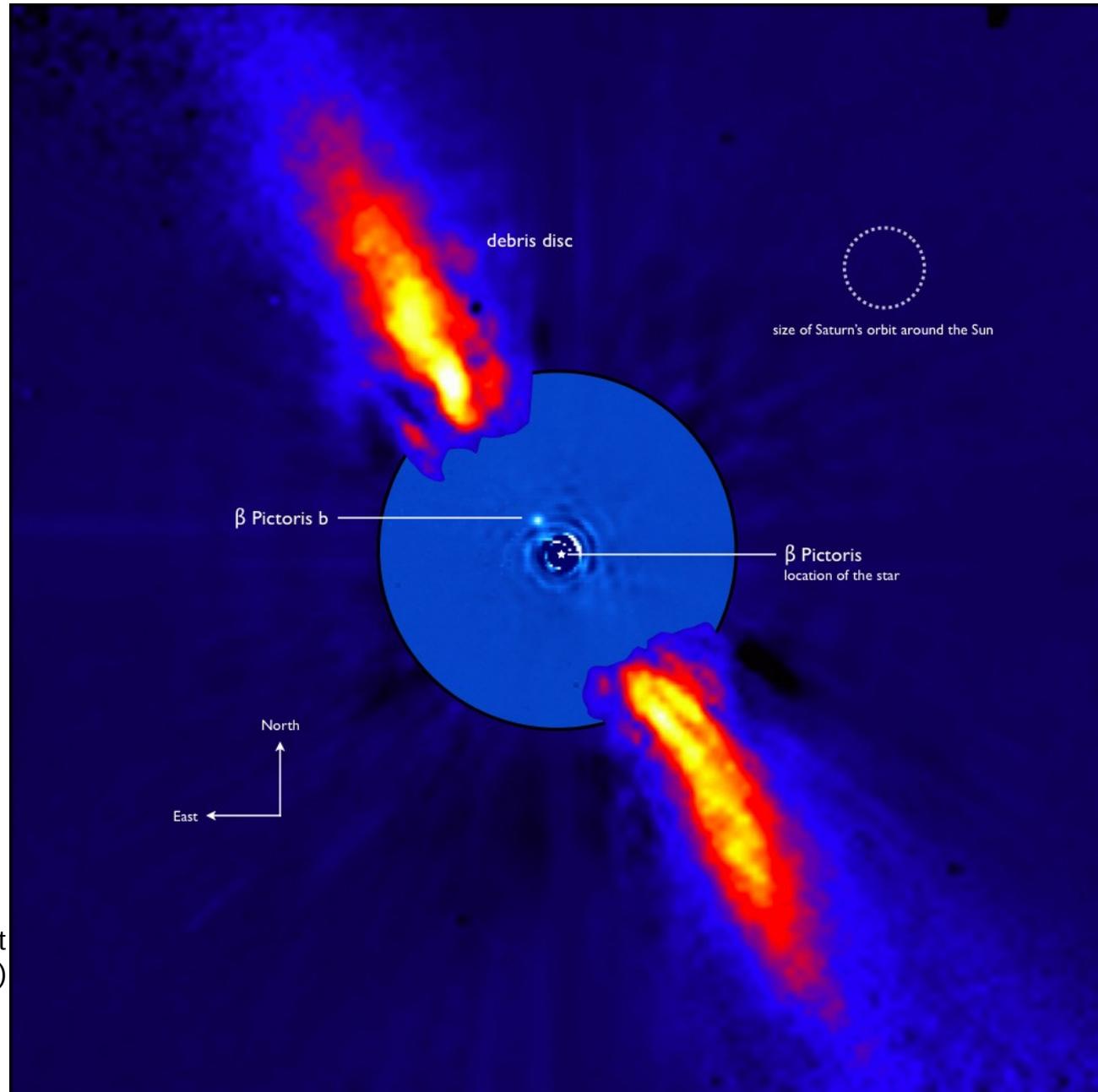
# Exoplanets & dust disks

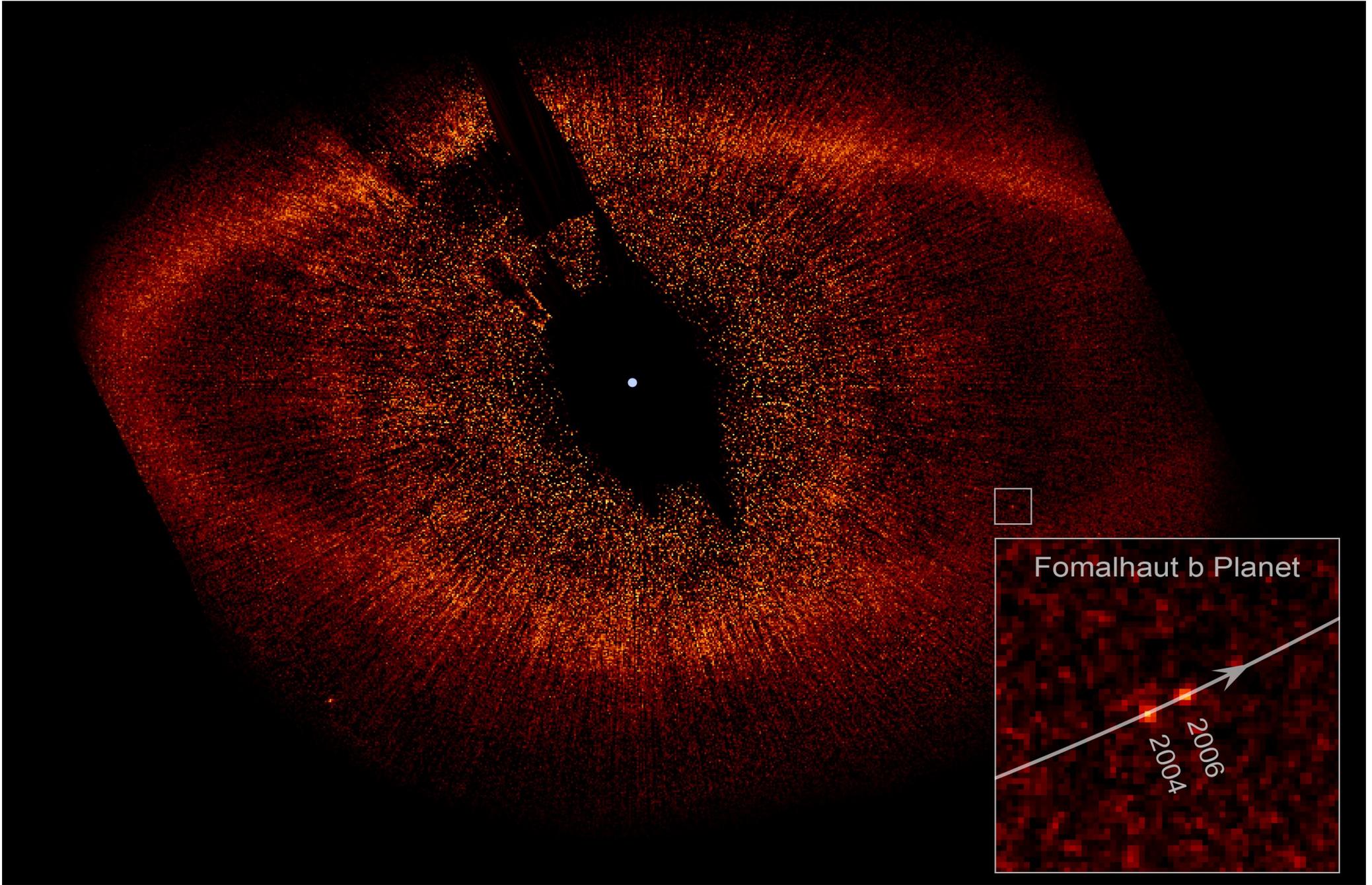
Protoplanetary disk:  
Disk in the process of forming planets

Debris disk:  
Disk generated by collision between small bodies

Ability to image planets and disks → study planetary formation and evolution of planetary systems

Beta Pic exoplanet and dust disk (Lagrange et al. 2009)





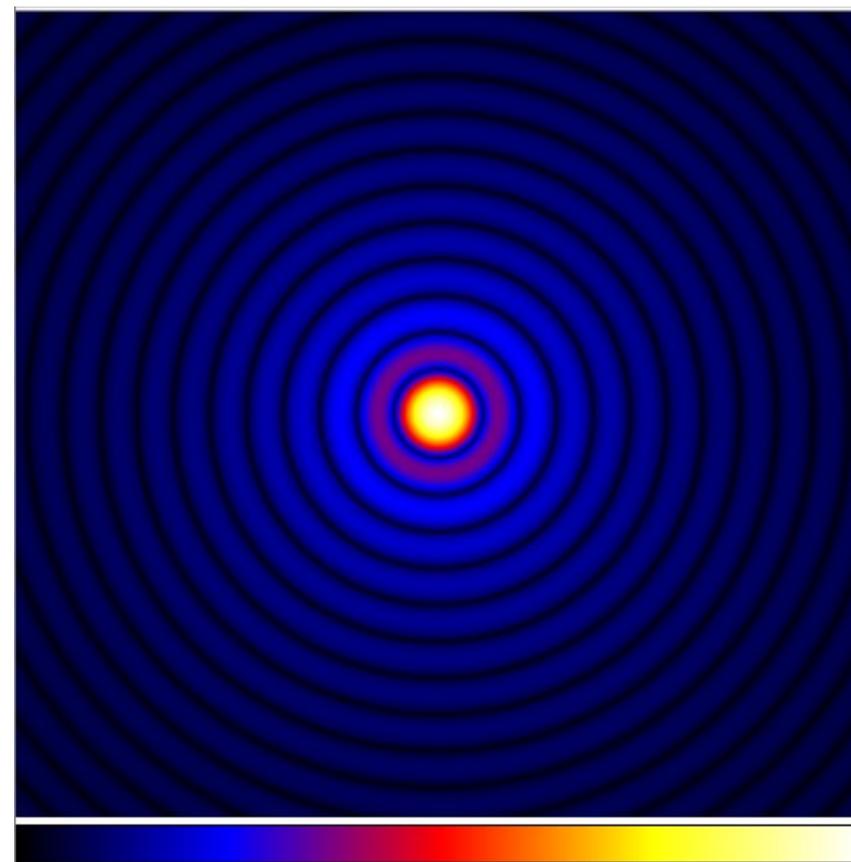
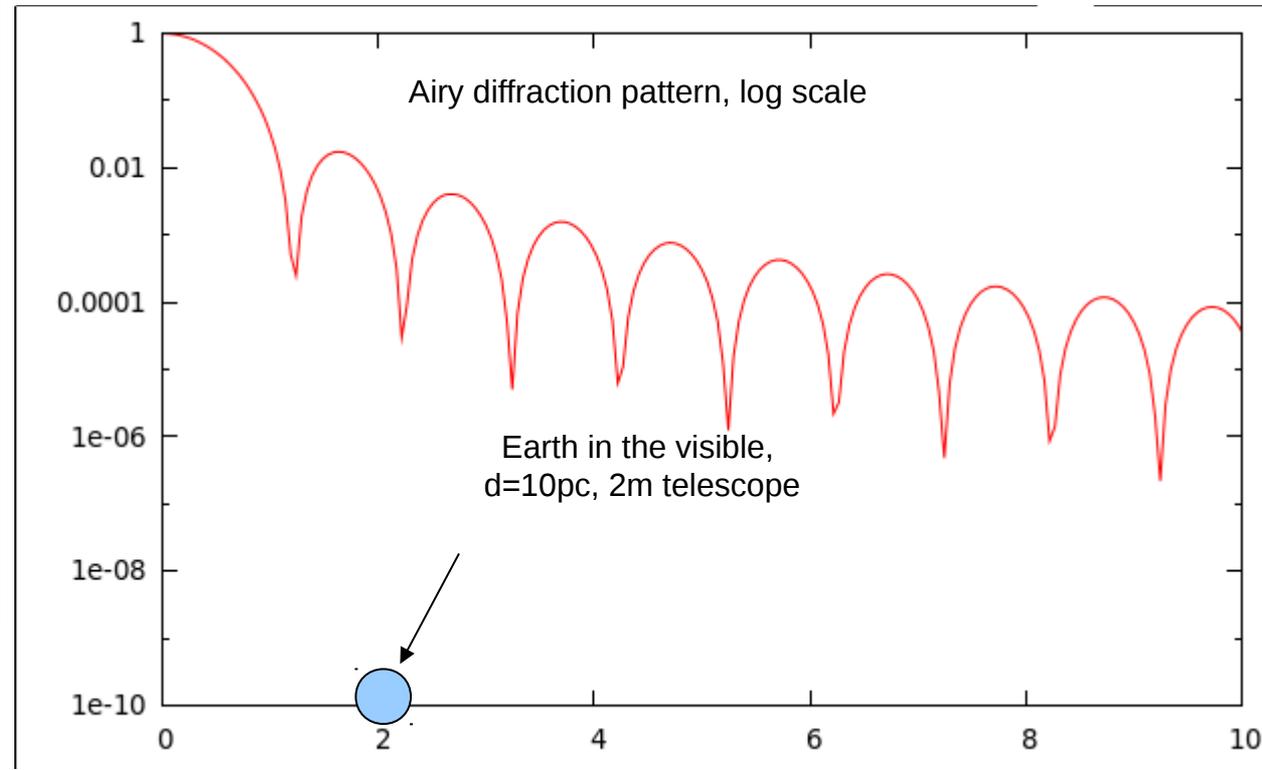
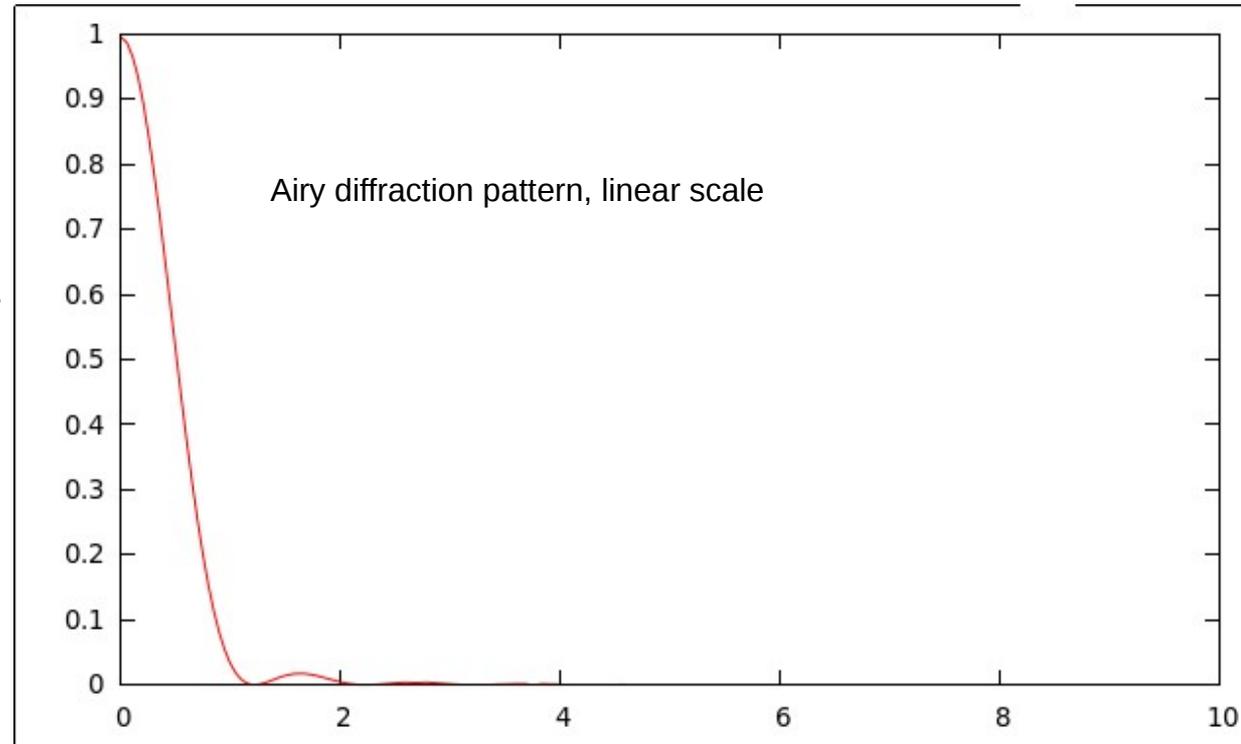
Kalas et al., HST image

# Coronagraphy



# Why coronagraphy ?

*Conventional imaging systems are not suitable for high contrast (even if perfect) due to diffraction*



# Why do we need coronagraphs ?

**Coronagraph can only remove known & static diffraction pattern**

**BUT:**

- static & known diffraction can be removed in the computer
- coronagraphs don't remove speckles due to WF errors

**Fundamental reasons:**

- (1) Photon Noise
- (2) Coherent amplification between speckles and diffraction pattern

**Practical reasons:**

- (3) Avoid detector saturation / bleeding
- (4) Limit scattering in optics -> "stop light as soon as you can"

# Coherent amplification between speckles and diffraction pattern

Final image = PSF diffraction (Airy) + speckle halo

This equation is true in complex amplitude, not in intensity. Intensity image will have product term -> speckles are amplified by the PSF diffraction.

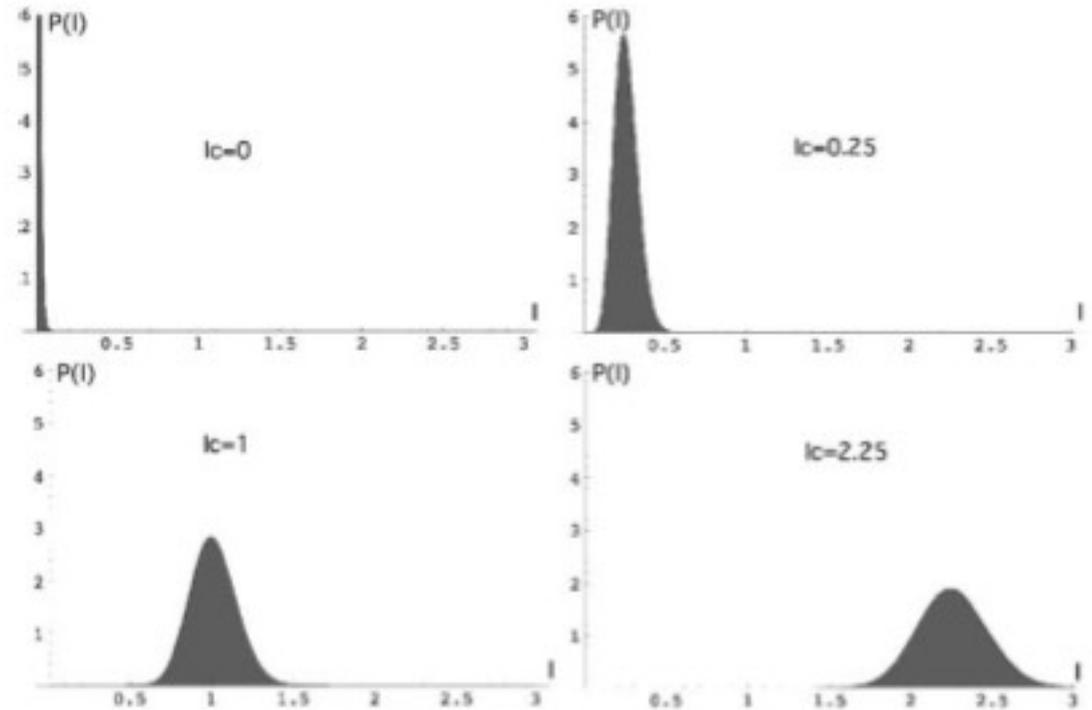


FIG. 3.—PDF of the light intensity at four different constant background intensity levels  $I_c$  and a single value of  $I_s = 0.1$ . High values of  $I_c$  correspond to locations near the perfect PSF maxima (rings), and low values of  $I_c$  correspond to locations near the zeros of the perfect PSF or far from the core. For  $I_c = 0$  we have the pure speckle exponential statistics. The width of the distribution increases with an increase in the level of  $I_c$ . This explains speckle pinning; speckle fluctuations are amplified by the coherent addition of the perfect part of the wave.

# Coherent amplification between speckles and diffraction pattern

Final image = PSF diffraction (Airy) + speckle halo

$$\begin{aligned} \text{Image} &= |A_{\text{PSF}} + A_{\text{speckles}}|^2 \\ &= |A_{\text{PSF}}|^2 + |A_{\text{speckles}}|^2 + 2 |A_{\text{PSF}}| |A_{\text{speckle}}| \cos(\theta) \end{aligned}$$

With PSF  $\gg$  Speckles, this term dominates speckles



# Coronagraph concepts & systems

Types of coronagraphs

Coronagraph systems & instruments



Olivier's thumb...  
the simplest coronagraph  
Doesn't work well enough to  
see planets around other stars

***Coronagraphs for imaging exoplanets are based on diffractive optics, not geometrical optics***

# What is light: particle or wave ?



1807: Thomas Young publishes his double-slit experiment result ... cannot be explained by Newton's corpuscular theory of light

1818: French academy of science committee launches a competition to explain nature of light



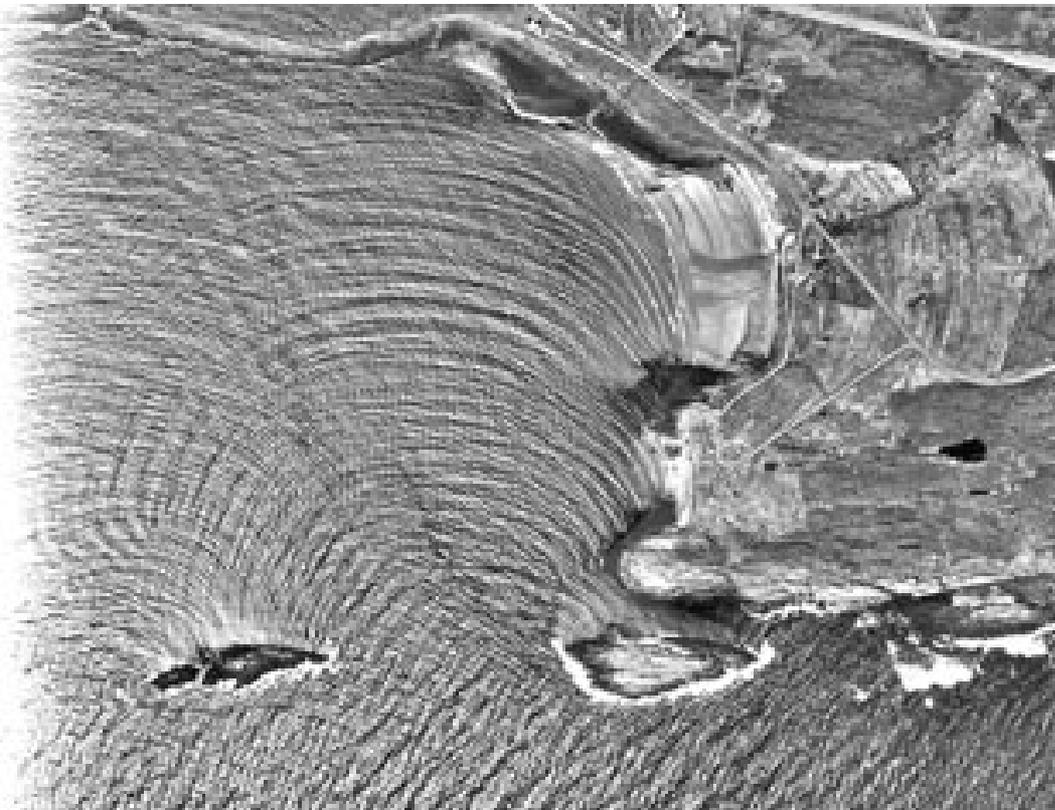
Augustin-Jean Fresnel submits wave theory of light

Simeon-Denis Poisson finds a flaw in Fresnel's theory: According to Fresnel's equations, a bright spot should appear in the shadow of a circular obstacle → this absurd result disproves Fresnel's theory

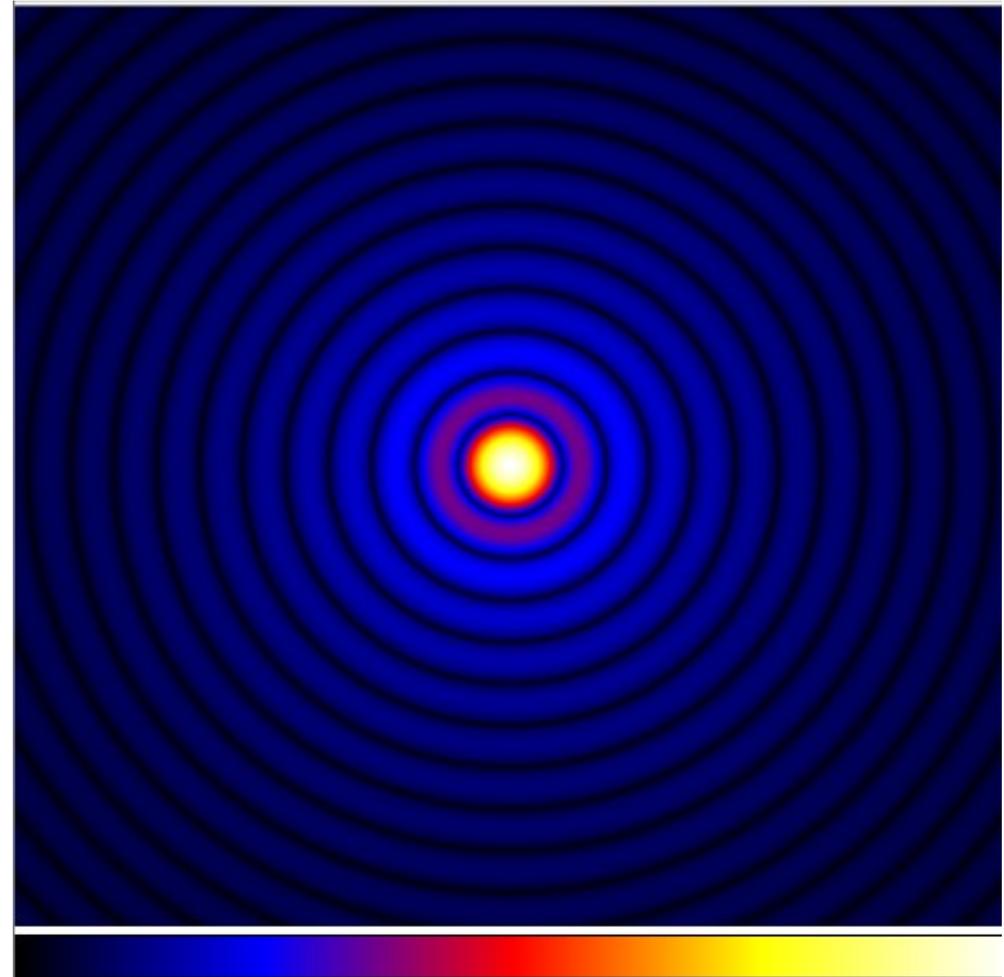
Dominique-Francois-Jean Arago, head of the committee, performs the experiment He finds the predicted spot → Fresnel wins the competition

# Water waves diffract around obstacles, edges, and so does light

→ designing a coronagraph is more complicated than simply putting an opaque mask at the star location in an image



Waves diffracted by coastline and islands



Ideal image of a distant star by a telescope  
Diffraction rings around the image core

# Types of Coronagraphs

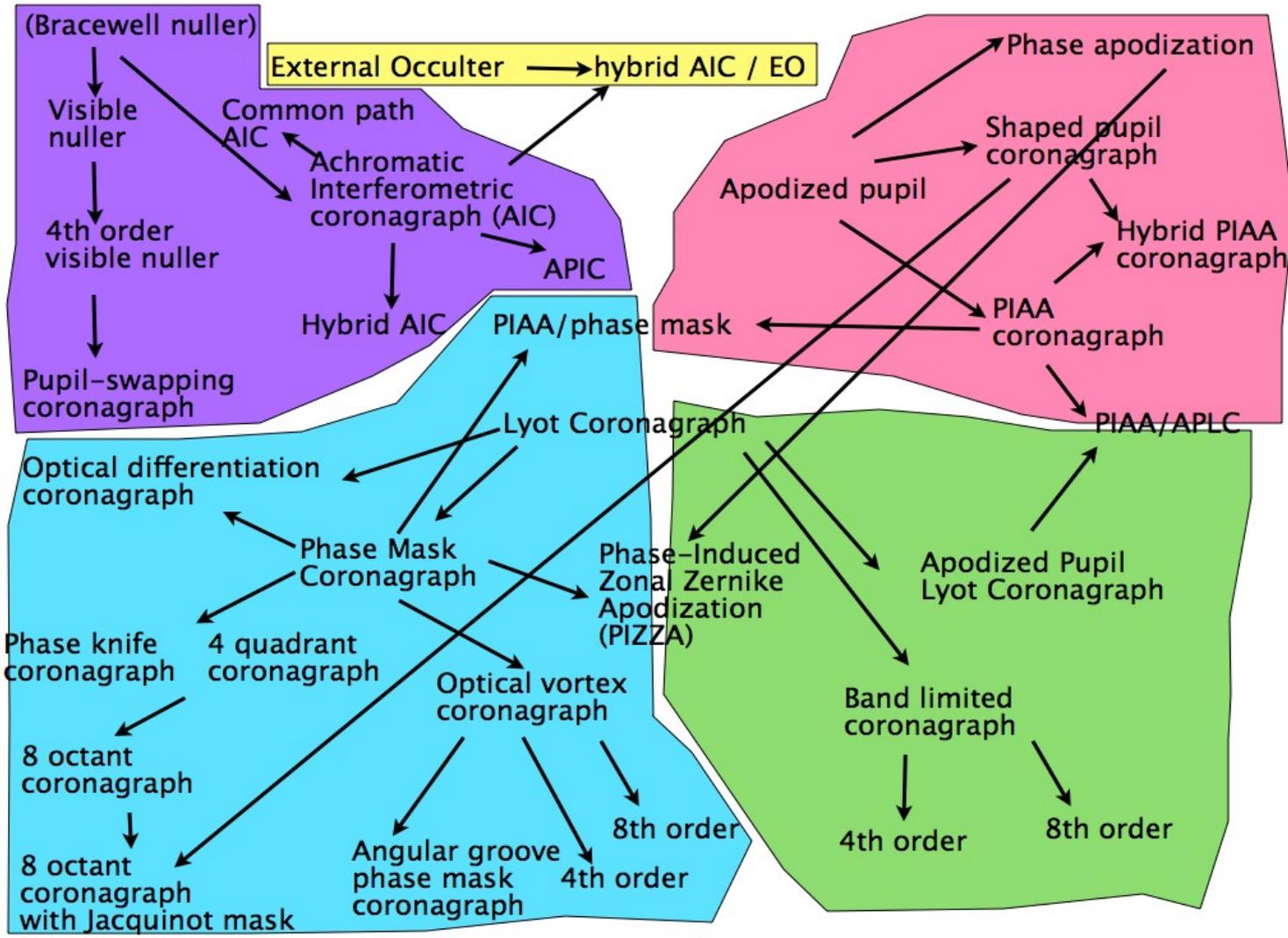
3 main approaches to remove starlight :

- Block starlight BEFORE it enters the telescope using a large **external occulter** ~50000 km in front of the telescope
- Design masks and optical components inside the telescope to induce starlight destructive interference at the expected location of a planet in the image: **internal coronagraph**
- Induce destructive interference between beams of multiple telescopes: **nulling interferometer**

# Internal Coronagraphs: main approaches

*Apodization*

*Beam splitting and destructive interference*



*Phase masks in focal plane*

*Amplitude masks in focal plane*

# **High Contrast Imaging systems**

# What is a high contrast imaging system (ground or space) ?

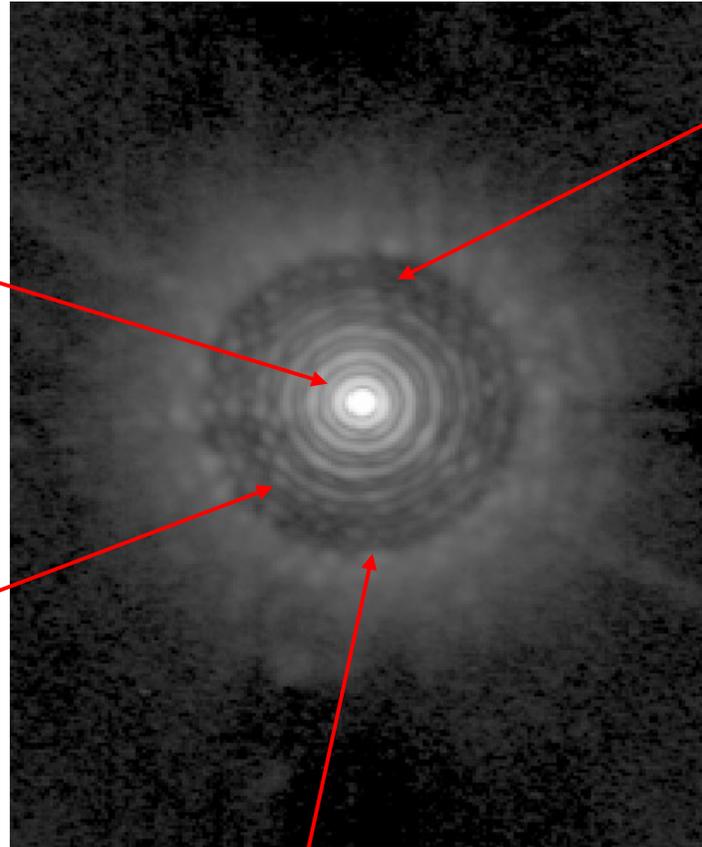
*Imaging system optimized to provide high contrast at small angular separation.*

## Key elements:

- **Coronagraph** or nulling interferometer to optically remove starlight and isolate planet light (overcomes diffraction)
- **Wavefront correction system** to reduce and calibrate residual wavefront errors
  - For coronagraphs: Extreme-AO system to flatten wavefront
  - For interferometers: Optical pathlength sensing / correction (+ AO on individual apertures of the interferometer)
- **Science detector (+ differential detection technique)** for imaging, spectroscopy and polarimetry
  - (note: the science detector can be part of the wavefront control system, and measure residual scattered light to be removed)

# From conventional AO to Coronagraphic Extreme-AO

We use a non-extreme AO system image as starting point  
Example of a very good PSF with a current AO system: LBT AO image



PSF diffraction  
(Airy rings, spiders)

**REMOVED BY  
CORONAGRAPH**

Static and slow  
speckles

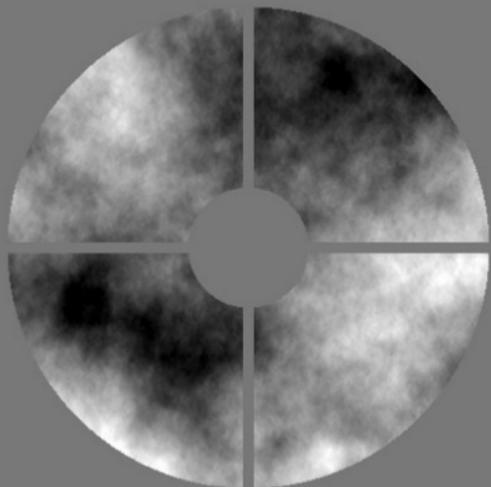
**MUST BE  
REMOVED BY  
CALIBRATION SYSTEM  
OR DIFFERENTIAL IMAGING  
(actively or in post  
processing)**

Residual atmospheric  
speckle halo

**REDUCED BY FAST,  
ACCURATE AND  
EFFICIENT AO SYSTEM**

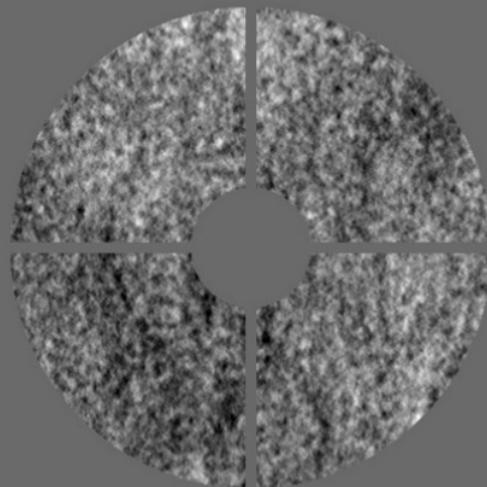
Control radius of AO  
**DEFINED BY NUMBER  
OF ACTUATORS IN DM:  
MAY BE INCREASED WITH  
MORE ACTUATORS IF REQUIRED**

1186 nm RMS



No AO correction

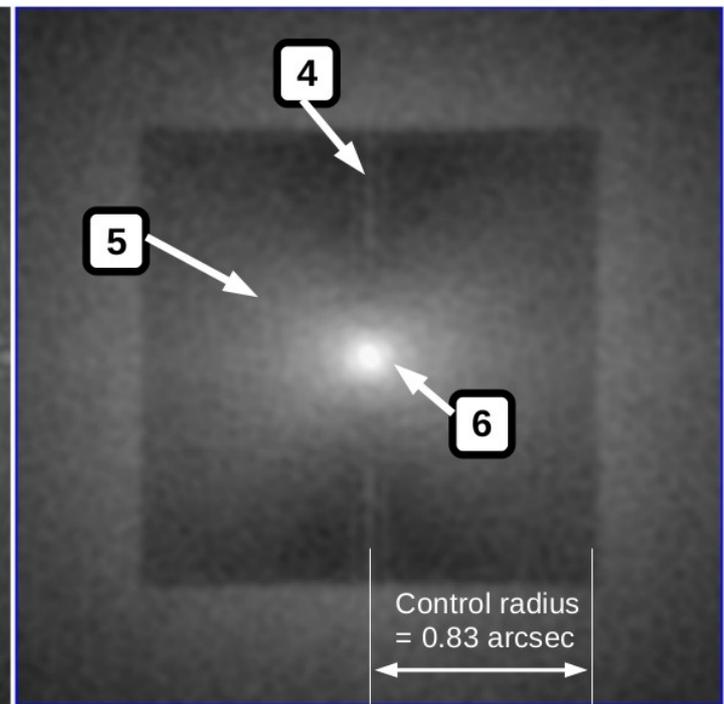
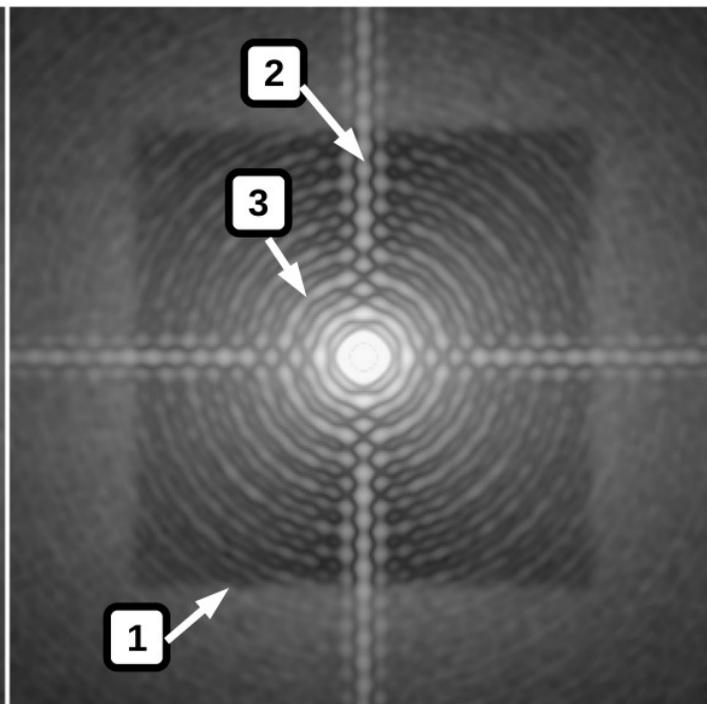
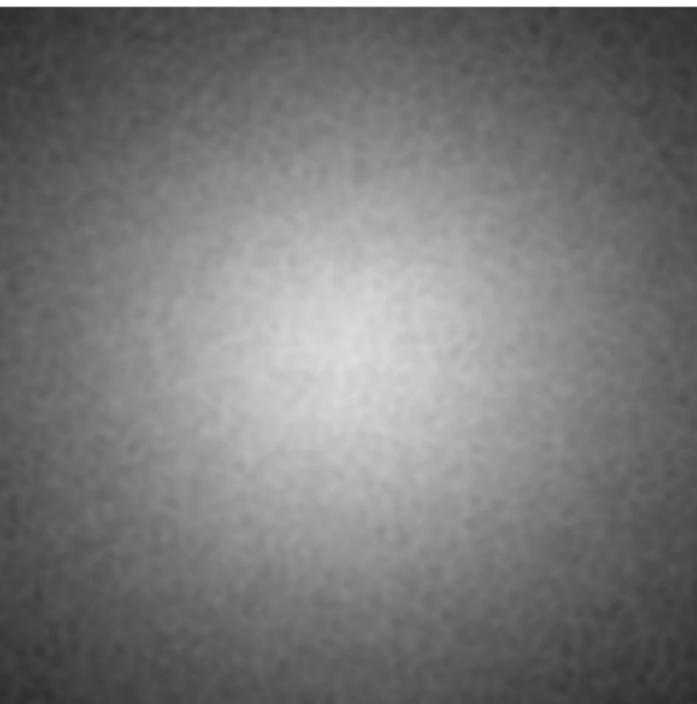
141 nm RMS



Extreme-AO correction

- 1: ExAO control radius
- 2: Telescope spider diffraction
- 3: Diffraction rings
- 4: Ghost spider diffraction
- 5: "butterfly" wind effect
- 6: Coronagraphic leak (low order aberrations)

Monochromatic PSFs, 1.65um  
 No photon noise  
 10m/s wind speed, single layer  
 4ms wavefront control lag



-4.7      -4.4      -4.1      -3.8      -3.5      -3.2      -2.9      -2.6      -2.3

Contrast (10-base log)

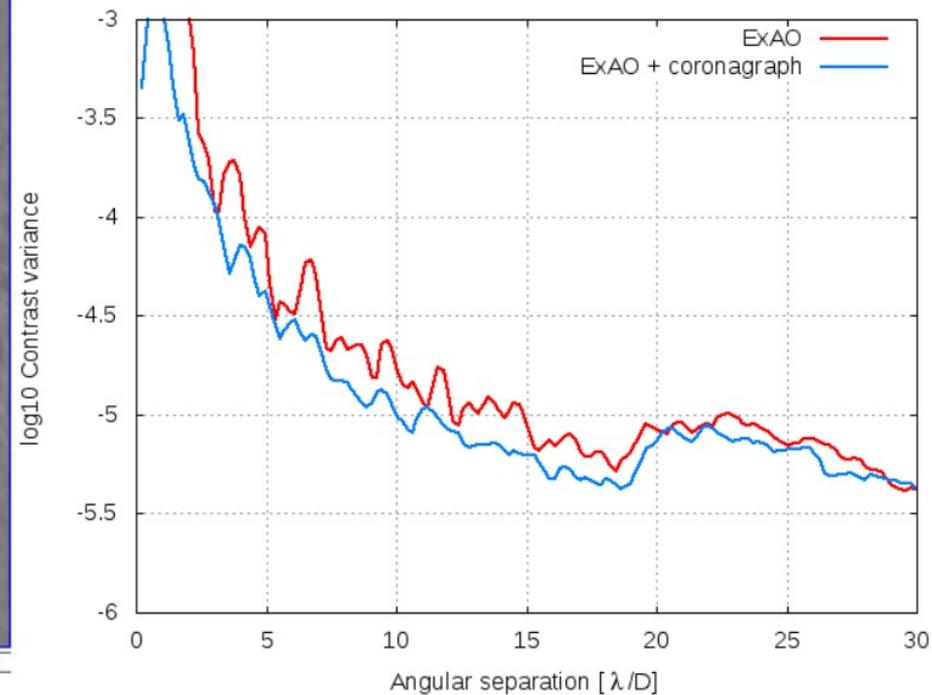
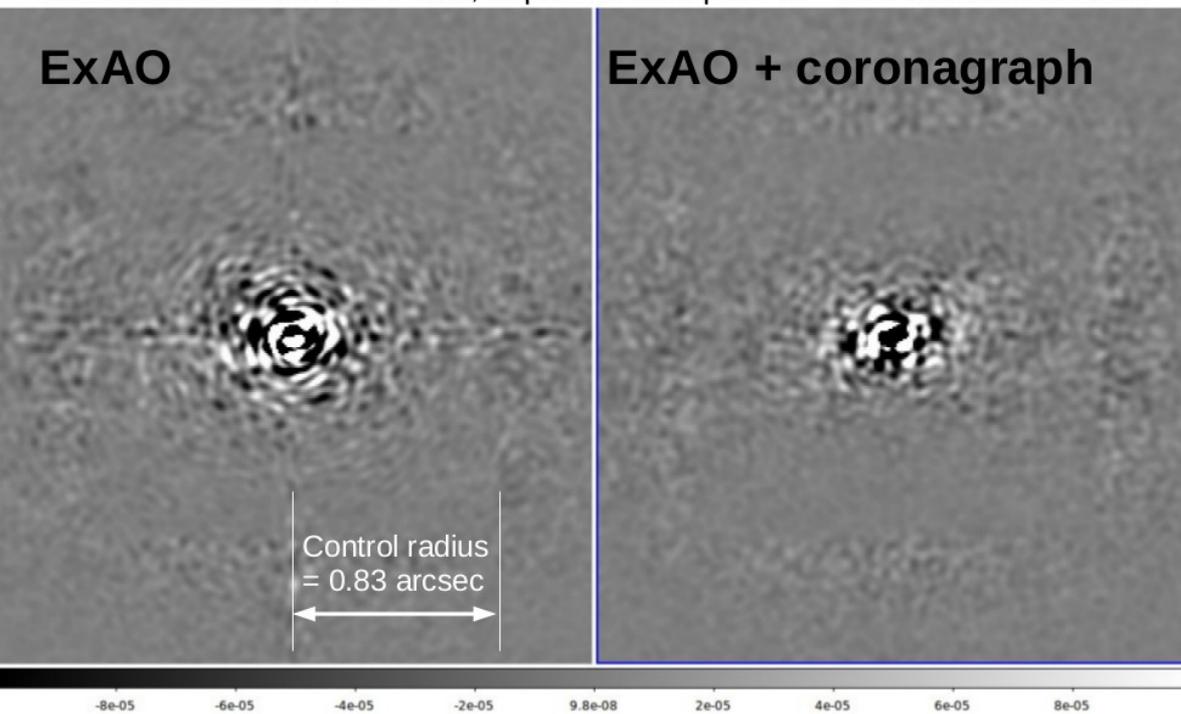
# Coronagraphs reduce speckle noise

“speckle pinning” effect

See: Bloemhof et al. 2001, Aime & Soummer 2004, Soummer et al. 2007

## PSF subtraction residual (no photon noise)

Difference between two PSFs, exposure time per PSF=100 coherence times



# Current and future high contrast systems - ground

**Subaru Coronagraphic Extreme AO** – under operation and development

Small inner working angle **PIAA coronagraph**

Pointing sensing and control with **coronagraphic low order WFS**

**Speckle control** using focal plane image as sensor

**2000-element deformable mirror**

Includes **Integral Field Spectrograph** to help remove speckles and acquire spectra

**Gemini Planet Imager (GPI)** – **large survey** starts observations in 2014

**ExAO system using 64x64 MEMS DM** + coronagraph

Includes **calibration interferometer** to accurately measure residual speckles

Includes Integral Field Spectrograph to help remove speckles and acquire spectra

**ESO's SPHERE on VLT** – **large survey** starts observations in 2014

ExAO system + coronagraph

Highly stable bench

Includes Integral Field Spectrograph to help remove speckles and acquire spectra

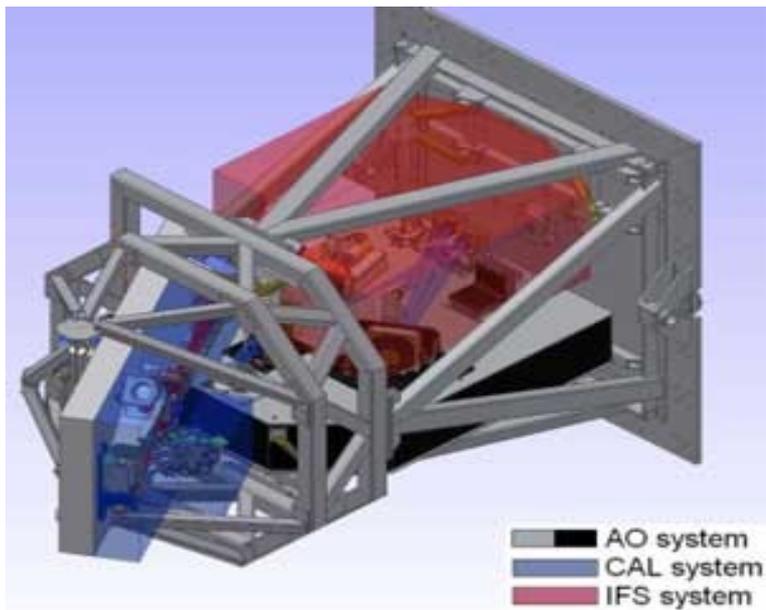
Includes **differential polarimetric imager**

**MagAO-X** – under development for 6.5m Magellan Telescope

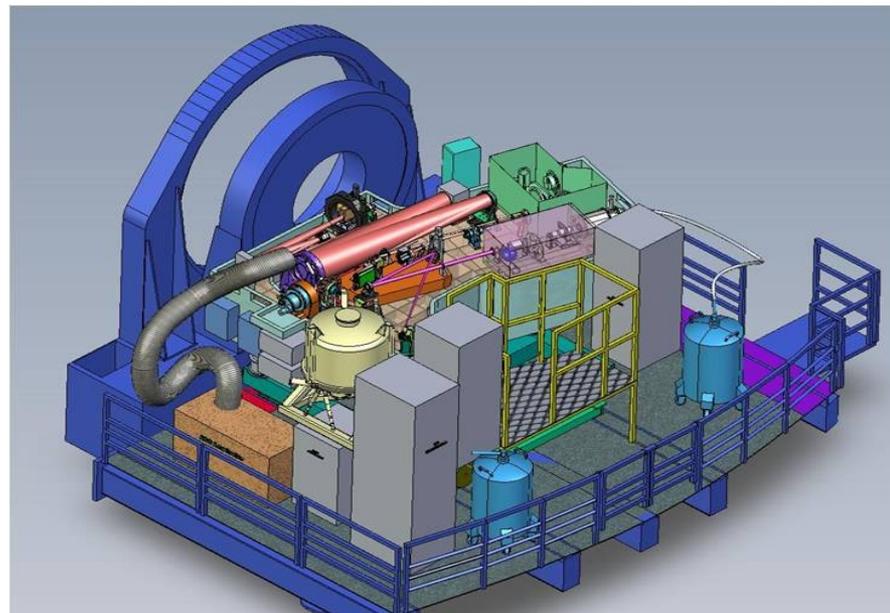
High speed, high efficiency ExAO system, visible light optimized, **2000 elements**

Small IWA coronagraph (PIAACMC + other modes)

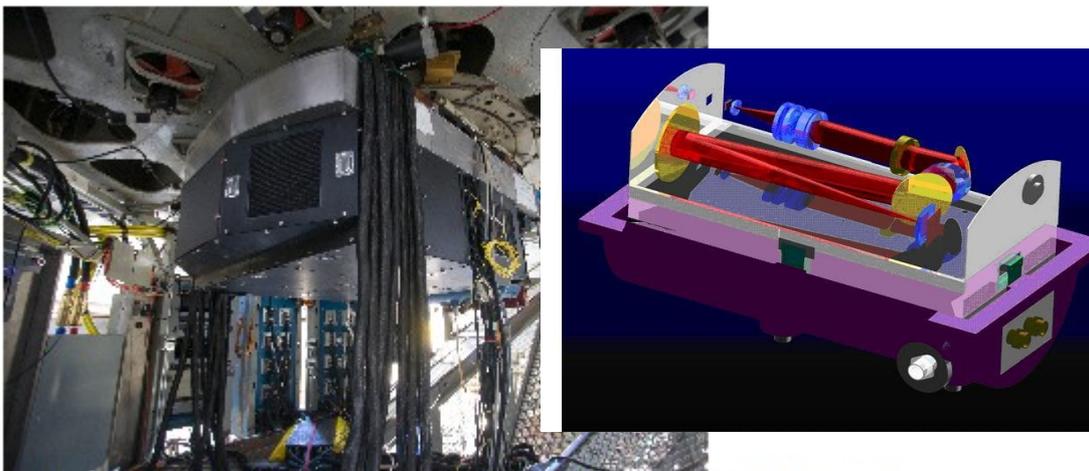
# Current and future high contrast systems - ground



Gemini Planet Imager

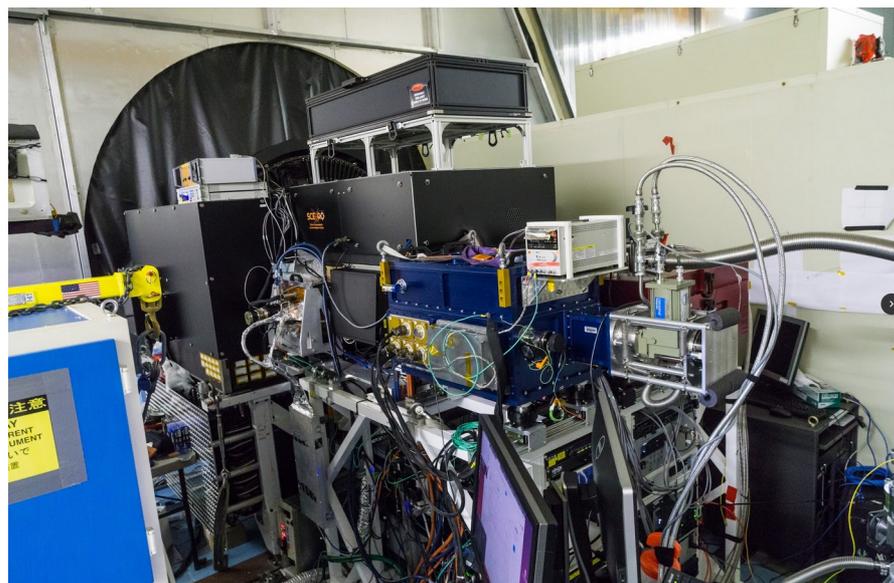


SPHERE (European Southern Observatory)



PALM-3000 installed at the Cass focus of the Hale Telescope at Palomar Mountain. Photo: Scott Kardel.

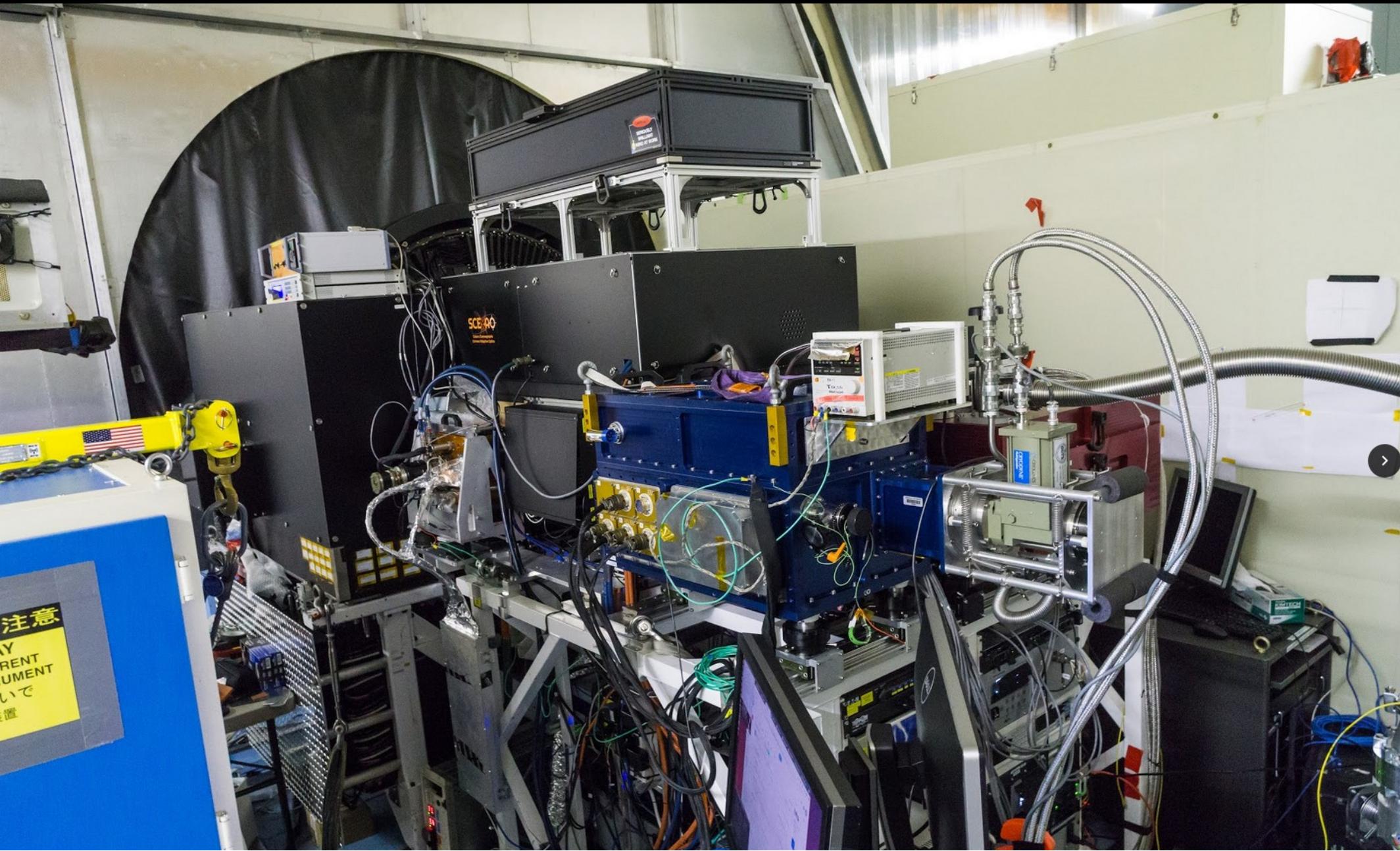
PALM3000/P1640 (Palomar 5-m Telescope)



Subaru Coronagraphic Extreme-AO<sup>3</sup>

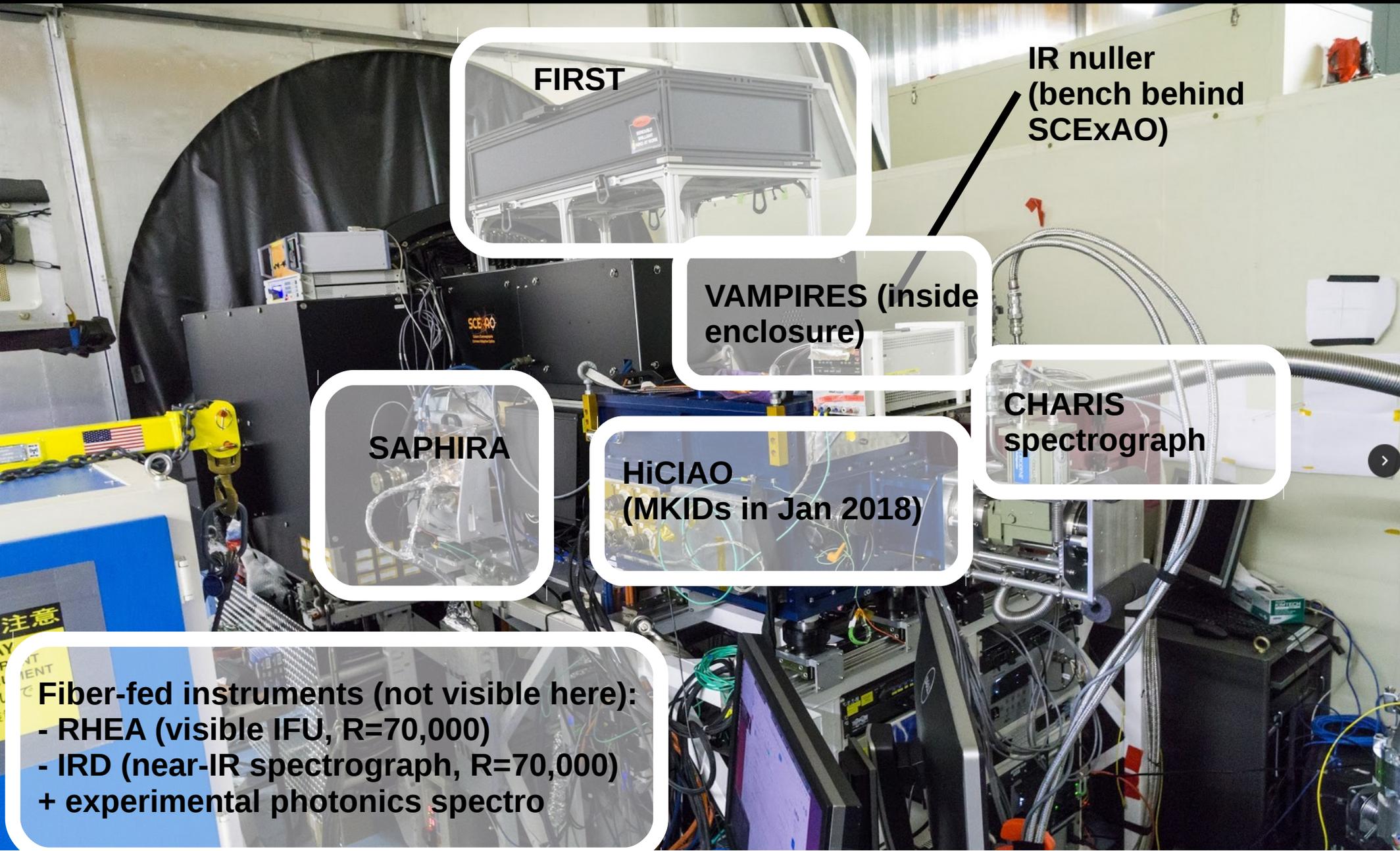


# Subaru Coronagraphic Extreme Adaptive Optics

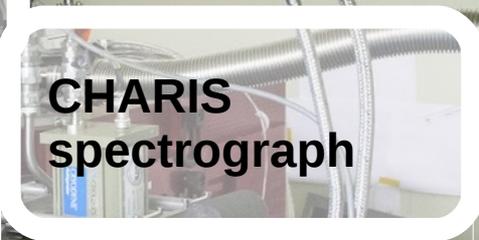




# Subaru Coronagraphic Extreme Adaptive Optics



IR nuller  
(bench behind  
SCEXAO)

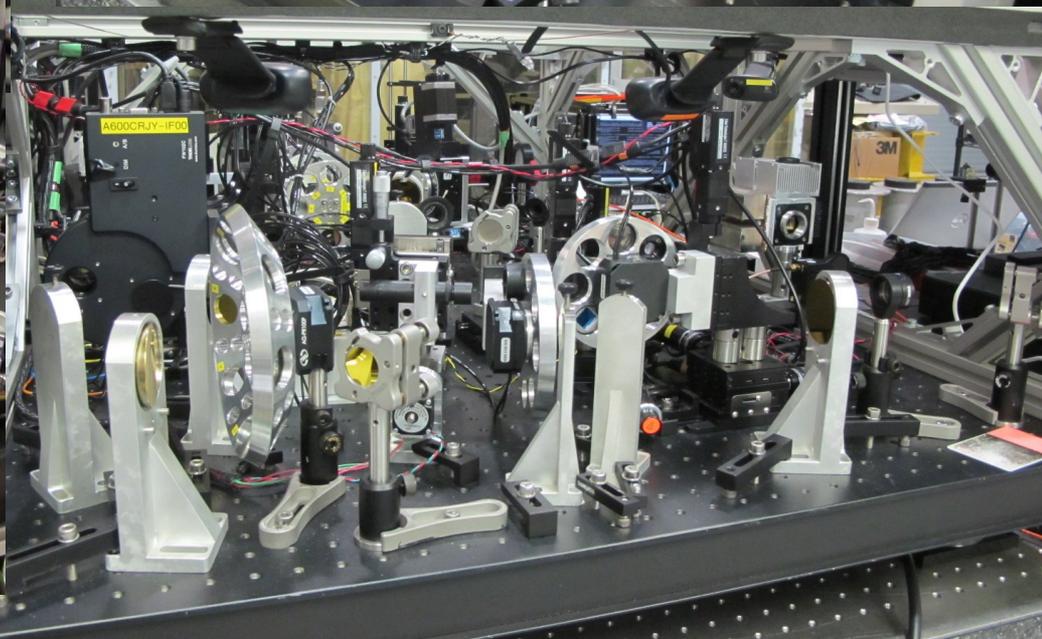
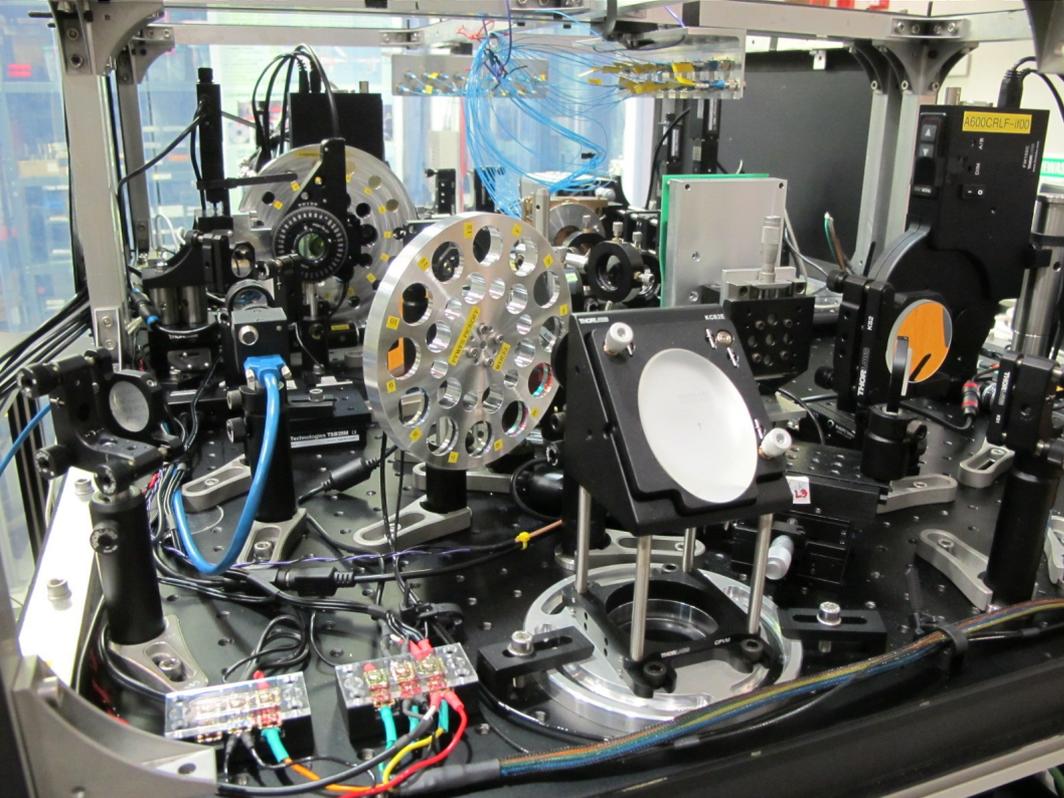
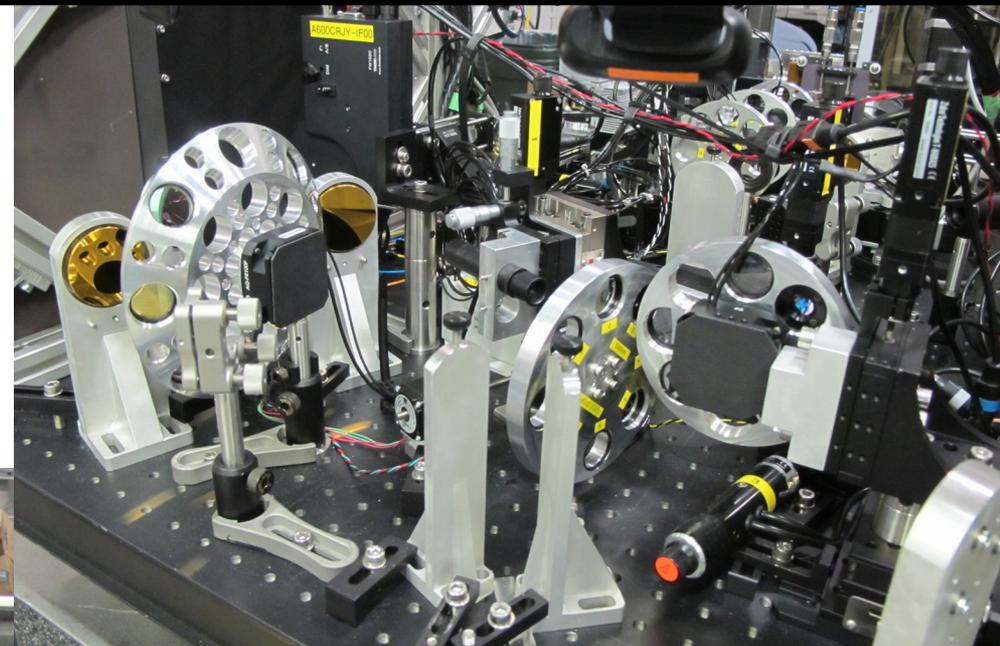
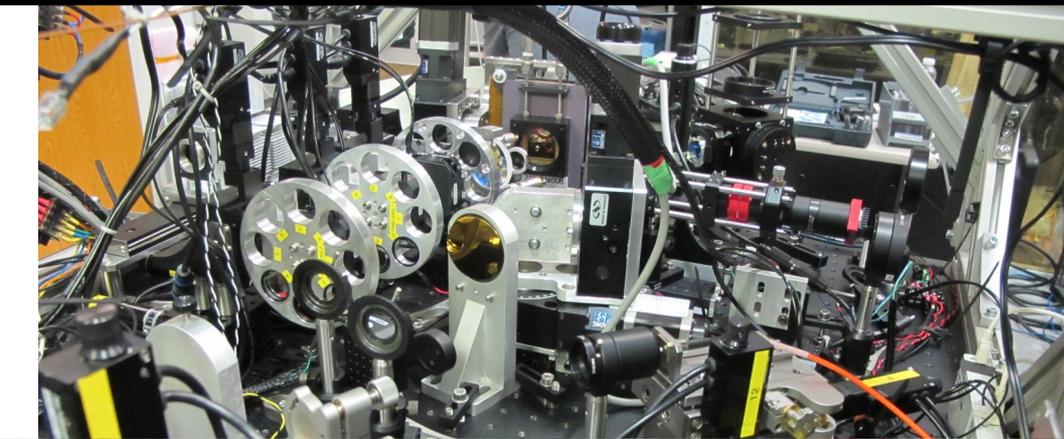


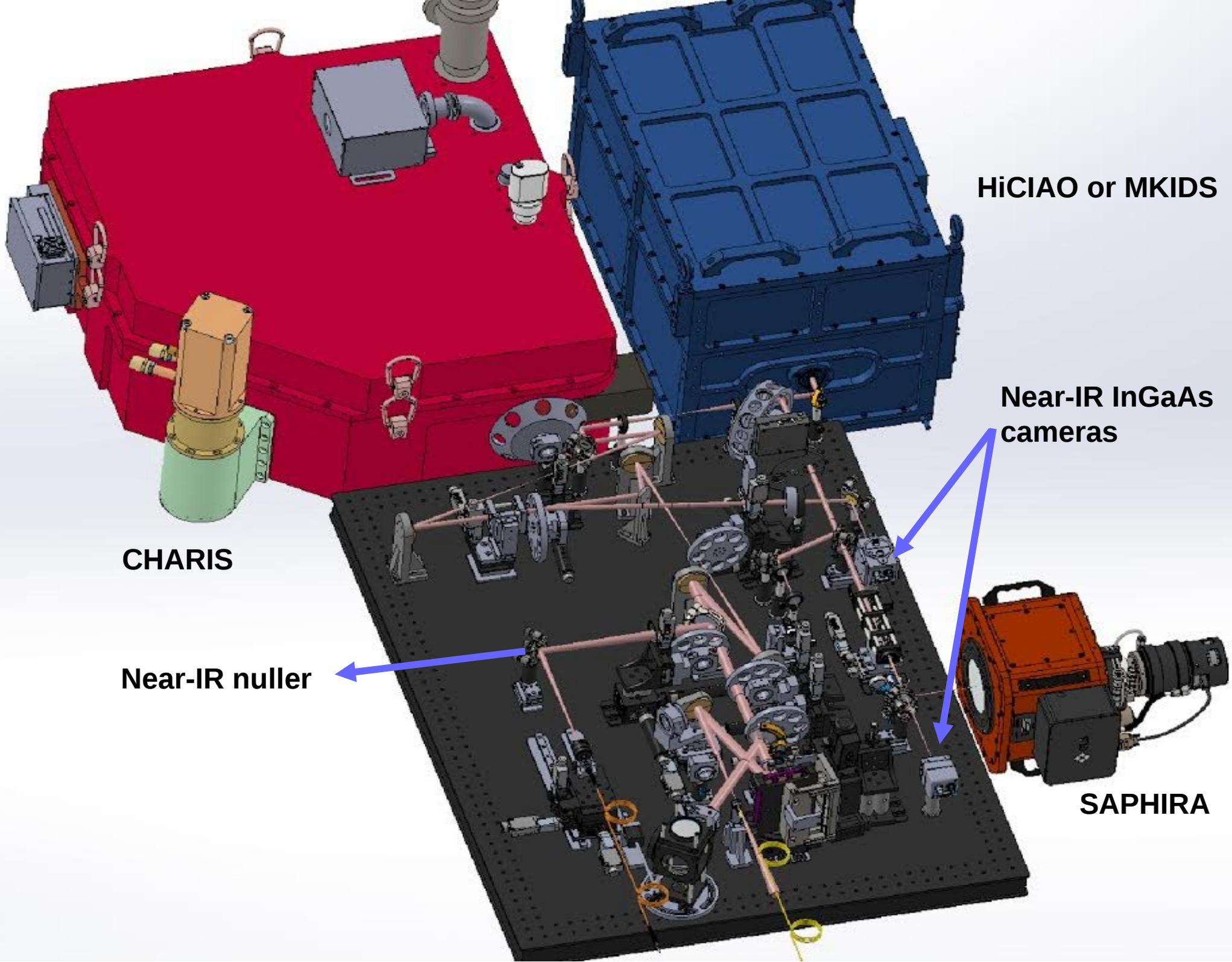
Fiber-fed instruments (not visible here):

- RHEA (visible IFU, R=70,000)
- IRD (near-IR spectrograph, R=70,000)
- + experimental photonics spectro



# Subaru Coronagraphic Extreme Adaptive Optics





HiCIAO or MKIDS

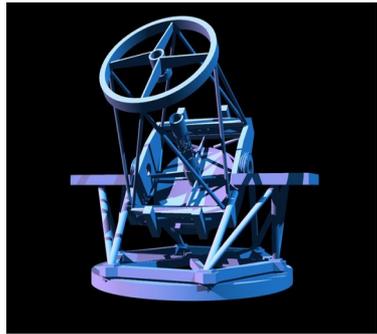
Near-IR InGaAs  
cameras

CHARIS

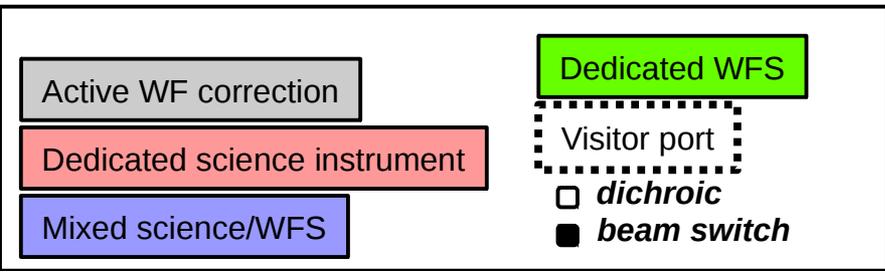
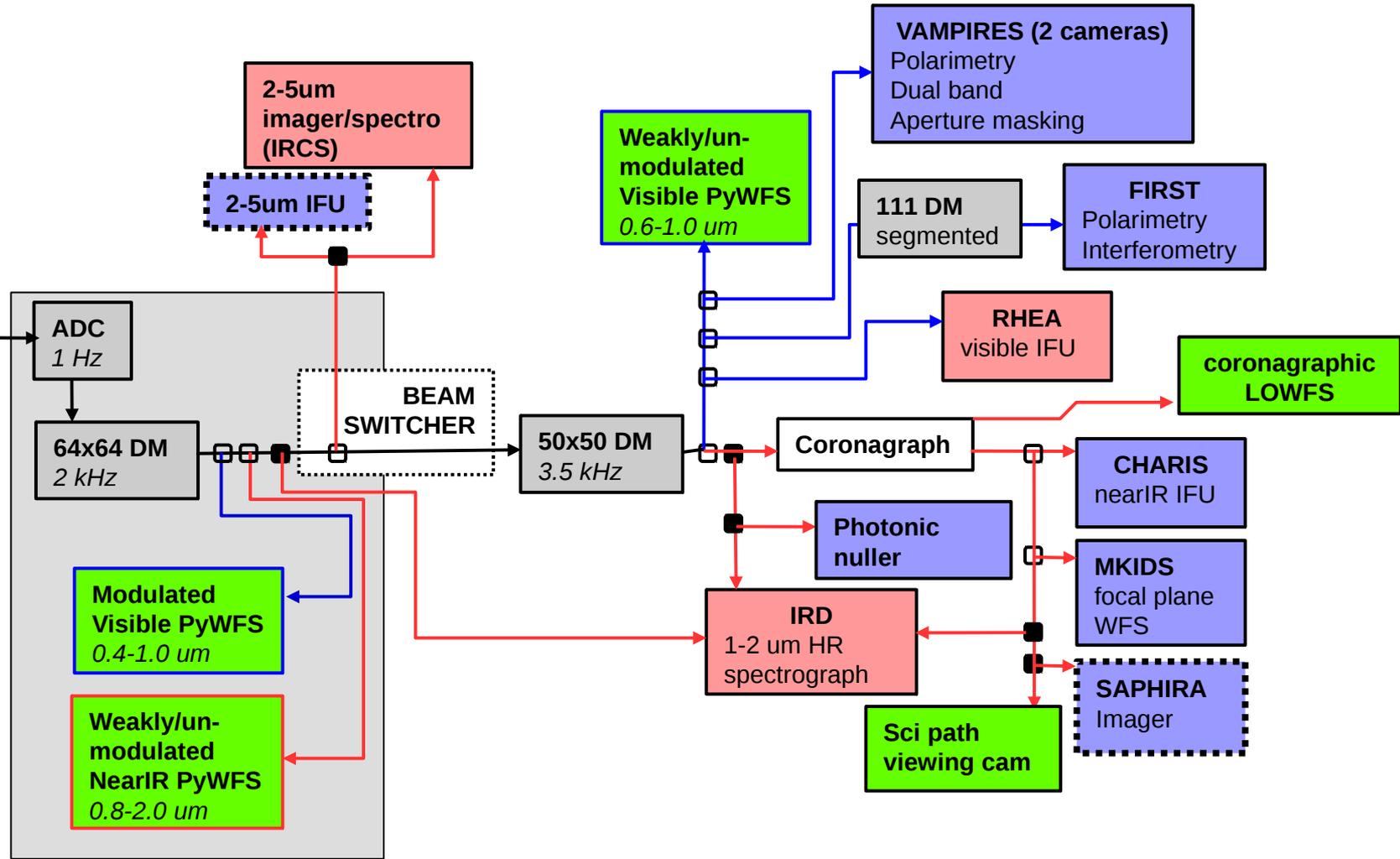
Near-IR nuller

SAPHIRA

# SCEAO Light path



Facility AO

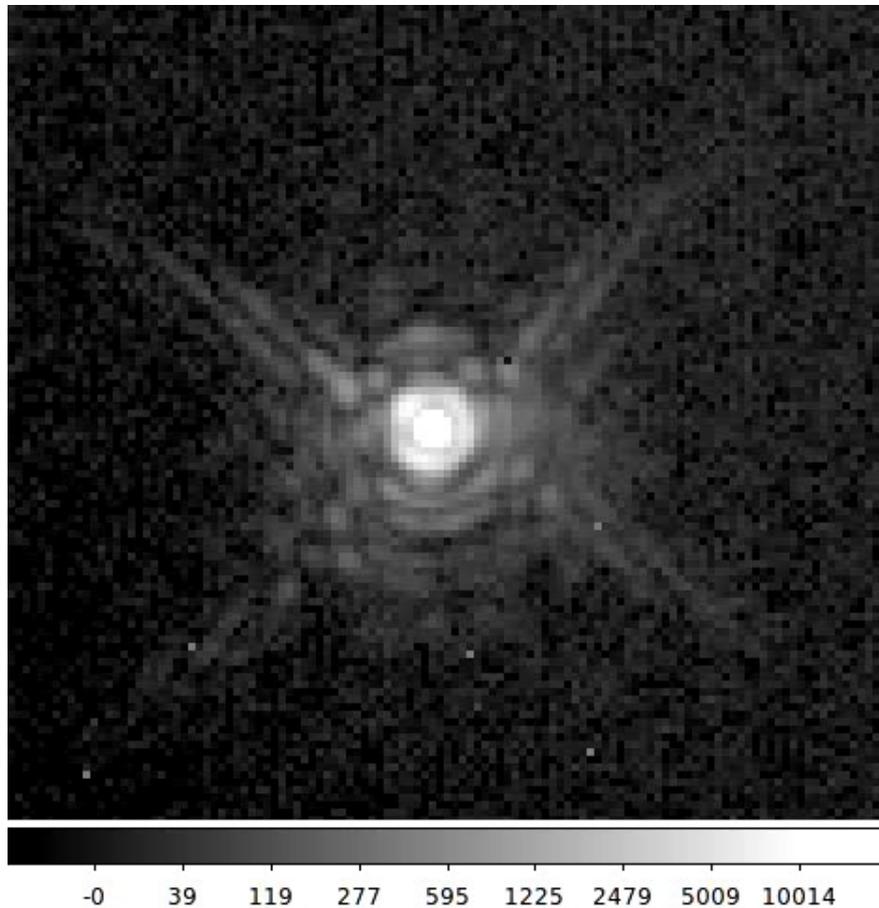


# Current PSF stability @ SCExAO

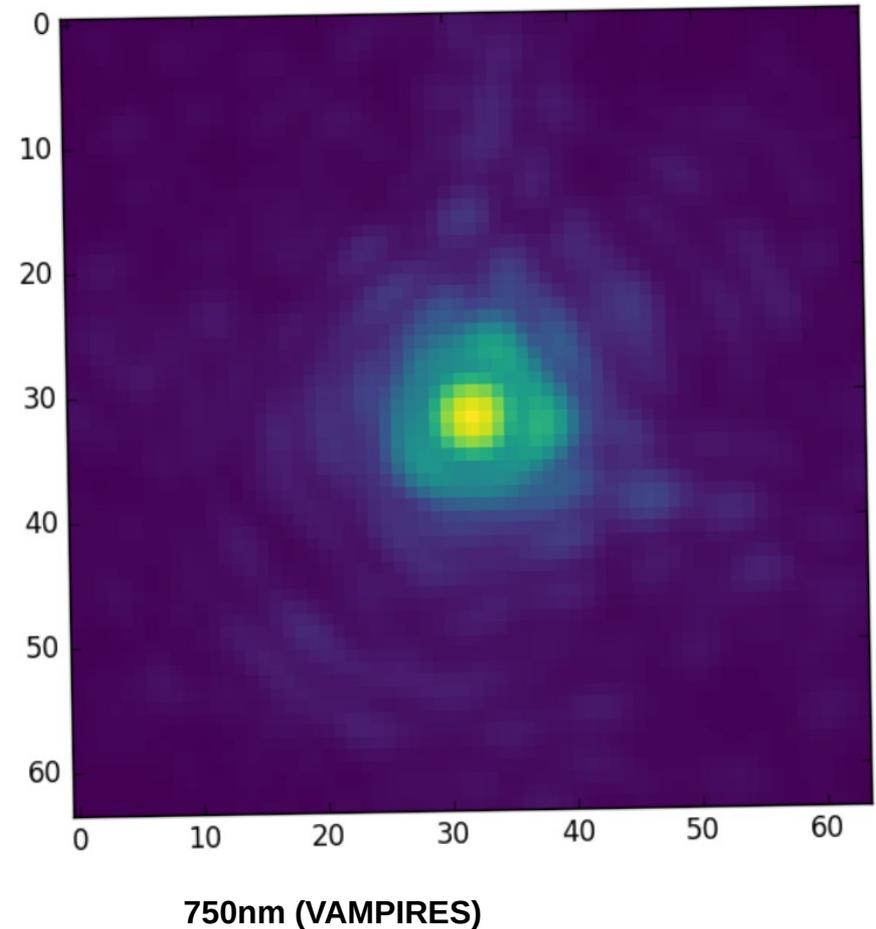
Stable PSF for coronagraphy

SCExAO provides sensing and correction at 500 Hz - 3.5 kHz

14,400 pixel WFS → 2000 actuators



1630nm (SCExAO internal camera)  
3 Hz sampling



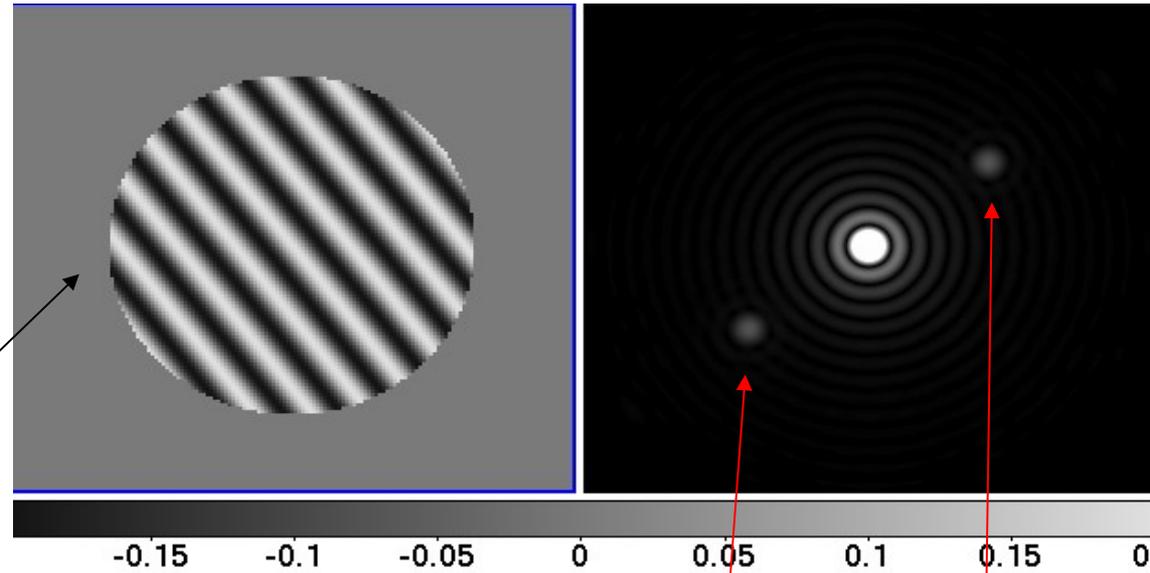
# Relationship between speckle and wavefront errors

pupil plane complex amplitude

$$W(\vec{u}) = \mathcal{A}(\vec{u}) e^{i\phi(\vec{u})}$$

Cosine aberration in pupil phase

$$\phi(\vec{u}) = \frac{2\pi h}{\lambda} \cos(2\pi \vec{f}\vec{u} + \theta)$$



$$I(\vec{\alpha}) = PSF(\vec{\alpha}) + \left(\frac{\pi h}{\lambda}\right)^2 [PSF(\vec{\alpha} + \vec{f}\lambda) + PSF(\vec{\alpha} - \vec{f}\lambda)]$$

## EXAMPLE:

Earth-like planet around Sun-like star is  $\sim 1e-10$  contrast  
 In visible light,  $h=1.6e-12$  m (0.0012 nm) =  $1e-10$  speckle

$1e-10$  speckle (or  $1e-10$  contrast planet) around Sun at 10pc = 0.1 ph/sec/m<sup>2</sup>/um

On a 4-m telescope, with 10% efficiency and a 0.5 um spectral band:

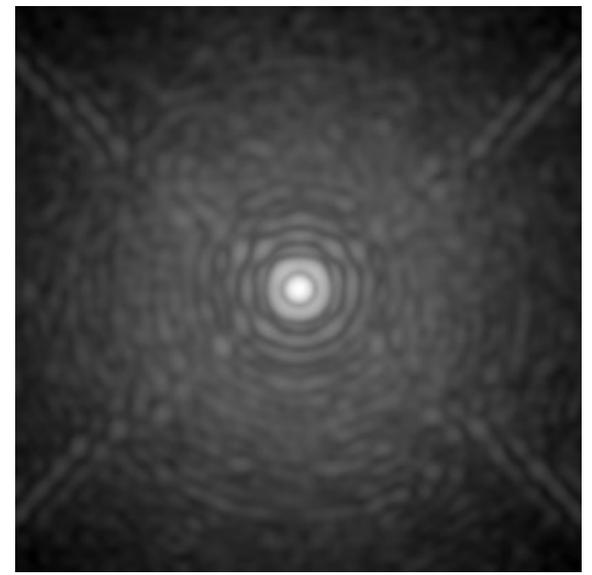
Earth = 0.6 ph/sec

To measure phase and amplitude of speckle requires  $\sim 10$  photon

10 photon = 16 sec

→ This spatial frequency needs to be stable to 1/1000 nm over  $\sim$  minute

# Focal plane AO and speckle calibration



Use Deformable Mirror (DM) to add speckles

**SENSING**: Put “test speckles” to measure speckles in the image, watch how they interfere

**CORRECTION**: Put “anti speckles” on top of “speckles” to have destructive interference between the two (Electric Field Conjugation, Give'on et al 2007)

**CALIBRATION**: If there is a real planet (and not a speckle) it will not interfere with the test speckles

Fundamental advantage:

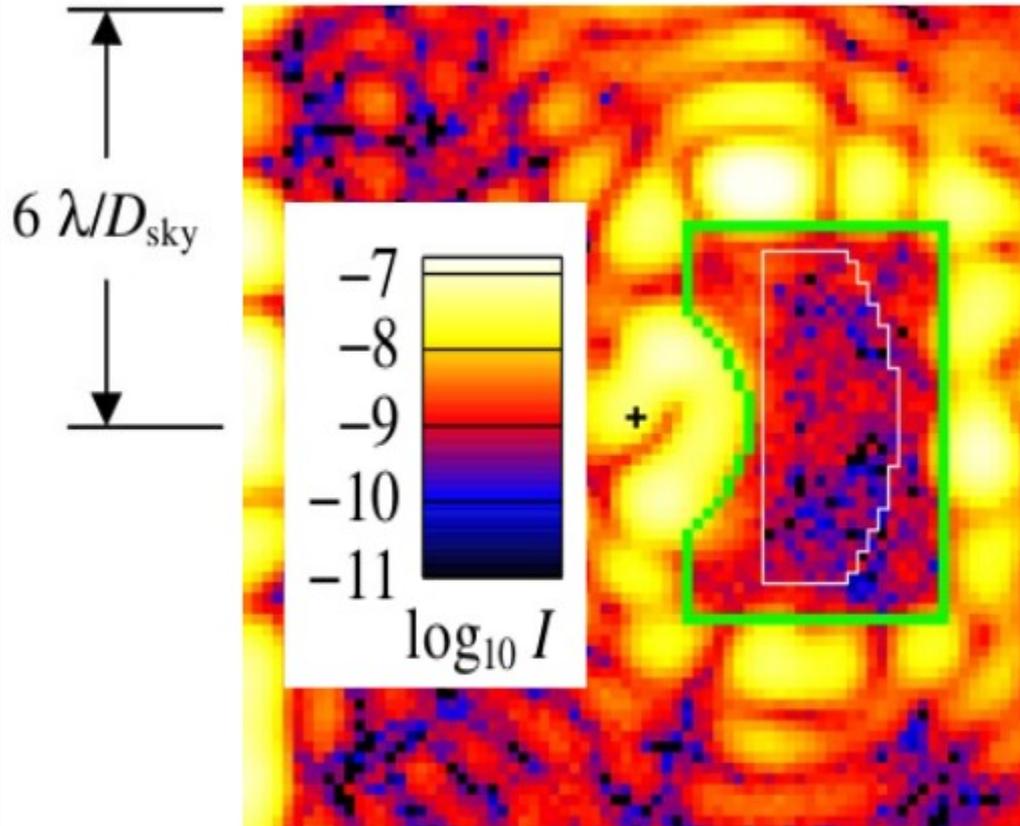
Uses science detector for wavefront sensing:

“What you see is EXACTLY what needs to be removed / calibrated”

# High contrast images obtained in NASA labs

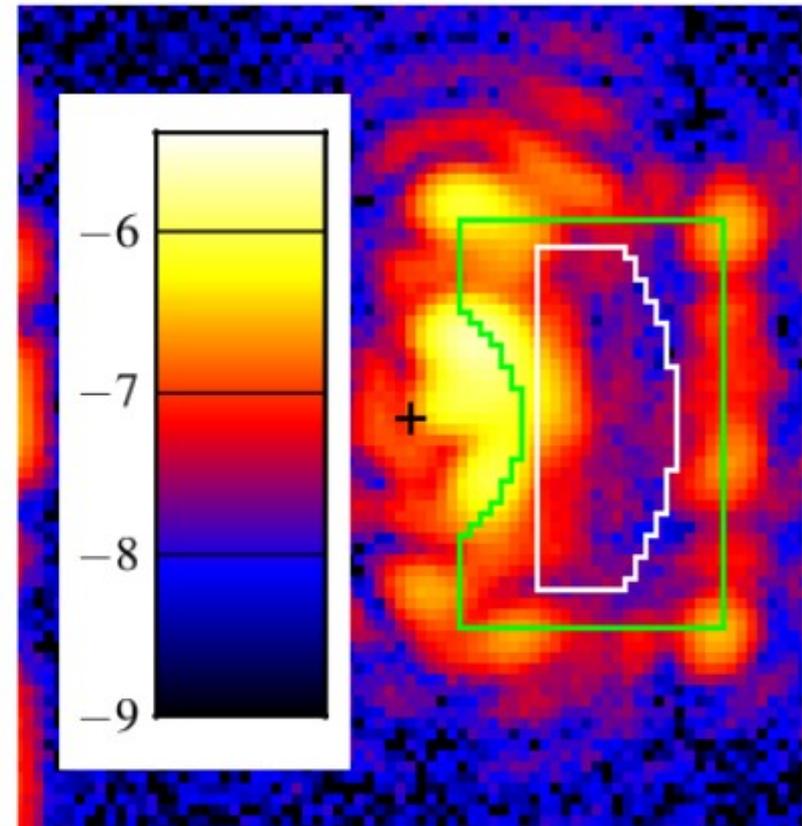
## Example: PIAA coronagraph lab results

Monochromatic light (800nm, vacuum)



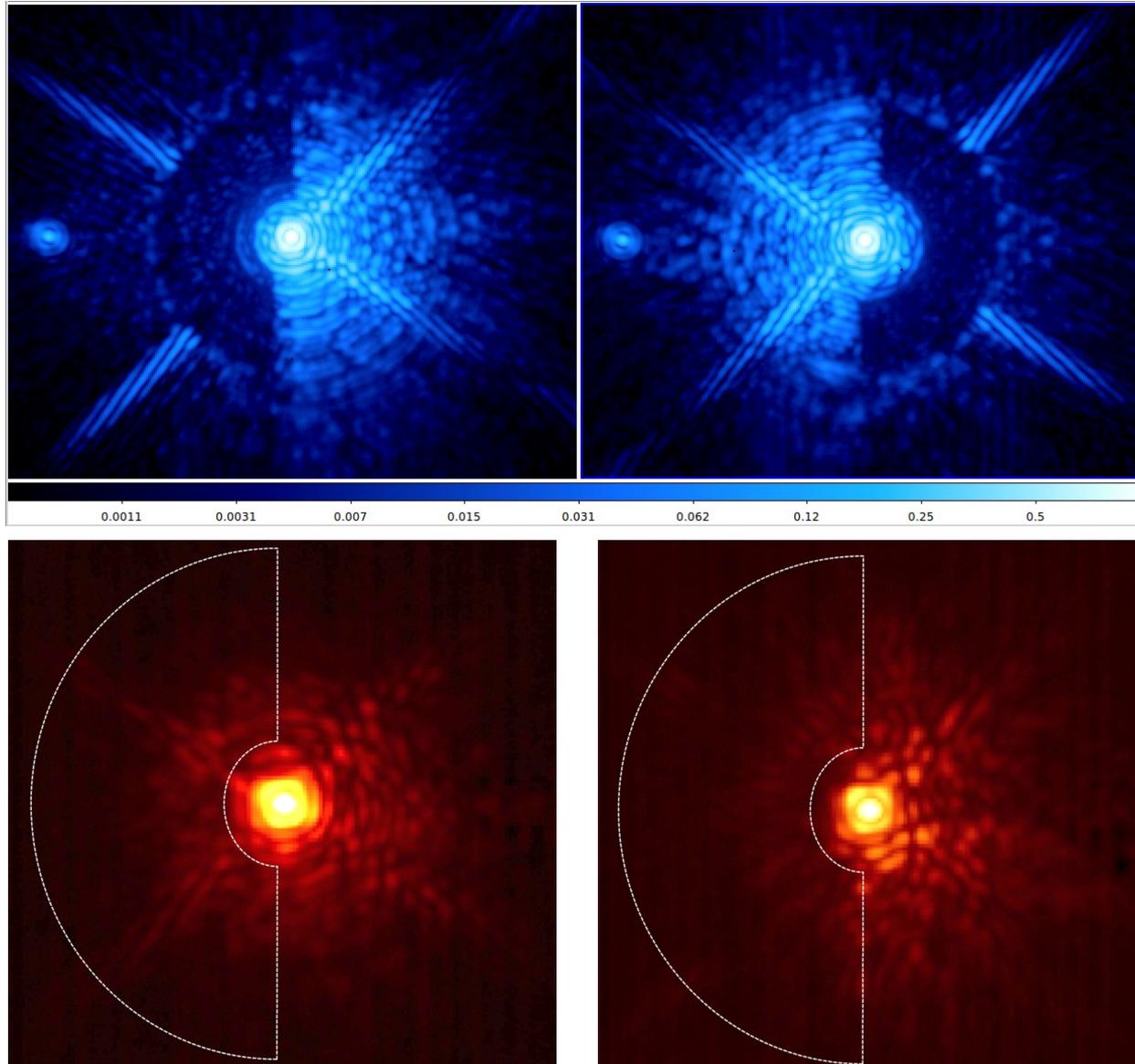
3 runs, contrast values averaged from 2 to 4  $\lambda/D$  between  $5 \cdot 10^{-10}$  to  $9 \cdot 10^{-10}$   
(figure shows  $7.3 \cdot 10^{-10}$  result)

7.5% wide band (770 – 830 nm, in air)



$5 \cdot 10^{-8}$  contrast from 2 to 4  $\lambda/D$ ,  
 $2 \cdot 10^{-8}$  contrast from 3 to 4  $\lambda/D$   
Contrast performance limited by wavefront instability (test in air)

# Speckle Control



Speckle nulling, in the lab and on-sky (no XAO).

Experience limited by detector readout noise and speed.

KERNEL project: C-RED-ONE camera.

From:

- 114 e- RON
- 170 Hz frame rate

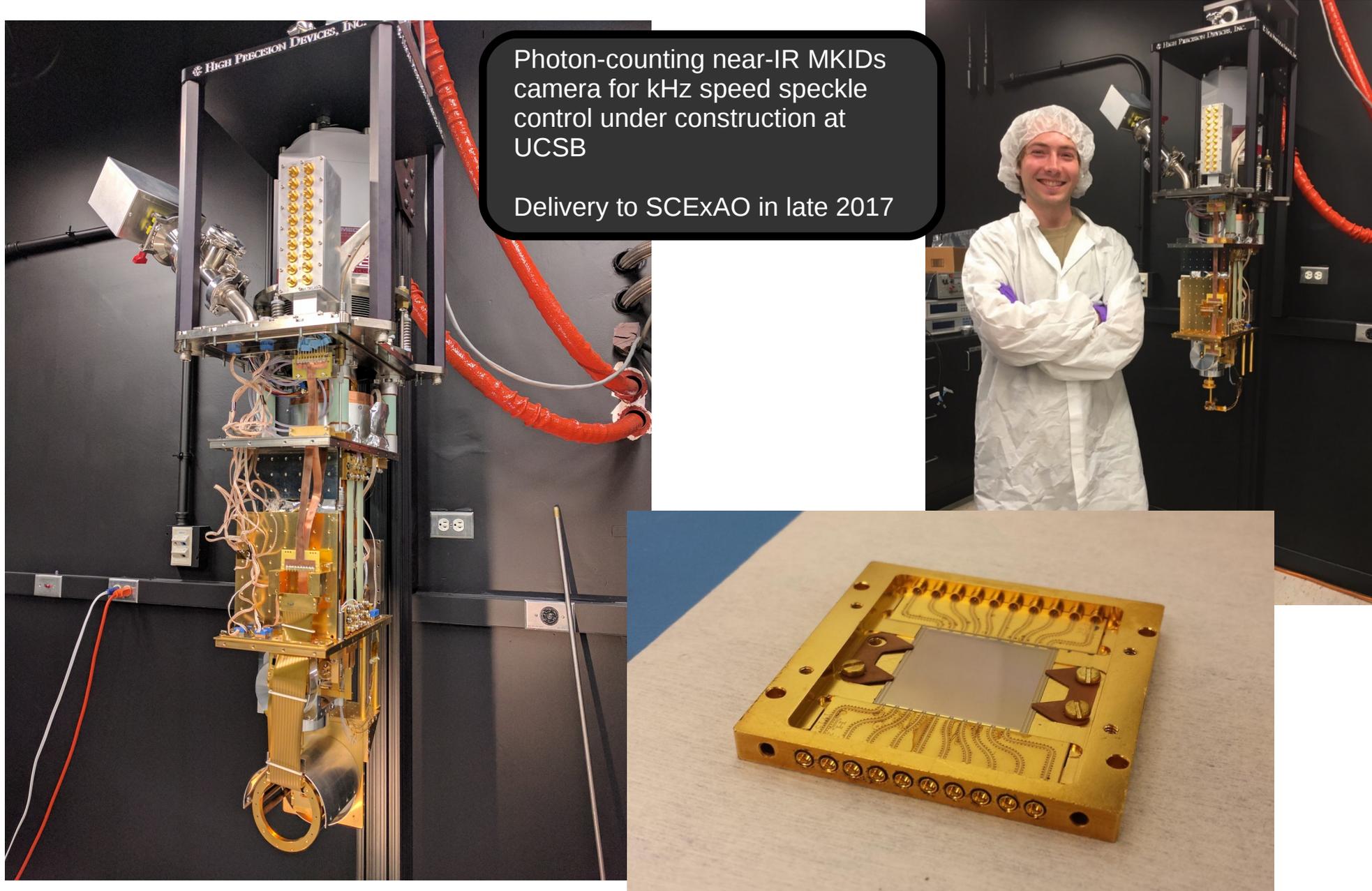
To:

- 0.8 e- RON
- 3500 Hz frame rate

Expect some updates

# MKIDS camera

Photon-counting, wavelength resolving 140x140 pixel camera

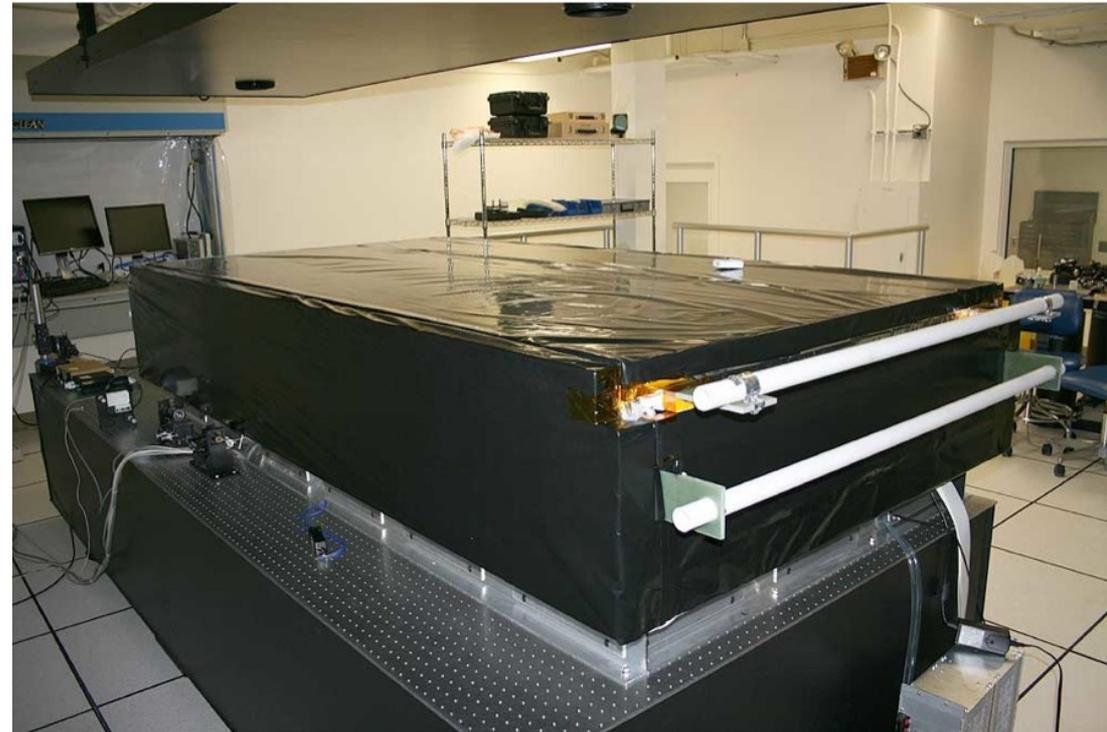


# Coronagraphy testbeds for high contrast ( $< 1e-8$ ) work need to achieve high stability

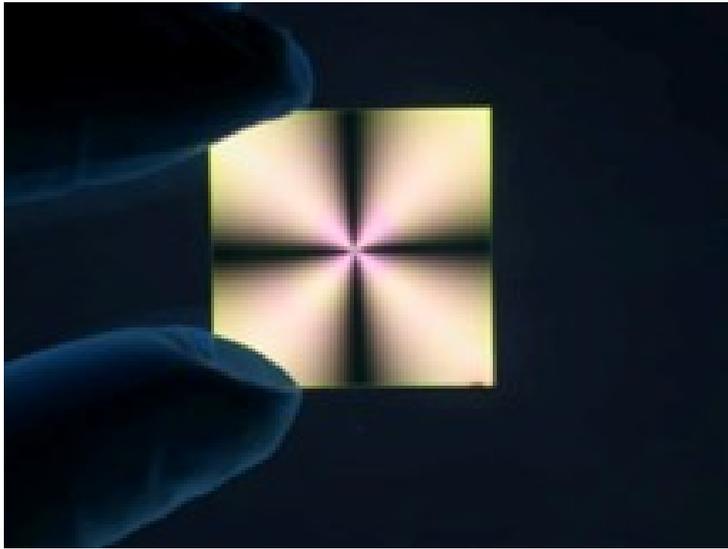
*High Contrast Imaging Testbed (HCIT) is a vacuum facility at NASA JPL*



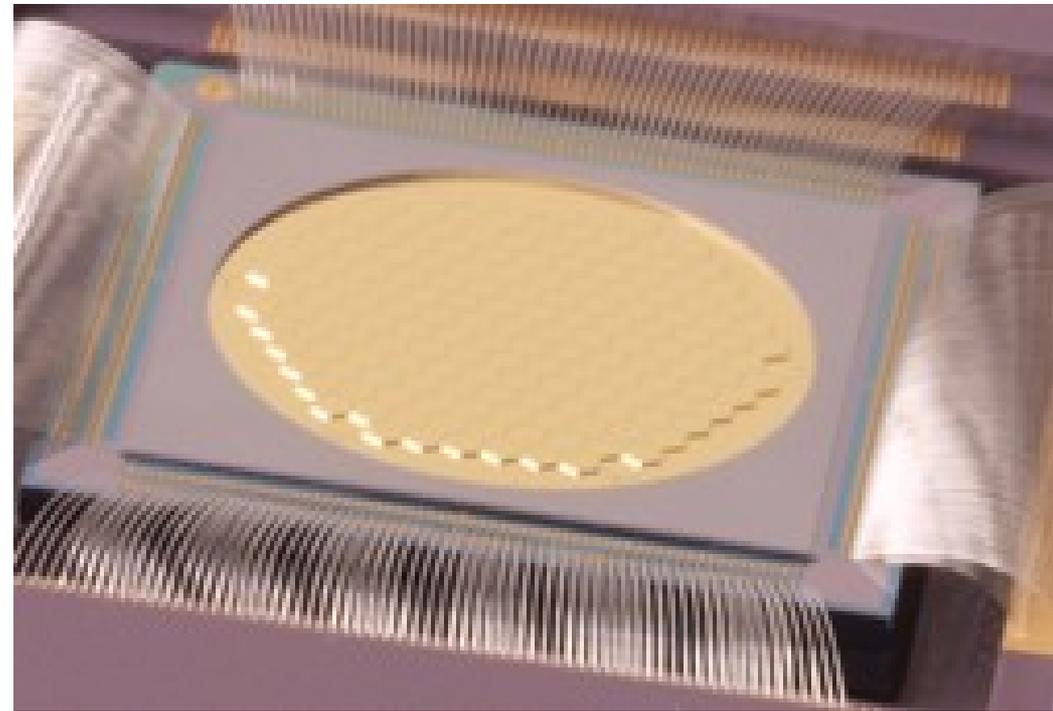
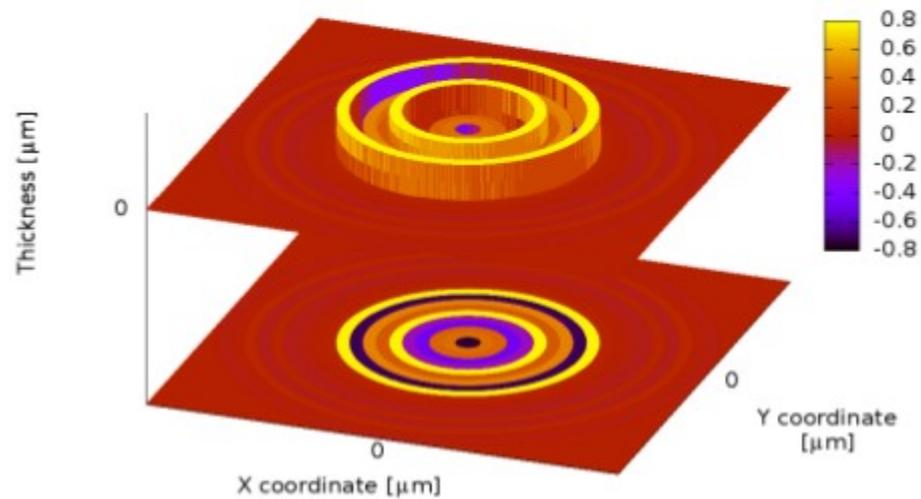
*NASA Ames testing PIAA coronagraph / WFC architectures & MEMs DMs.*



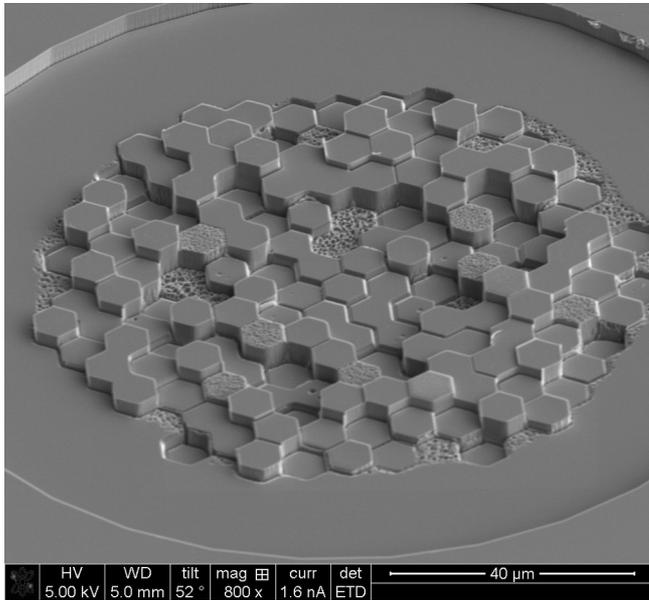
# Technology: components



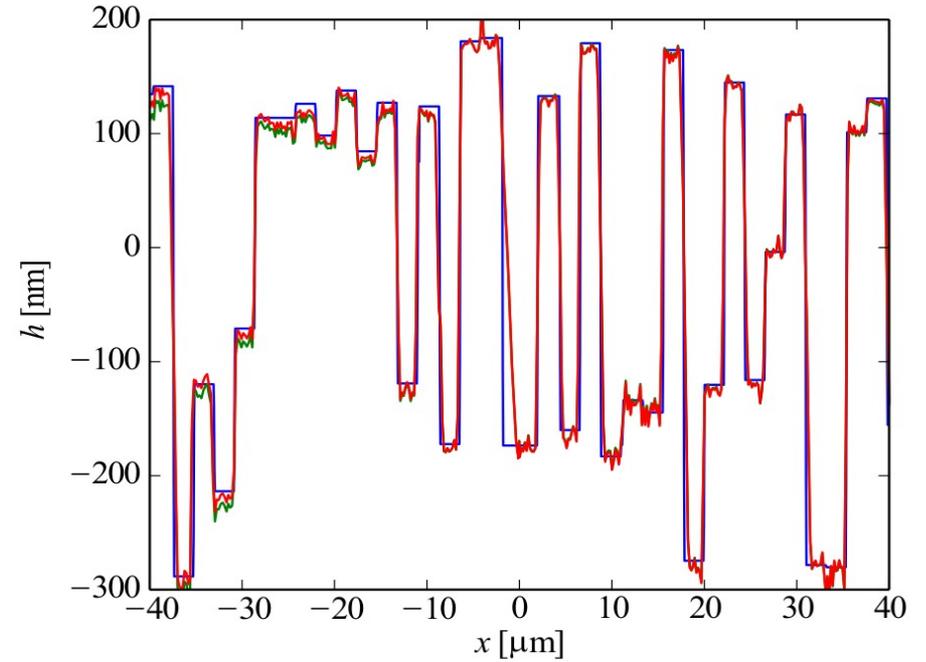
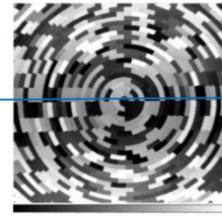
PIAACMC optimized focal plane mask  
F/20 beam, 10% bandwidth around 0.5  $\mu\text{m}$   
SiO<sub>2</sub>, 20 zones, 4  $\mu\text{m}$  max deviation



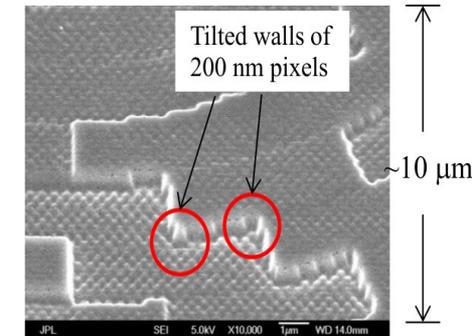
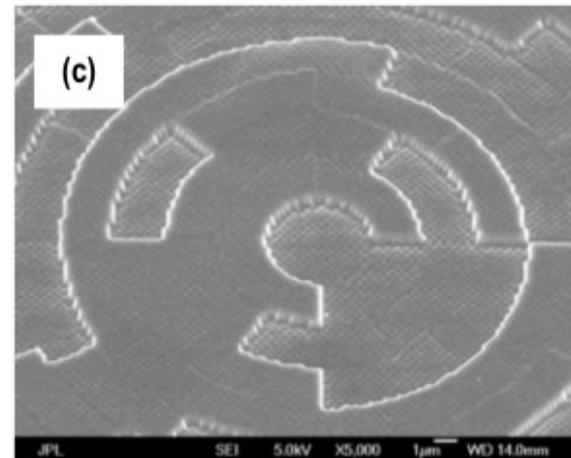
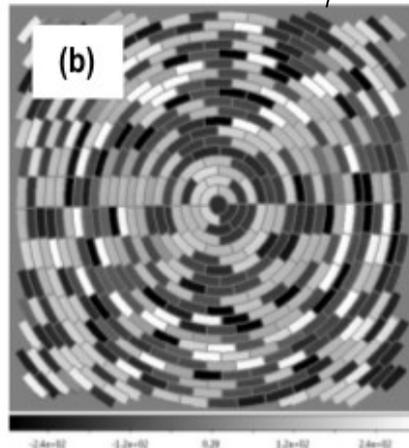
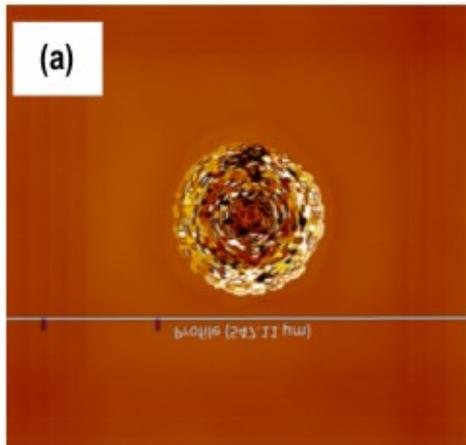
# Multi-zone PIAACMC focal plane mask



← SCEXAO focal plane mask (2017)



Focal plane mask manufactured at JPL's MDL  
Meets performance requirements  
(WFIRST PIAACMC Milestone report)



# Habitable planet imaging: Scientific opportunities

Space allows access to very high contrast (no atmosphere), but aperture size is limited

Ground-based telescopes can be very large ( $\sim 30\text{m}$ ), but the contrast is limited due to atmosphere

# Habitable planets in reflected light: separation, contrast

total stellar luminosity:  $L$  (usually scaled to Sun)

Distance to Sun:  $d$  (in pc)

Physical distance to star scales as  $a=L^{1/2}$

Angular distance (arcsec) =  $L^{1/2}/d$

Example:  $d=10\text{pc}$ ,  $L = 1 \rightarrow 0.1''$

Contrast  $\sim 2e-10$  for Earth at maximum elongation

**Contrast for Earth-like planets in habitable zone =  $2e-10 / L$**

Example:  $L=0.01$  (M type star)  $\rightarrow$  contrast =  $2e-8$

Orbital period  $P = \text{sqrt}(a^3/M)$

Example: Proxima Centauri...

1/600 Sun luminosity, 0.123 Sun Mass,  $d=1.3$  pc

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Example: Proxima Centauri...

1/600 Sun luminosity, 0.123 Sun Mass,  $d=1.3$  pc

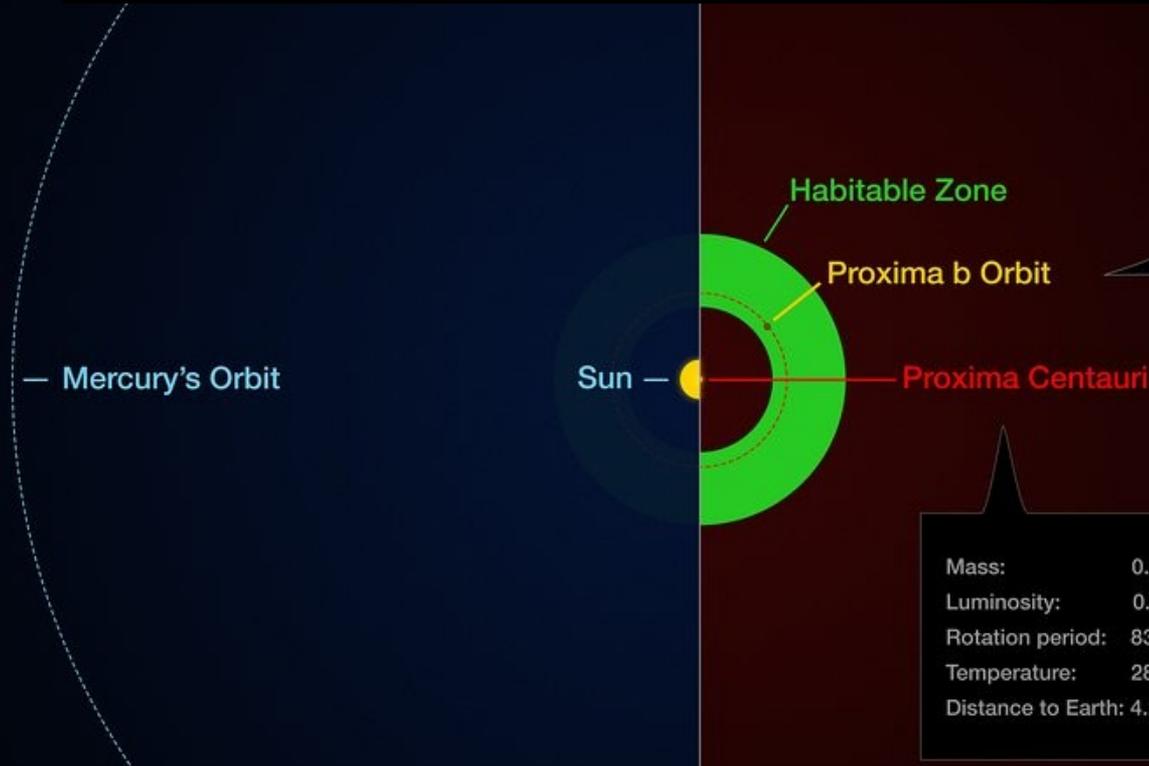
Orbital radius :  $a=0.04$  AU

Angular separation =  $a/d = 0.03$  arcsec

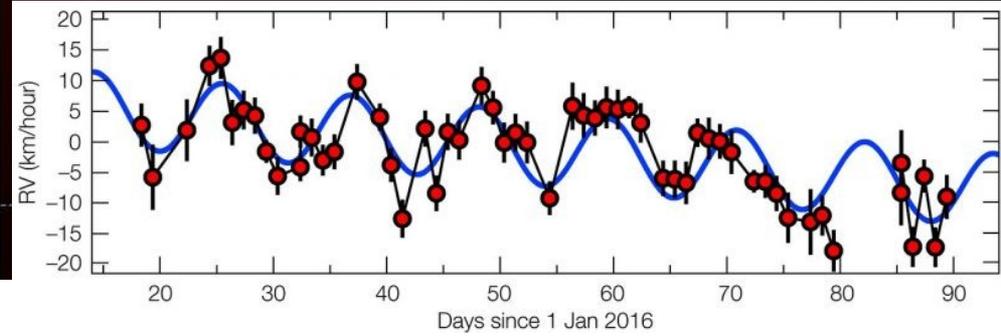
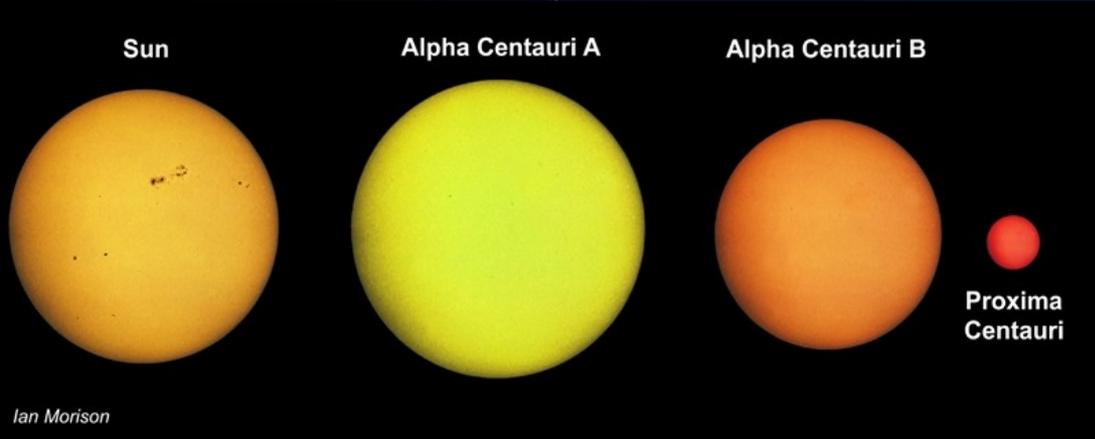
Contrast =  $1.2e-7$

Orbital Period = 8 day

# Proxima Centauri

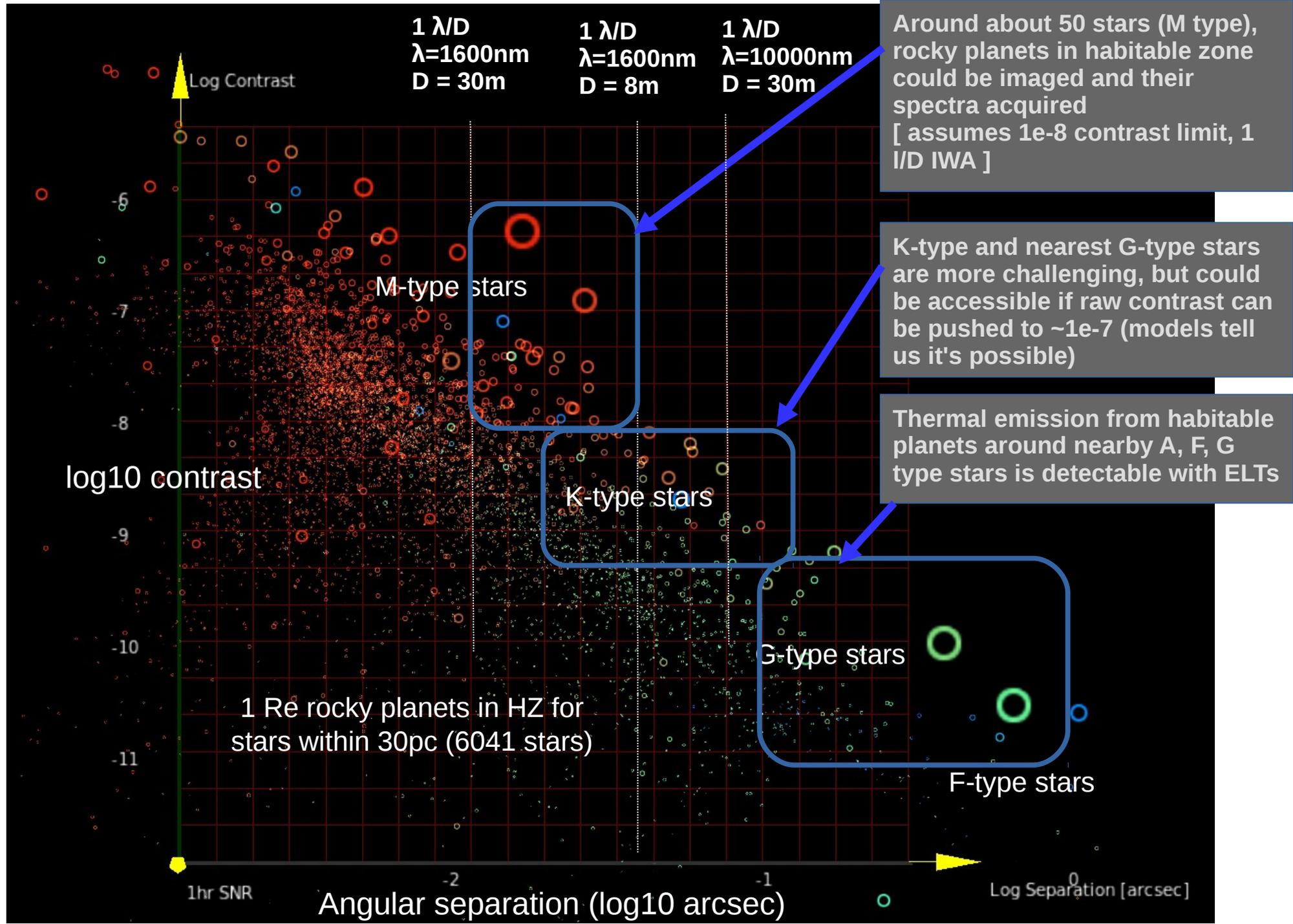


Mass: 0.12 solar masses  
Luminosity: 0.00155 solar luminosities  
Rotation period: 83 days  
Temperature: 2800 Celsius  
Distance to Earth: 4.23 light-years

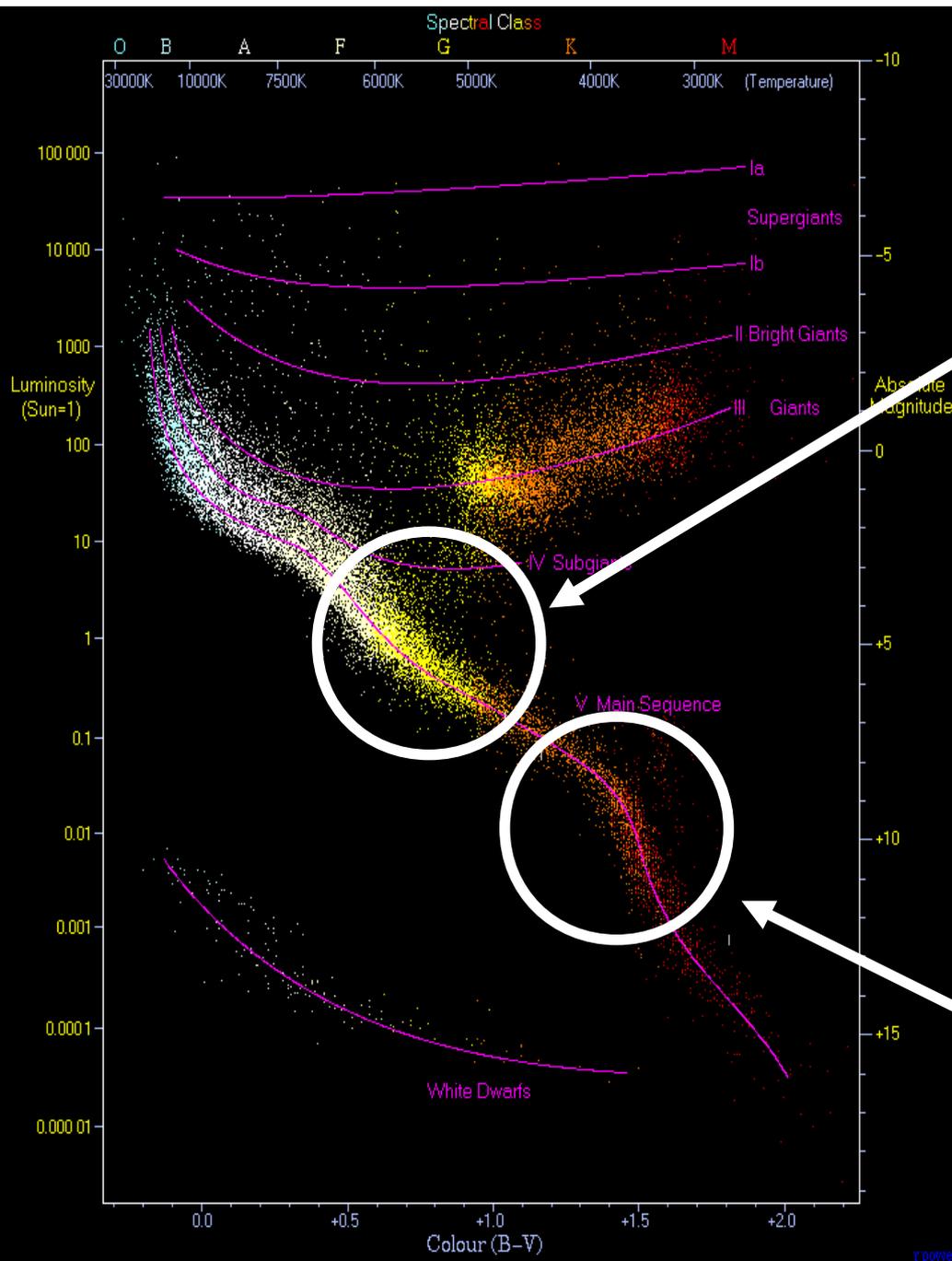


# Habitable Planets: Contrast and Angular separation

## Ground-based observation opportunities



# Imaging habitable planets from space and ground



----- Space -----

Habitable planets can be imaged around nearby Sun-like stars with 2-4+m telescope

----- Ground -----

Next generation of 30-m telescopes will image habitable planets around nearby low-mass stars

**Backup slides : Coronagraph design**

# Types of Coronagraphs

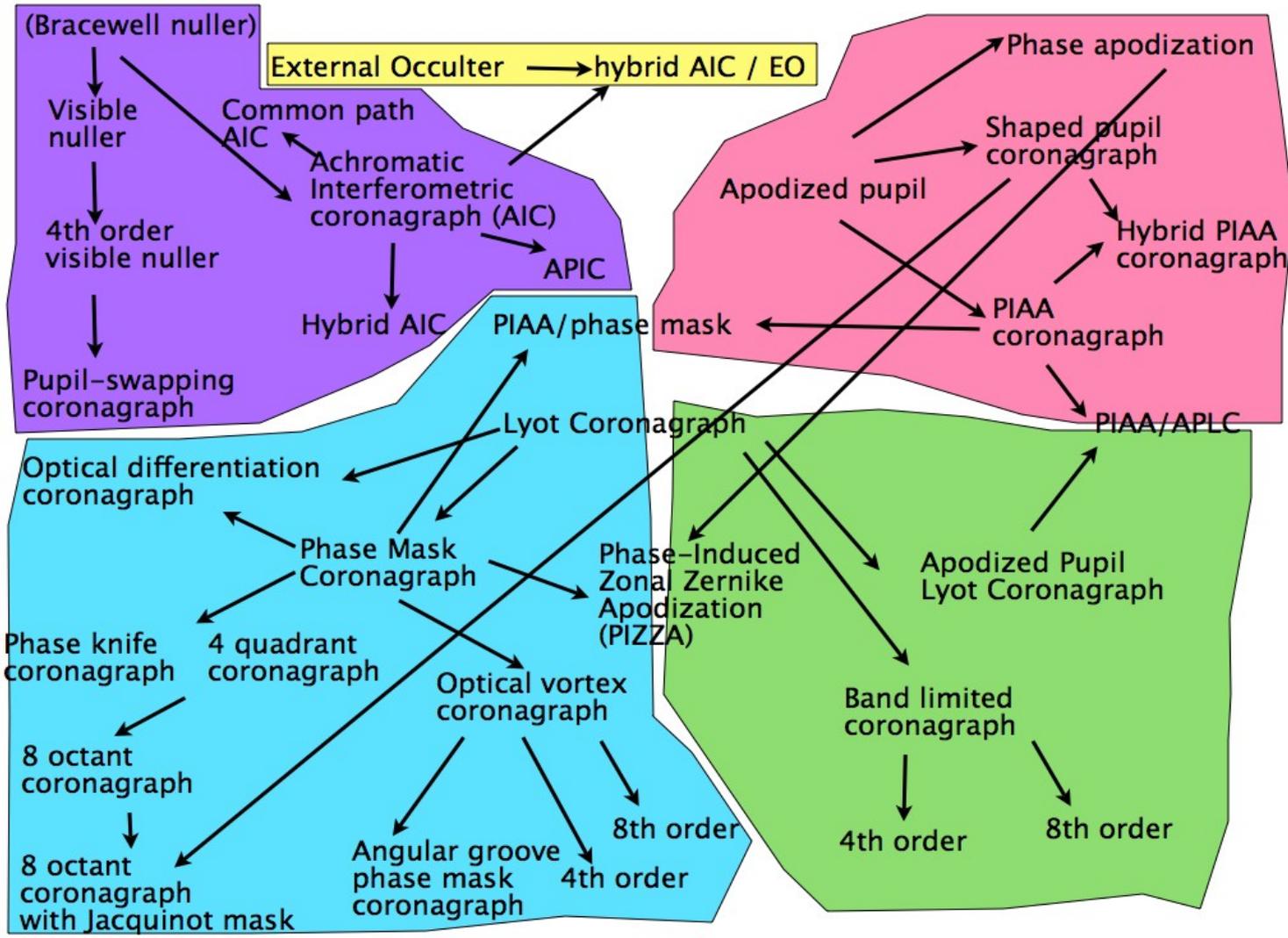
3 main approaches to remove starlight :

- Block starlight BEFORE it enters the telescope using a large **external occulter** ~50000 km in front of the telescope
- Design masks and optical components inside the telescope to induce starlight destructive interference at the expected location of a planet in the image: **internal coronagraph (this lecture)**
- Induce destructive interference between beams of multiple telescopes: **nulling interferometer**

# Internal Coronagraphs: main approaches

*Apodization*

*Beam splitting and destructive interference*



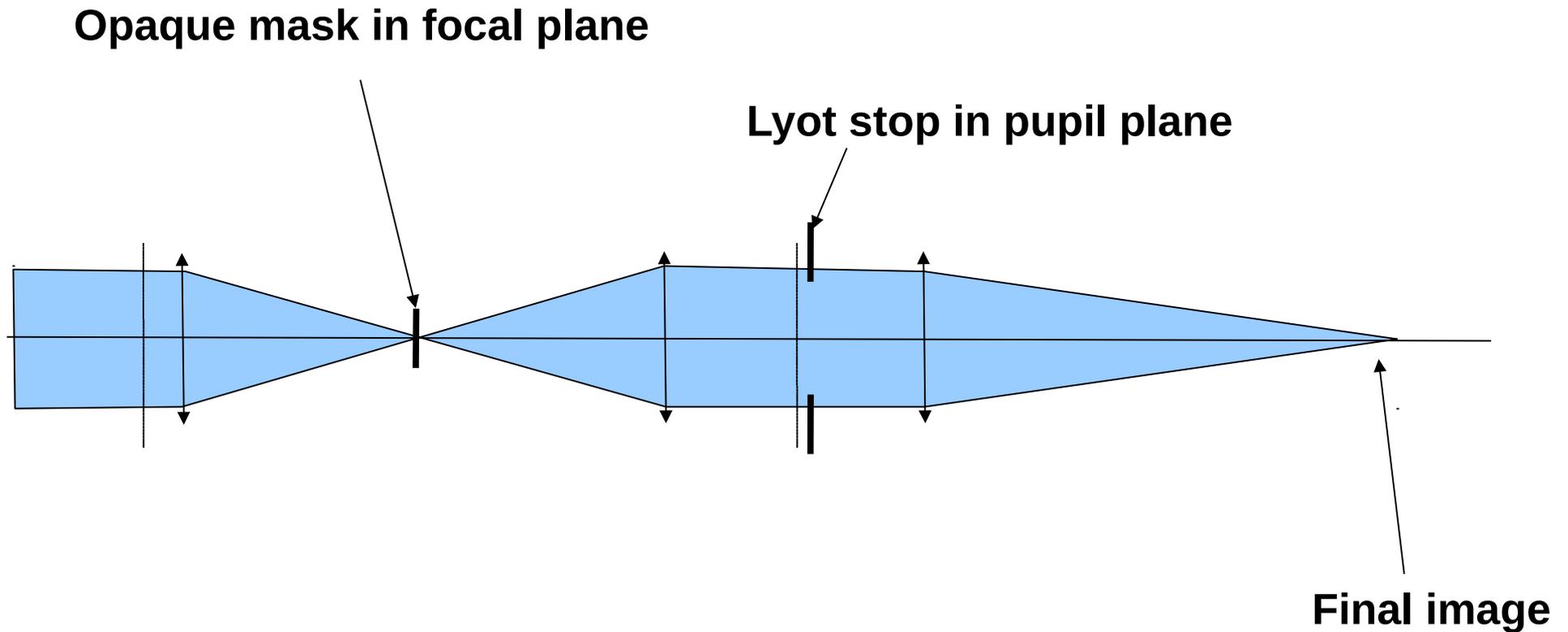
*Phase masks in focal plane*

*Amplitude masks in focal plane*

# Lyot Coronagraph

Developped by Bernard Lyot in 1930 to observe the solar corona

It is the origin of many current high performance coronagraph designs



# Lyot Coronagraph explained by Fourier transforms

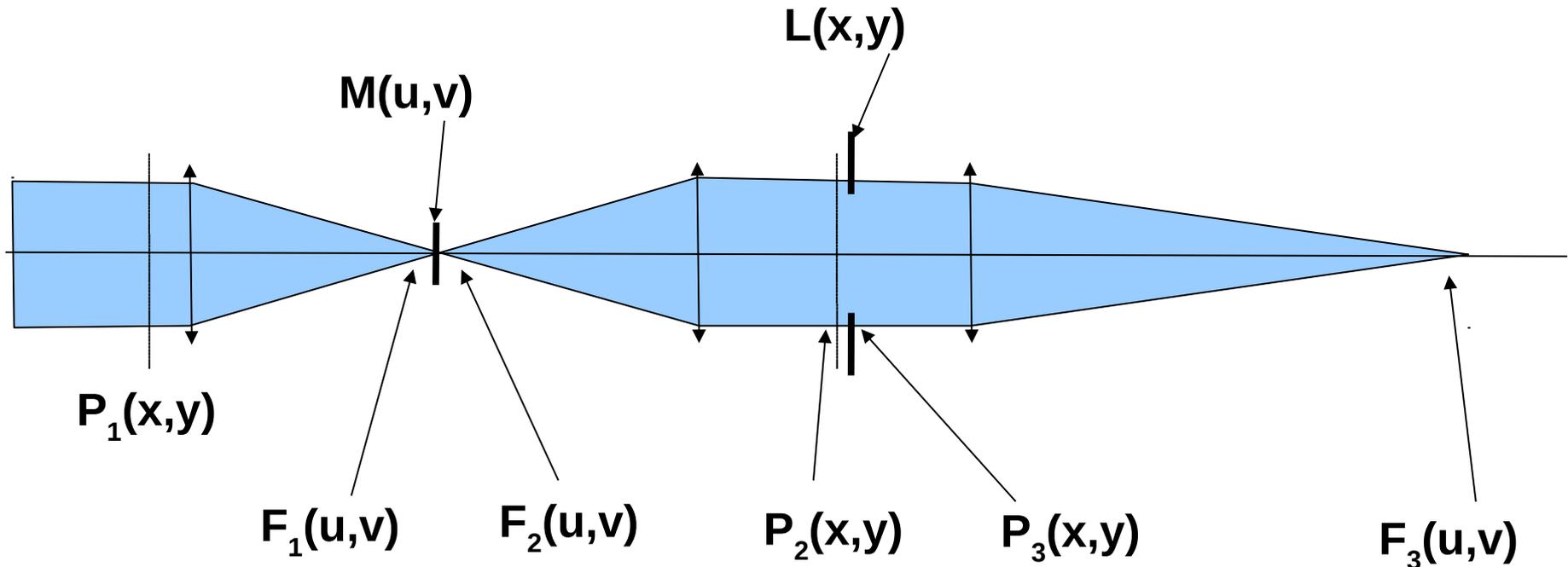
Pupil plane complex amplitude  $\leftrightarrow$  focal plane complex amplitude

$\rightarrow$  Fourier transform  
 $\leftarrow$  Inverse Fourier transform

Coordinates in pupil plane:  $x,y$

Coordinates in focal plane :  $u,v$

\* denoting convolution (product = convolution in Fourier transform)



# Lyot Coronagraph explained by Fourier transforms

Full set of equations (explained in next slides):

Entrance pupil of telescope:  $P_1(x,y)$

Focal plane complex amplitude (before focal plane mask):  $F_1(u,v)$

$$F_1(u,v) = \text{FT} ( P_1(x,y) )$$

Focal plane mask complex amplitude transmission:  $M(u,v)$

Focal plane complex amplitude (after focal plane mask):  $F_2(u,v)$

$$F_2(u,v) = F_1(u,v) \times M(u,v) = \text{FT}(P_1(x,y)) \times M(u,v)$$

Exit pupil plane:

$$P_2(x,y) = \text{FT}^{-1}( F_2(u,v) ) = \text{FT}^{-1} ( \text{FT}(P_1(x,y)) \times M(u,v) ) = P_1(x,y) * \text{FT}^{-1}(M(u,v))$$

With \* denoting convolution

$$P_3(x,y) = L(x,y) \times P_2(x,y)$$

$$\mathbf{P_3(x,y) = L(x,y) \times (P_1(x,y) * \text{FT}^{-1}(M(u,v)))}$$

$$F_3(u,v) = \text{FT}(L(x,y)) * (F_1(u,v) \times M(u,v))$$

Coronagraphy problem: minimize  $P_3(x,y)$  for on-axis point source

# Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude  $\leftrightarrow$  focal plane complex amplitude

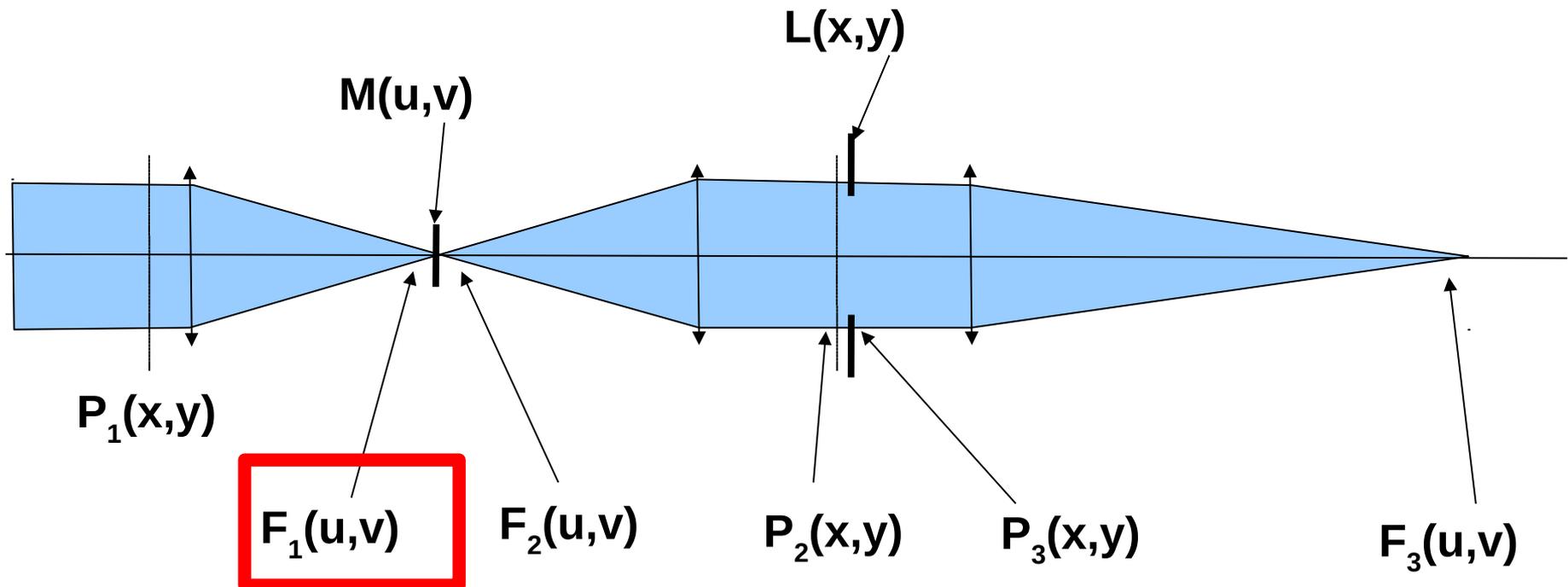
$\rightarrow$  Fourier transform

$\leftarrow$  Inverse Fourier transform

Coordinates in pupil plane:  $x, y$

Coordinates in focal plane :  $u, v$

\* denoting convolution (product = convolution in Fourier transform)

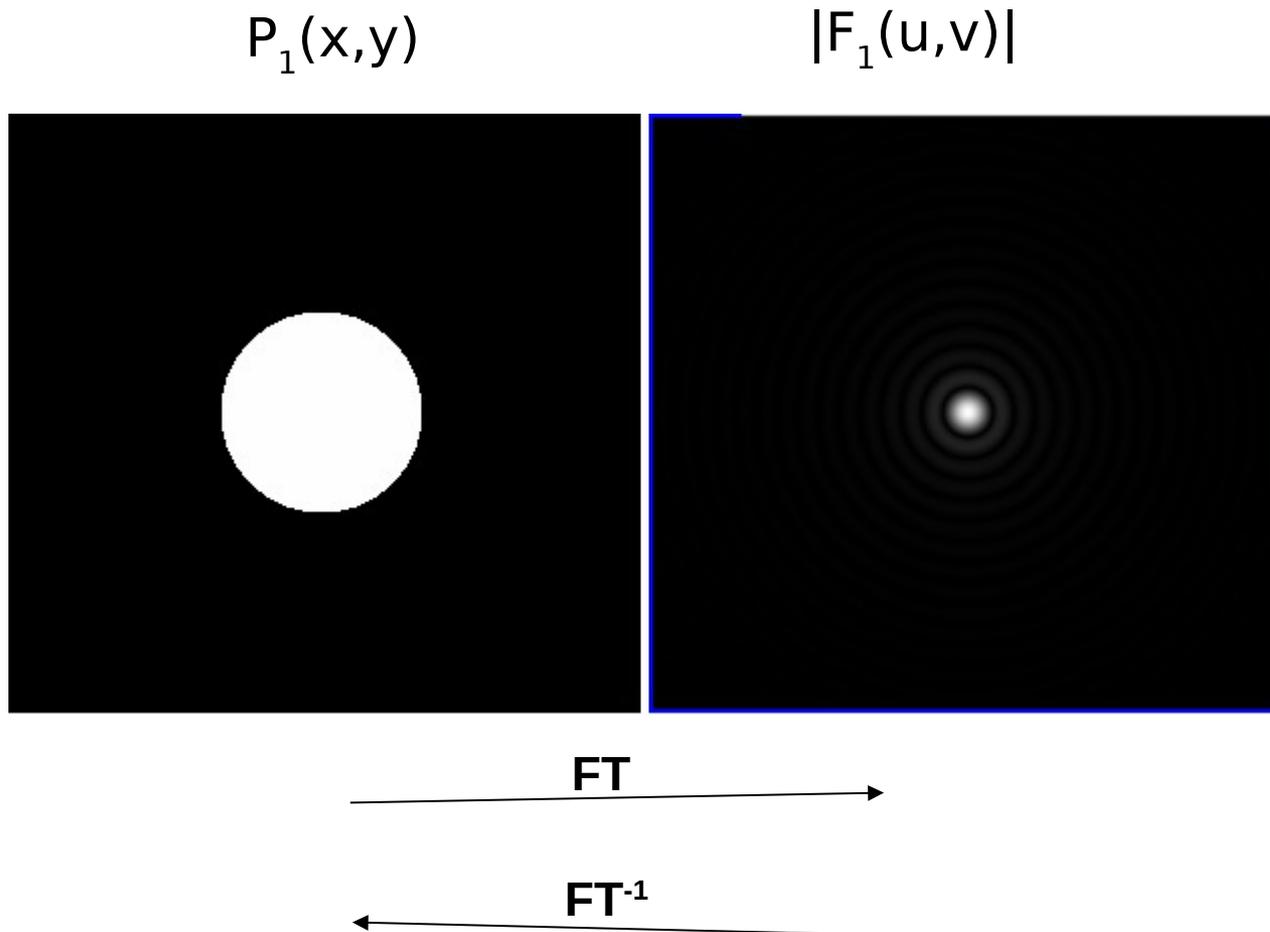


# Focal plane image = FT of pupil complex amplitude

Entrance pupil of telescope:  $P_1(x,y)$

Focal plane complex amplitude (before focal plane mask):  $F_1(u,v)$

$$F_1(u,v) = \text{FT} ( P_1(x,y) )$$



# Lyot Coronagraph explained by Fourier transforms

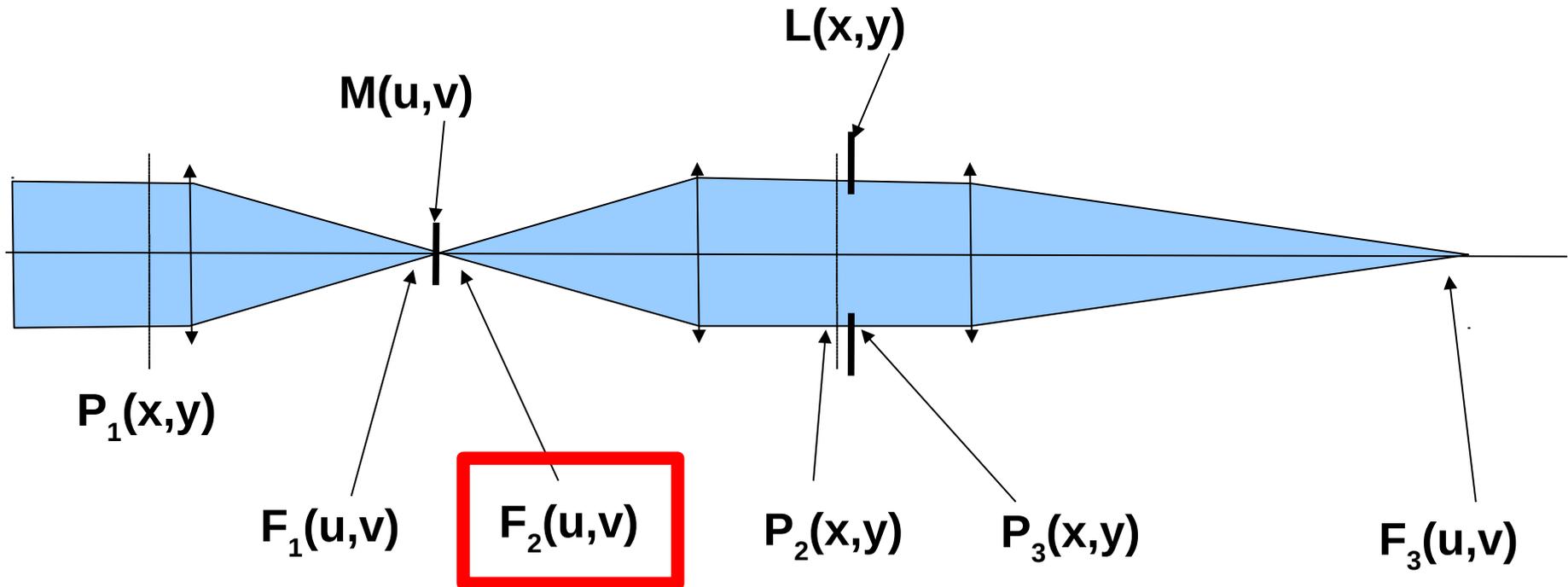
Pupil plane complex amplitude  $\leftrightarrow$  focal plane complex amplitude

$\rightarrow$  Fourier transform  
 $\leftarrow$  Inverse Fourier transform

Coordinates in pupil plane:  $x,y$

Coordinates in focal plane :  $u,v$

\* denoting convolution (product = convolution in Fourier transform)



# Inserting an opaque mask in the focal plane

Focal plane mask complex amplitude transmission:  $M(u,v)$

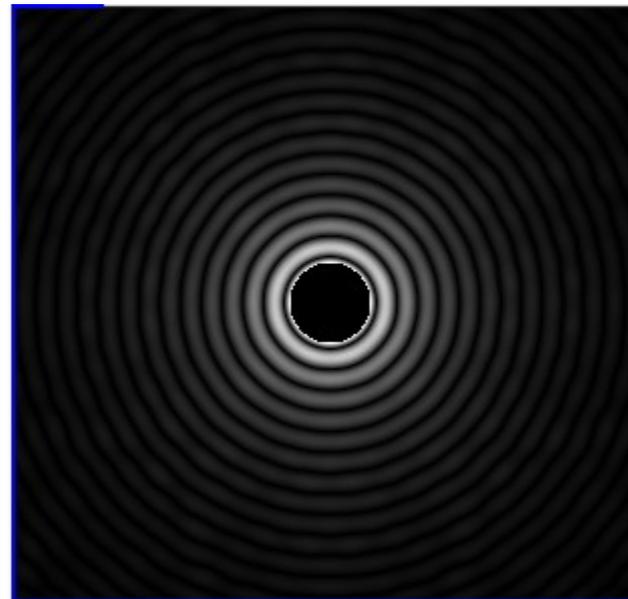
Focal plane complex amplitude (after focal plane mask):  $F_2(u,v)$

$$F_2(u,v) = F_1(u,v) \times M(u,v) = \text{FT}(P_1(x,y)) \times M(u,v)$$

$M(u,v)$



$|F_2(u,v)|$



# Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude  $\leftrightarrow$  focal plane complex amplitude

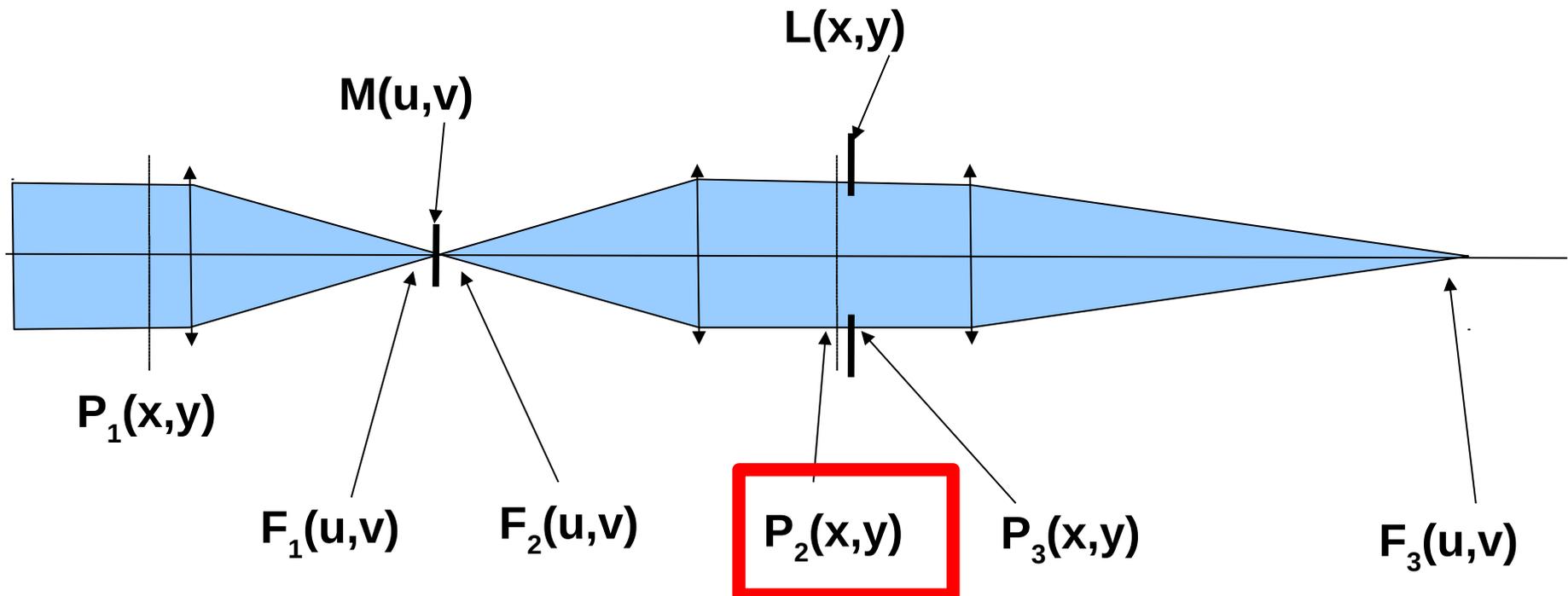
$\rightarrow$  Fourier transform

$\leftarrow$  Inverse Fourier transform

Coordinates in pupil plane:  $x,y$

Coordinates in focal plane :  $u,v$

\* denoting convolution (product = convolution in Fourier transform)



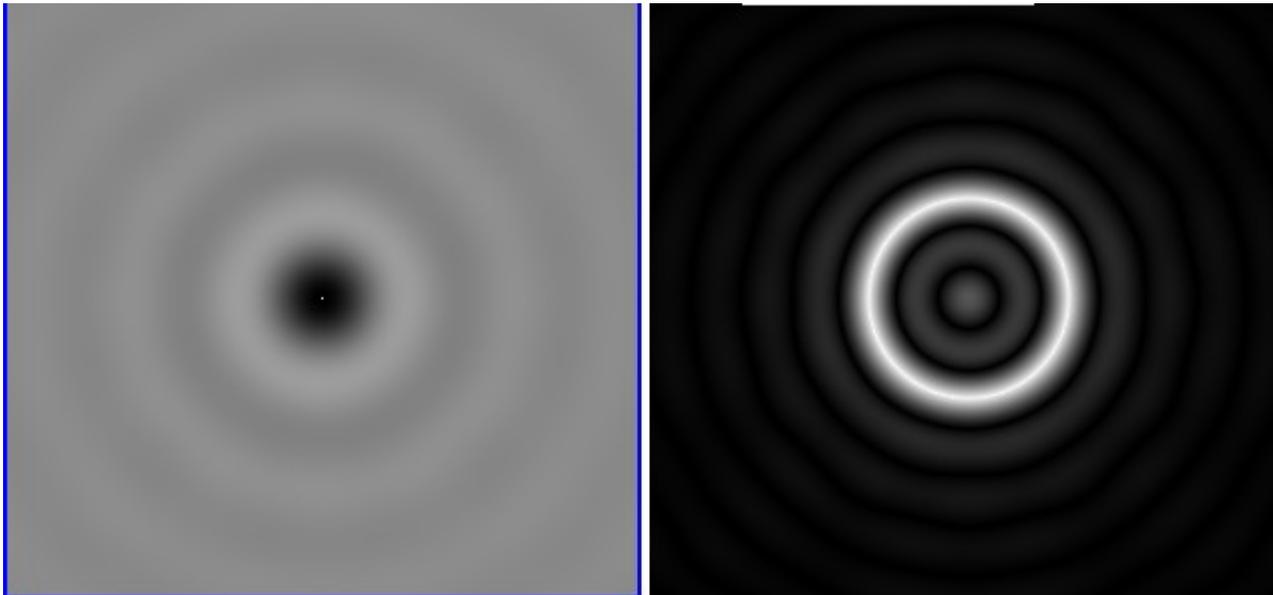
# Lyot Coronagraph : light distribution in output pupil plane

Exit pupil plane:

$$\begin{aligned} P_2(x,y) &= \text{FT}^{-1}( F_2(u,v) ) \\ &= \text{FT}^{-1} ( \text{FT}(P_1(x,y) \times M(u,v)) ) = P_1(x,y) * \text{FT}^{-1}(M(u,v)) \end{aligned}$$

$\text{FT}^{-1}(M(u,v))$

$|P_2(x,y)|$



# Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude  $\leftrightarrow$  focal plane complex amplitude

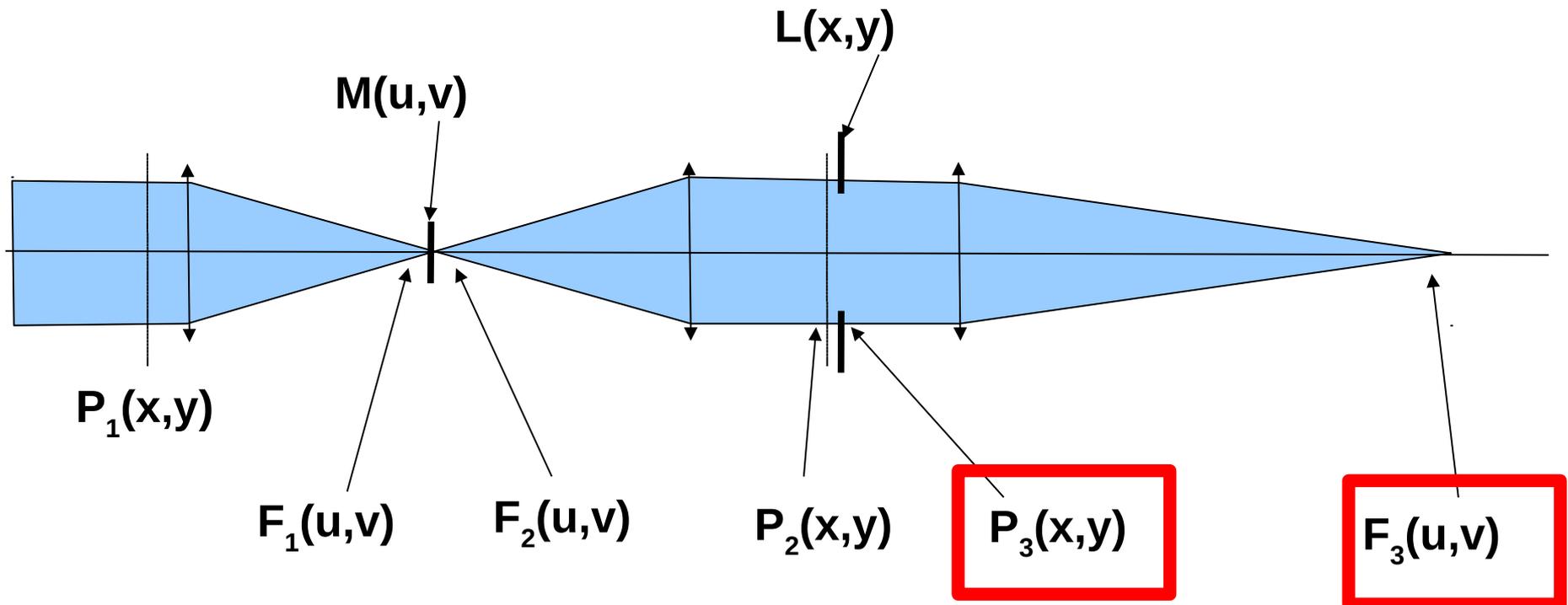
$\rightarrow$  Fourier transform

$\leftarrow$  Inverse Fourier transform

Coordinates in pupil plane:  $x, y$

Coordinates in focal plane:  $u, v$

\* denoting convolution (product = convolution in Fourier transform)



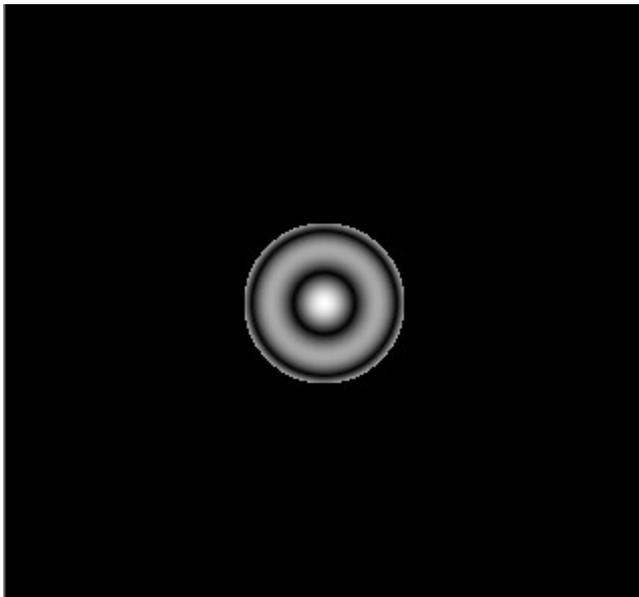
# Lyot Coronagraph : Lyot stop (L)

$$P_3(x,y) = L(x,y) \times P_2(x,y)$$

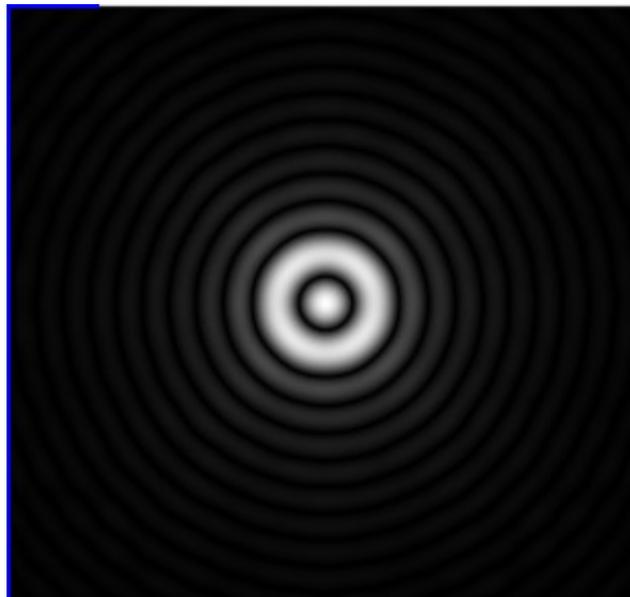
$$\mathbf{P}_3(\mathbf{x},\mathbf{y}) = \mathbf{L}(\mathbf{x},\mathbf{y}) \times (\mathbf{P}_1(\mathbf{x},\mathbf{y}) * \mathbf{FT}^{-1}(\mathbf{M}(\mathbf{u},\mathbf{v})))$$

$$F_3(u,v) = \mathbf{FT}(L(x,y)) * (F_1(u,v) \times M(u,v))$$

$|P_3(x,y)|$

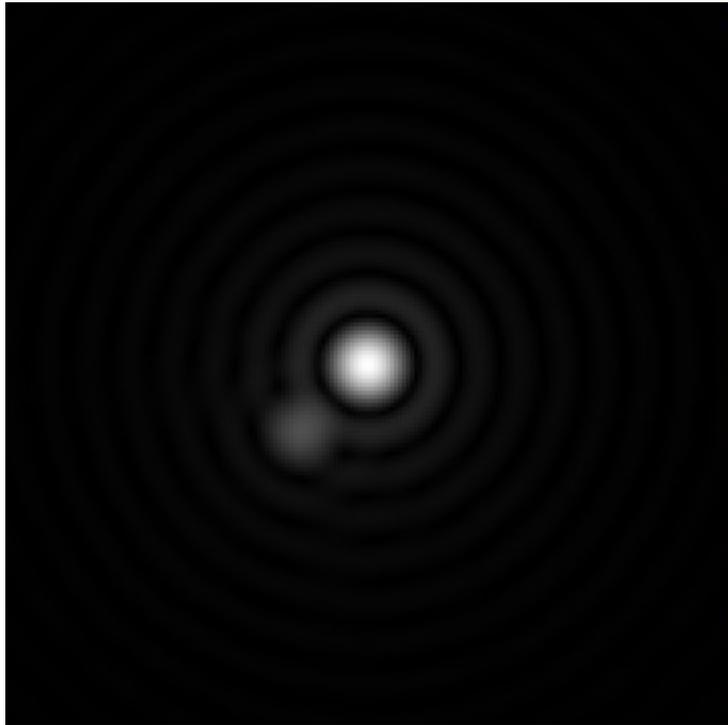


$|F_3(u,v)|$

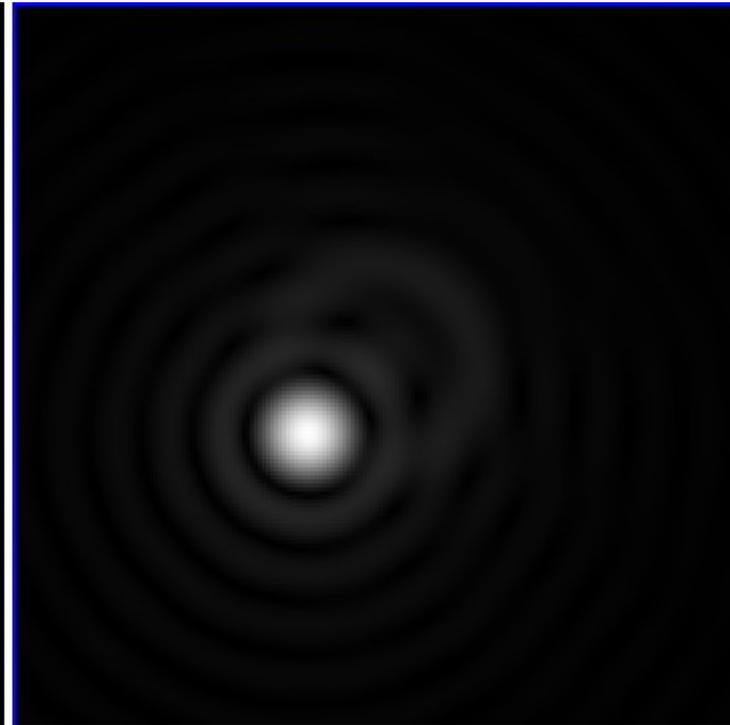


# Numerical simulation of final image for 10:1 contrast

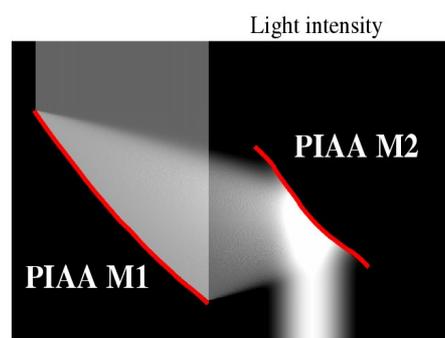
No coronagraph



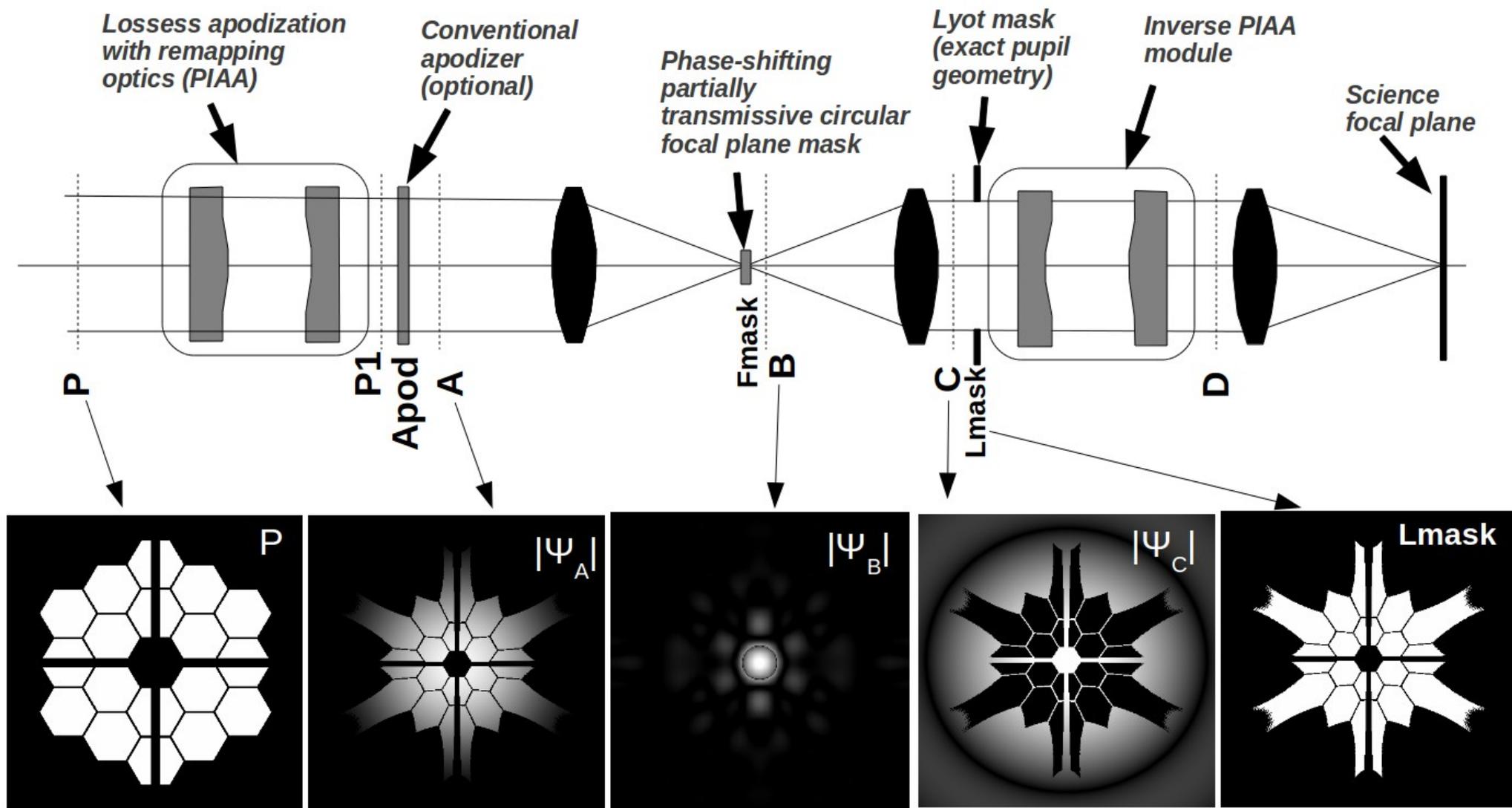
With Lyot  
Coronagraph



# A more fancy coronagraph design



## Phase Induced Amplitude Apodized Complex Mask Coronagraph (PIAACMC)



# Lyot Coronagraph : optimizations

Conventional Lyot coronagraph is limited in performance:

- cannot reach extremely high contrast (some light in pupil)
- tradeoff between throughput and contrast
- not able to get high contrast close to the optical axis

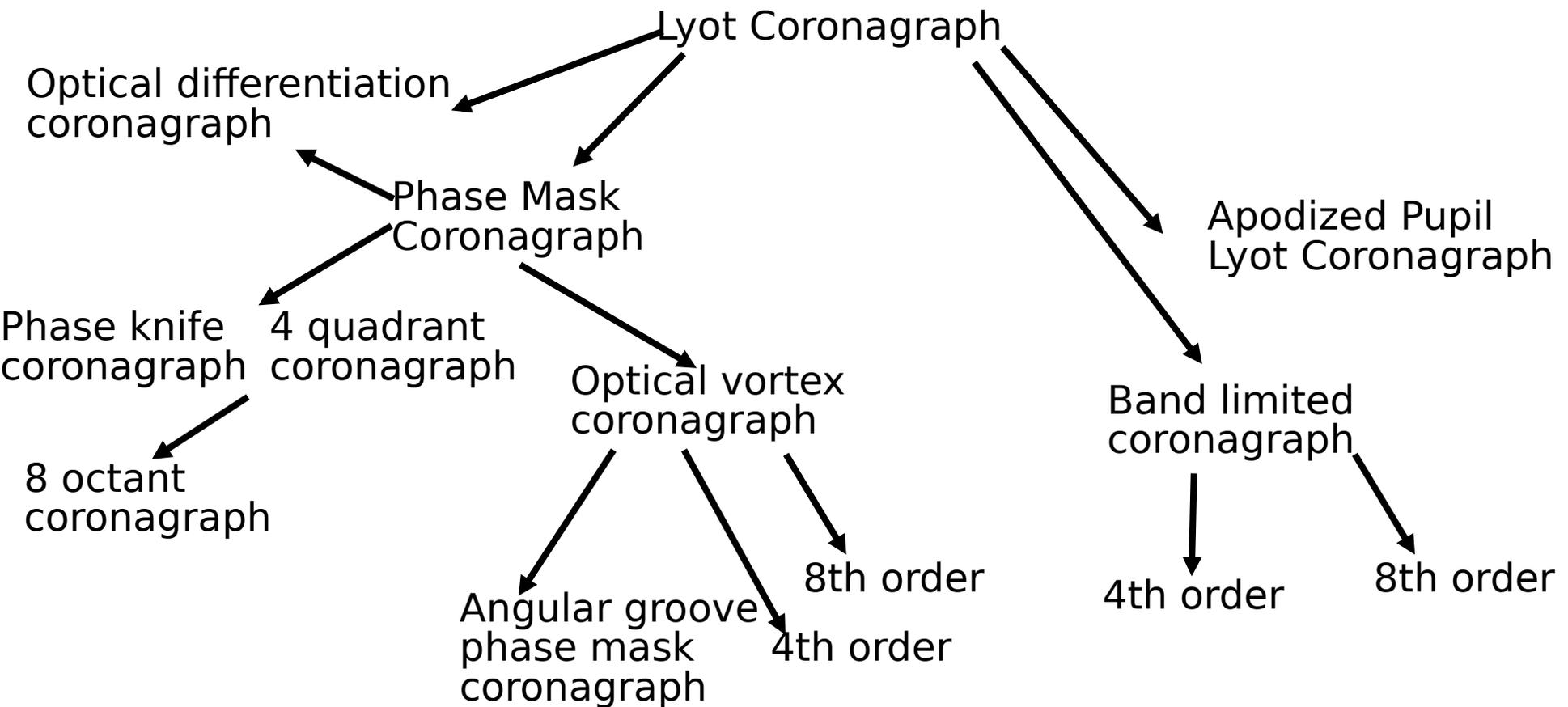
Optimization goal: make pupil dark inside Lyot mask

Possible optimizations include:

(1) Redesign of focal plane mask

- Band-limited
- Use phase as well as (or instead of) amplitude

(2) Apodize entrance aperture



# Pupil Apodization

Since Airy rings originate from sharp edges of the pupil, why not change the pupil ?

## **Conventional Pupil Apodization/ Shaped pupil**

**CPA**

[Kasdin et al. 2003](#)

Make the pupil edges fainter by absorbing light, either with a continuous or "binary" (shaped pupil) mask

## **Achromatic Pupil Phase Apodization**

**PPA**

[Yang & Kostinski, 2004](#)

Same as CPA, but achieved by a phase apodization rather than amplitude

## **Phase Induced Amplitude Apodization Coronagraph**

**PIAAC**

[Guyon, 2003](#)

Perform amplitude apodization by remapping of the pupil with aspheric optics

## **Phase Induced Zonal Zernike Apodization**

**PIZZA**

[Martinache, 2003](#)

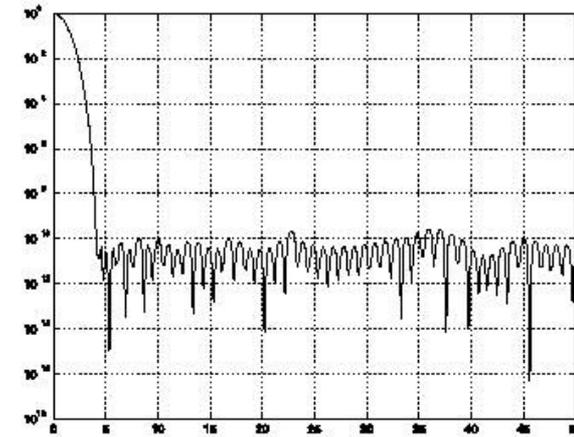
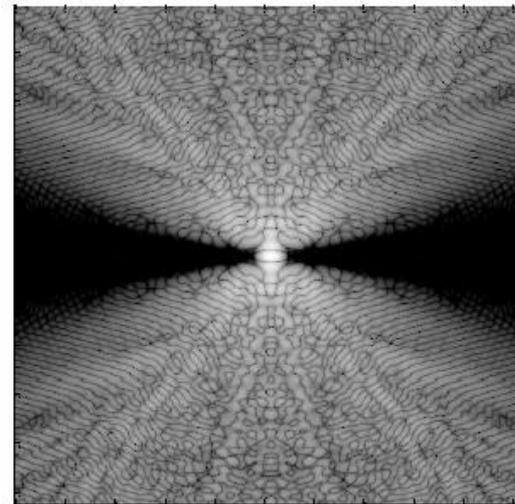
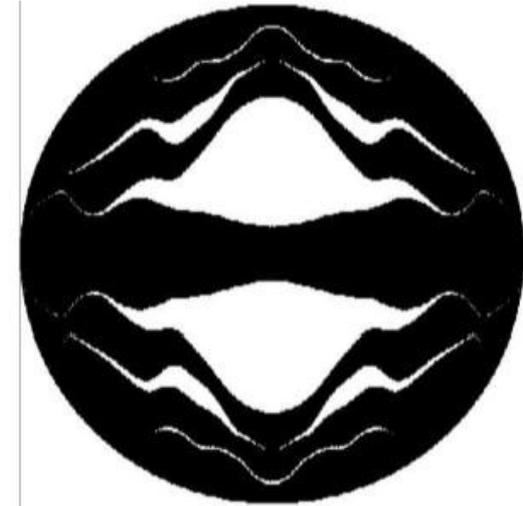
Transform a pupil phase offset into an amplitude apodization thanks to a focal plane Zernike mask

# Conventional Pupil Apodization (CPA)

Many pupil apodizations have been proposed.

Apodization can be continuous or binary.

- + Simple, robust, achromatic
- low efficiency for high contrast

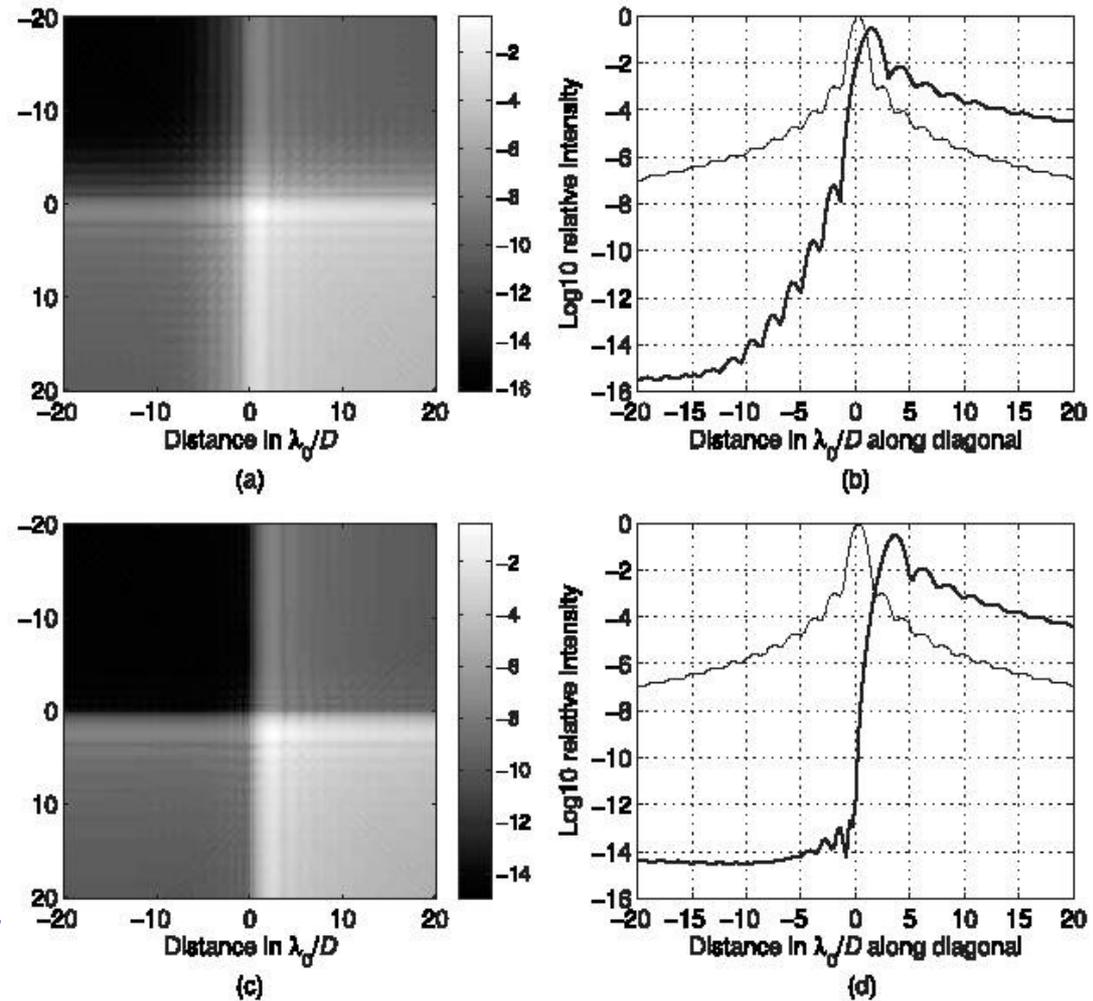


Jacquinot & Roisin-Dossier 1964  
Kasdin et al. 2003, *ApJ*, 582, 1147  
Vanderbei et al. 2003, *ApJ*, 590, 593  
Vanderbei et al. 2003, *ApJ*, 599, 686  
Vanderbei et al. 2004, *ApJ*, 615, 555

FIG. 9.—*Top*: Asymmetric multiopening mask designed to provide high-contrast,  $10^{-10}$ , from  $\lambda/D = 4$  to  $\lambda/D = 100$  in two angular sectors centered on the  $x$ -axis. Ten integrations are required to cover all angles. Total throughput and pseudoarea are 24.4%. Airy throughput is 11.85%. *Bottom*: Associated PSF. (Note that this mask was originally designed for an elliptical mirror. It has been rescaled to fit a circular aperture.)

# Pupil Phase Apodization (PPA)

Achromatic solutions exist.



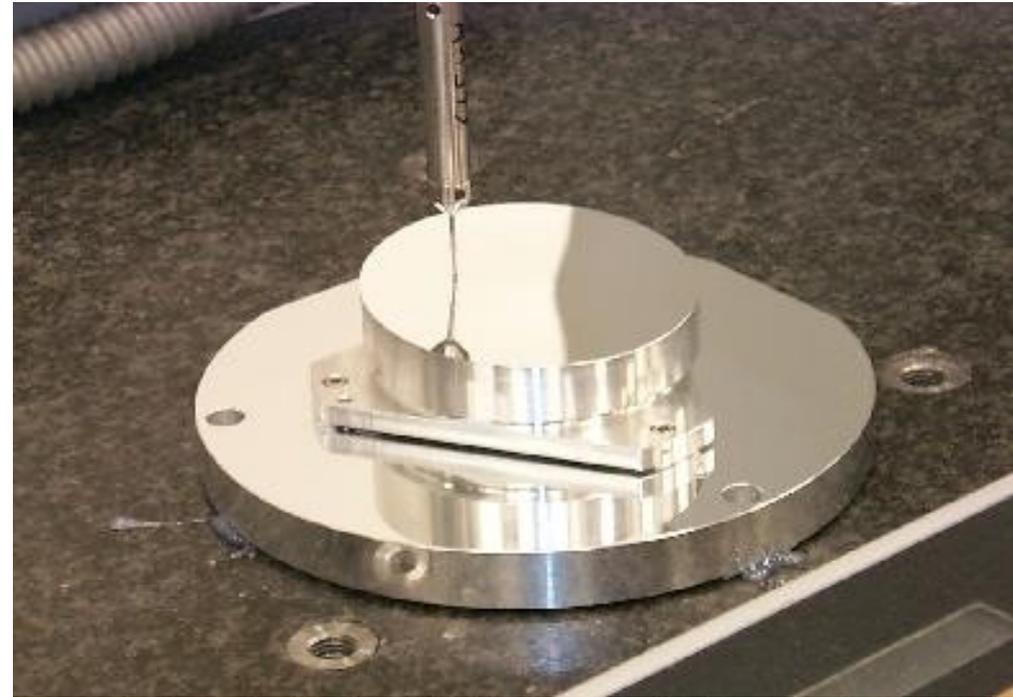
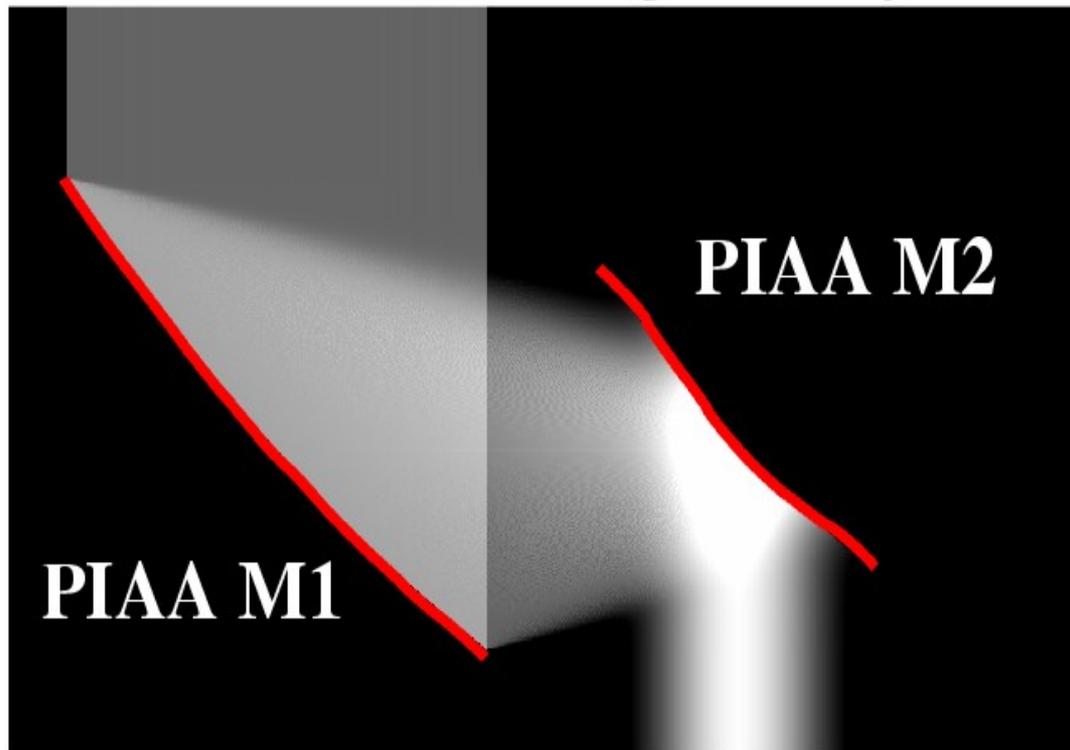
Yang & Kostinski 2004, ApJ, 605, 892  
Codona & Angel 2004, ApJ, 604, L117

FIG. 9.—Broad-bandwidth light reduction effect on one quadrant of focal plane. The simulation is based on a rectangular spectrum distribution with total bandwidth of  $0.6\lambda_0$ . (a)  $\log_{10}$  relative intensity image when phase  $\phi(x, y) = a \tan[0.5 - \epsilon]2\pi x/D + a \tan[0.5 - \epsilon]2\pi y/D$ , with  $a = 1$  and  $\epsilon = 0.005$ , is applied to a square pupil. (b) The thicker line represents the  $\log_{10}$  relative intensity along the diagonal line crossing the second and the fourth quadrants in (a). The thinner line represents the one without phase modulation. (c) Same as (a), but with phase  $\phi(x, y)$  from eq. (11), with  $a = 3$  and  $\epsilon = 0.001$ , applied to a square pupil. (d) Same as (b), but for the quadrants in (c). One can see that the reduction level of  $10^{-12}$ , with an inner working distance of about  $3.5\lambda_0/D$ , can still be kept with a broad bandwidth of  $0.6\lambda_0$  in the second quadrant.

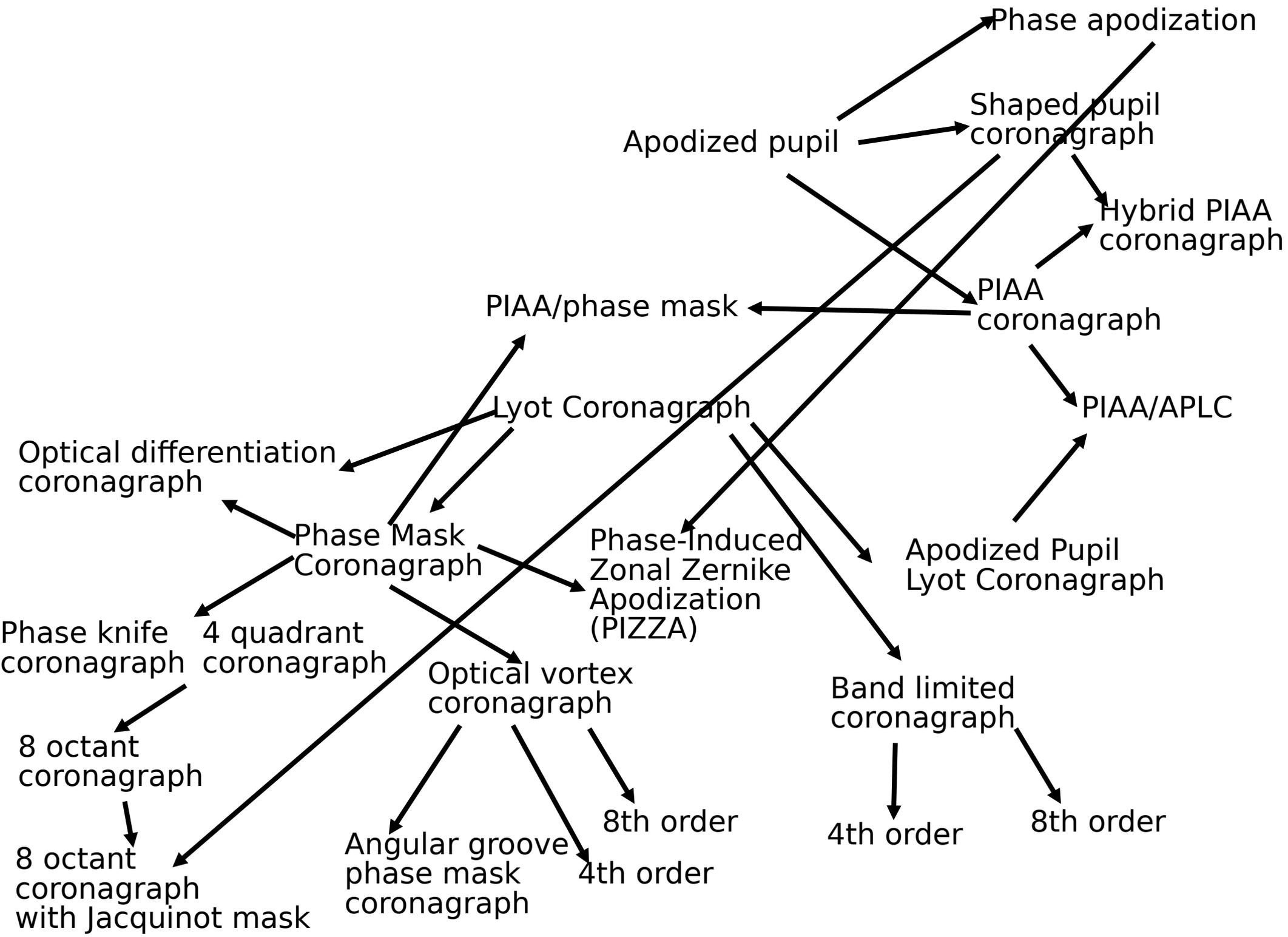
# Phase-Induced Amplitude Apodization Coronagraph (PIAAC)

Lossless apodization by aspheric optics.

Light intensity



Guyon, Belikov, Pluzhnik, Vanderbei, Traub, Martinache ... 2003-present



# "Interferometric" coronagraphs

= **Nulling interferometer on a single pupil telescope**

- Creates multiple (at least 2) beams from a single telescope beam
- Combines them to produce a destructive interference on-axis and constructive interference off-axis

## **Achromatic Interferometric Coronagraph Common Path AIC**

**AIC  
CPAIC**

[Baudoz et al. 2000](#), [Tavrov et al. 2005](#)

Destructive interference between pupil and flipped copy of the pupil  
Achromatic PI phase shift and geometrical flip performed by going through focus

## **Visible Nulling Coronagraph, X & Y shear, 4<sup>th</sup> order**

**VNC**

[Shao et al.](#), [Menesson et al. 2003](#)

Destructive interference between 2 copies of the pupil, sheared by some distance.  
4<sup>th</sup> order null obtained by cascading 2 shear/null

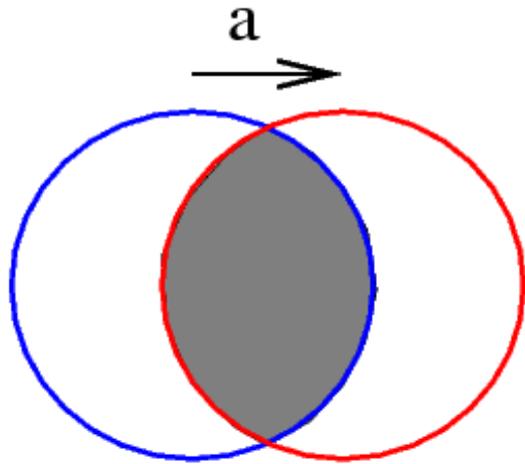
## **Pupil Swapping Coronagraph**

**PSC**

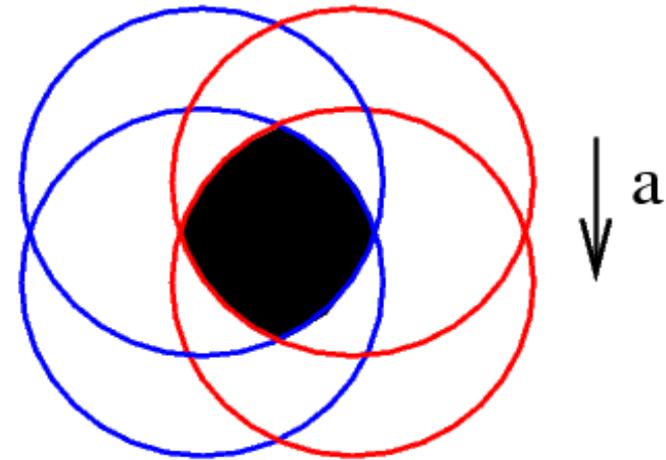
[Guyon & Shao, 2006](#)

Destructive interference between pupil and a copy of the pupil where 4 quadrants have been swapped

# Visible Nuller Coron. (VNC)



second order null  
phase offset prop. to  
pupil shear x source offset



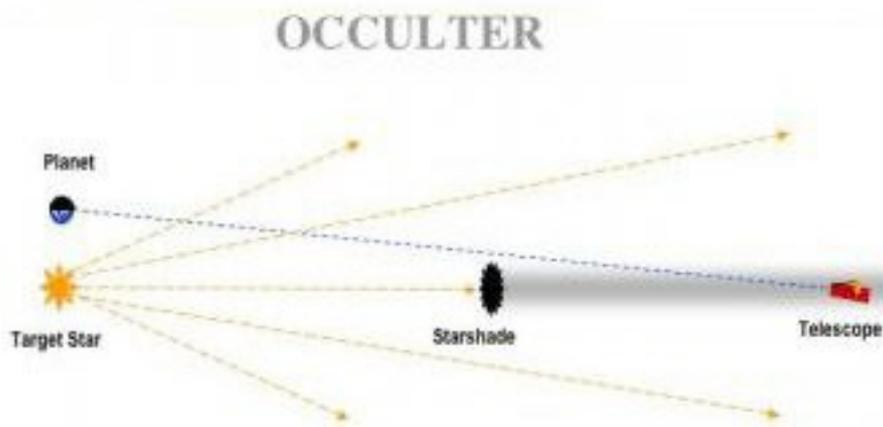
4th order null

Small shear : high throughput, low IWA  
Large shear : low throughput, small IWA  
The 2 shears can also be colinear

**Sounding rocket  
(PICTURE)**



# External Occulter



A properly placed and shaped occulter can drop a deep shadow of starlight over a telescope while allowing planet light to pass unimpeded.

