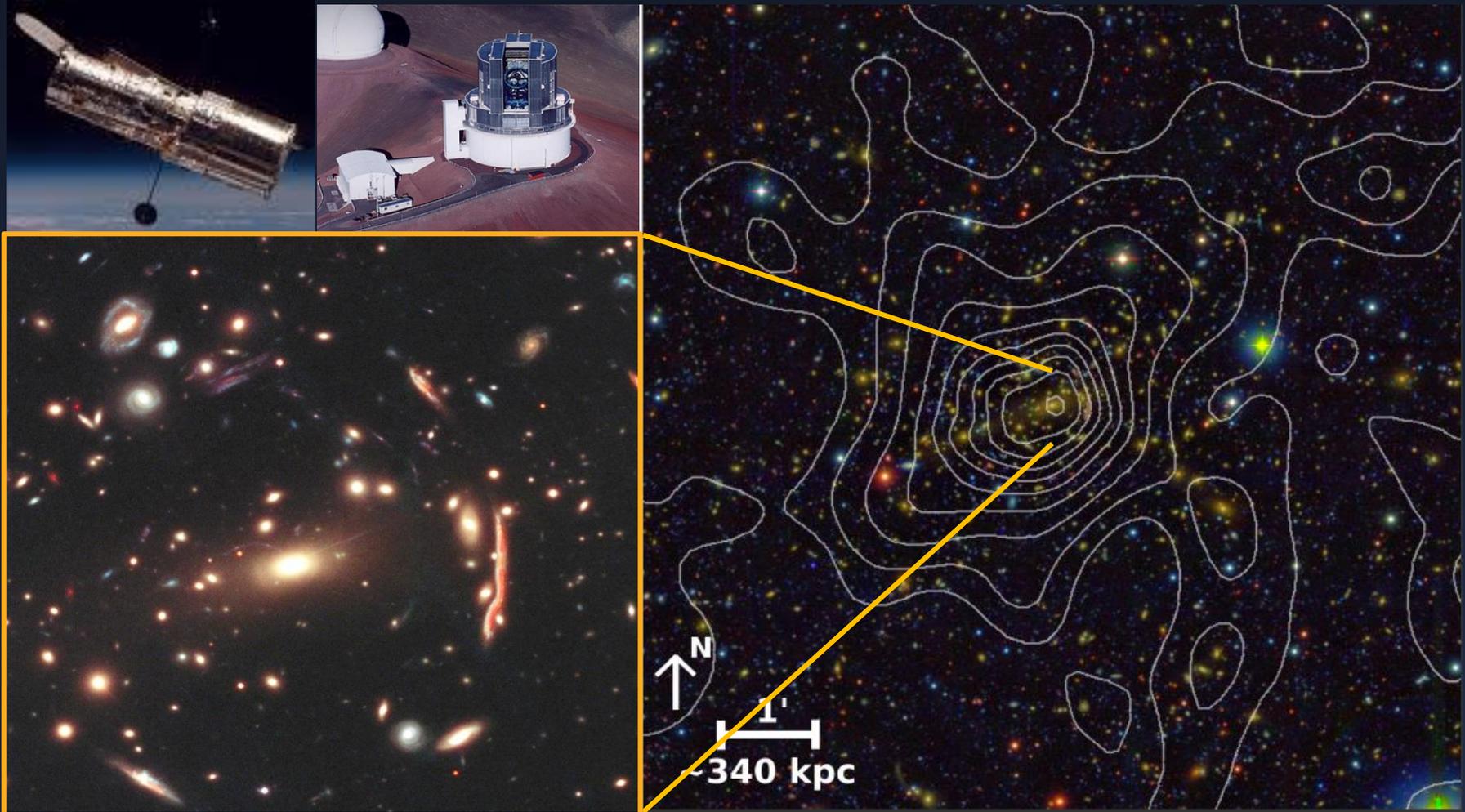


# Cluster Gravitational Lensing with Subaru

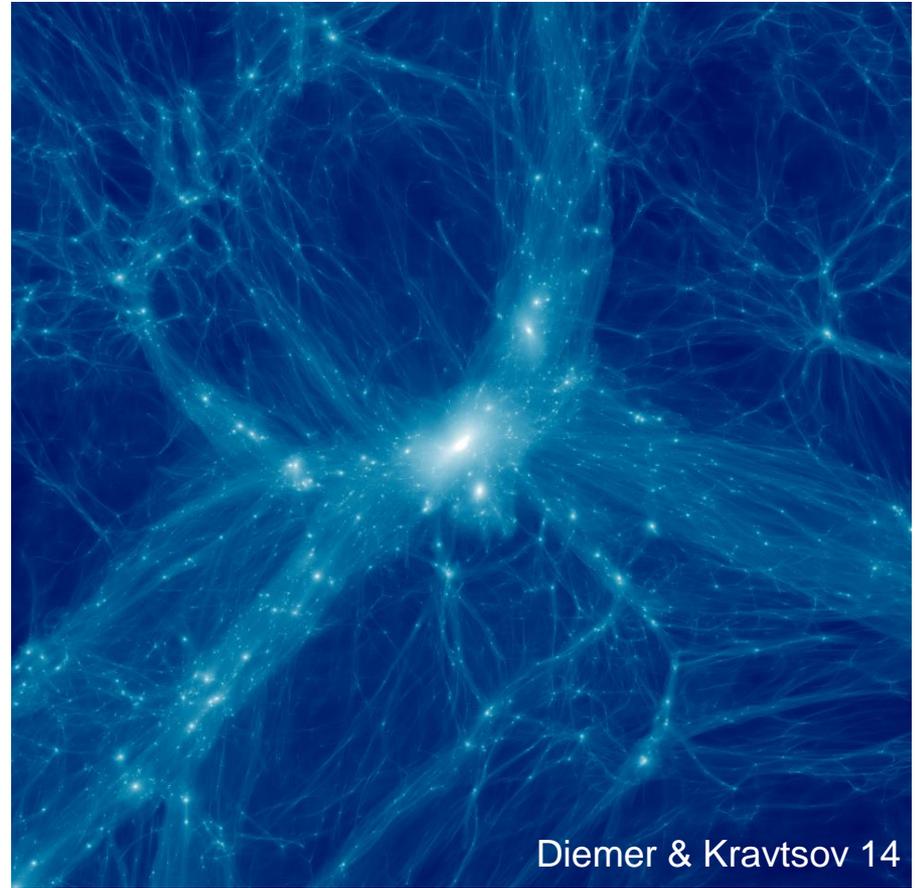
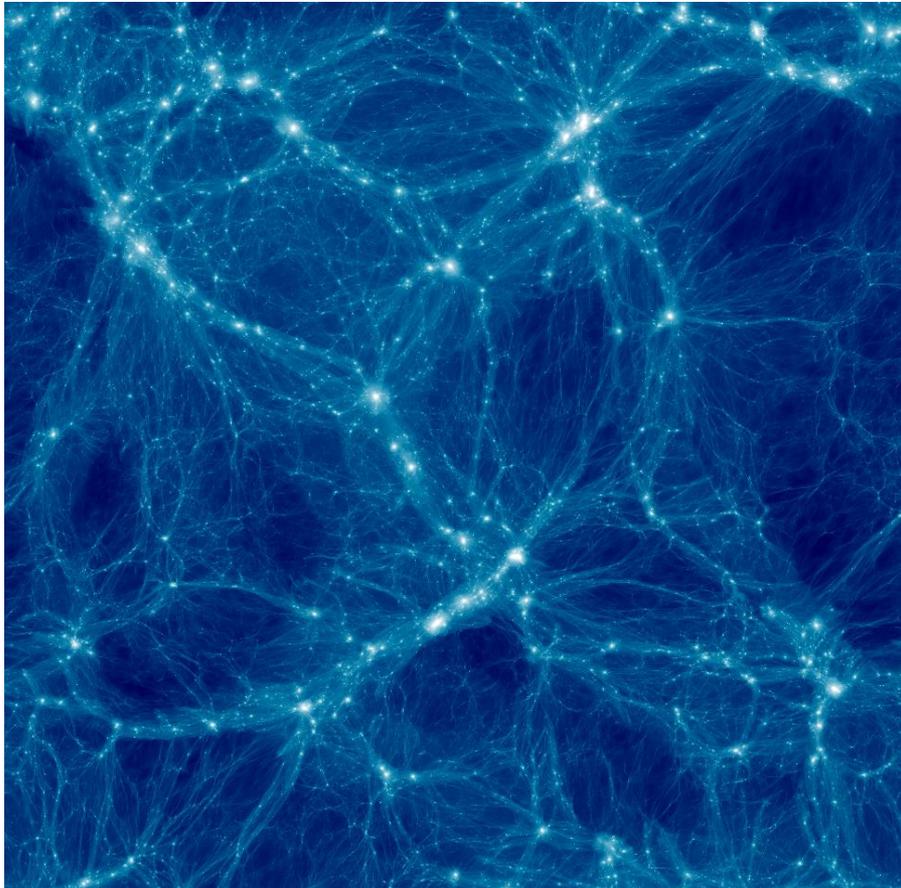


Keiichi Umetsu (ASIAA, since 2001)

# My Science Interests

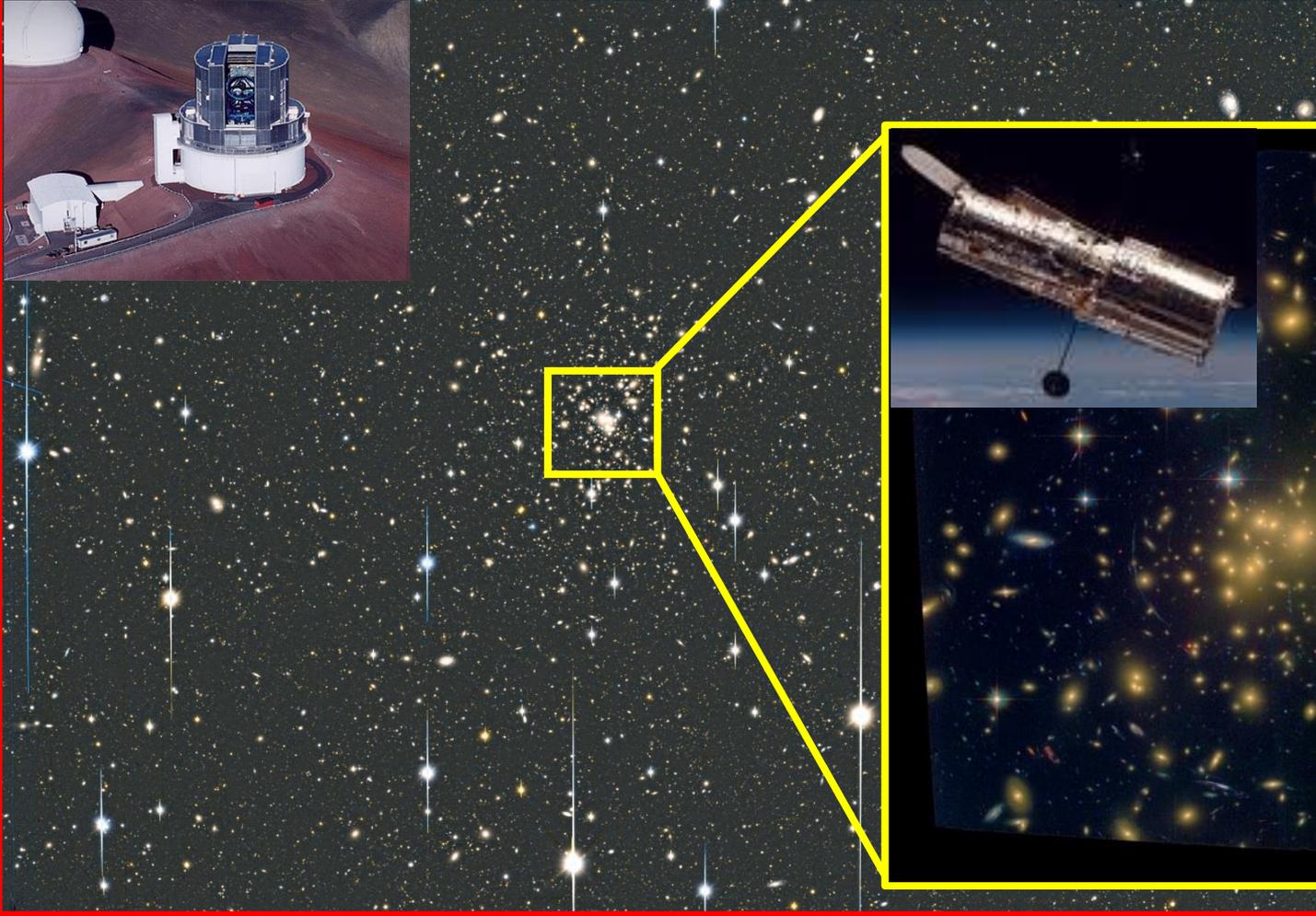
## **Nature of dark matter and its role in cosmic structure formation**

Study galaxy clusters and their surrounding environments using (weak + strong) gravitational lensing as a direct probe



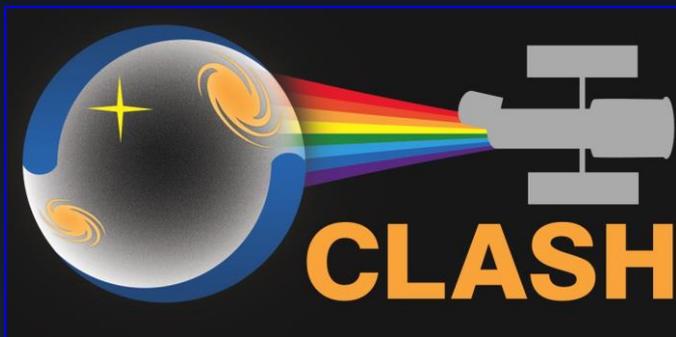
**Subaru/Suprime-Cam multi-color imaging for wide-field weak lensing**

**High-resolution space imaging with *HST* (ACS/WFC3) for strong lensing**



34 arcmin

# Cluster Lensing And Supernova survey with Hubble



524-orbit *HST* Treasury Program (2010-2013) to deeply observe 25 high-mass clusters in 16 filters (ACS/WFC3)

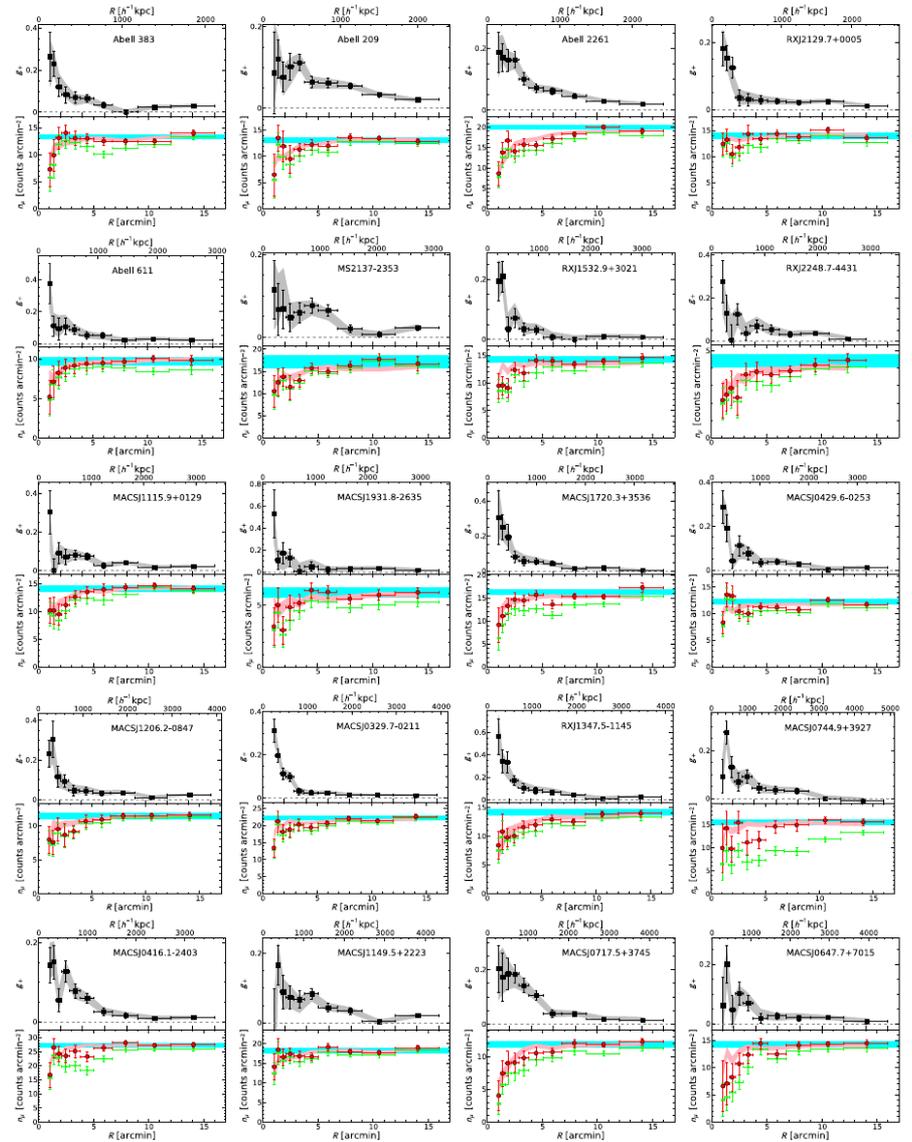
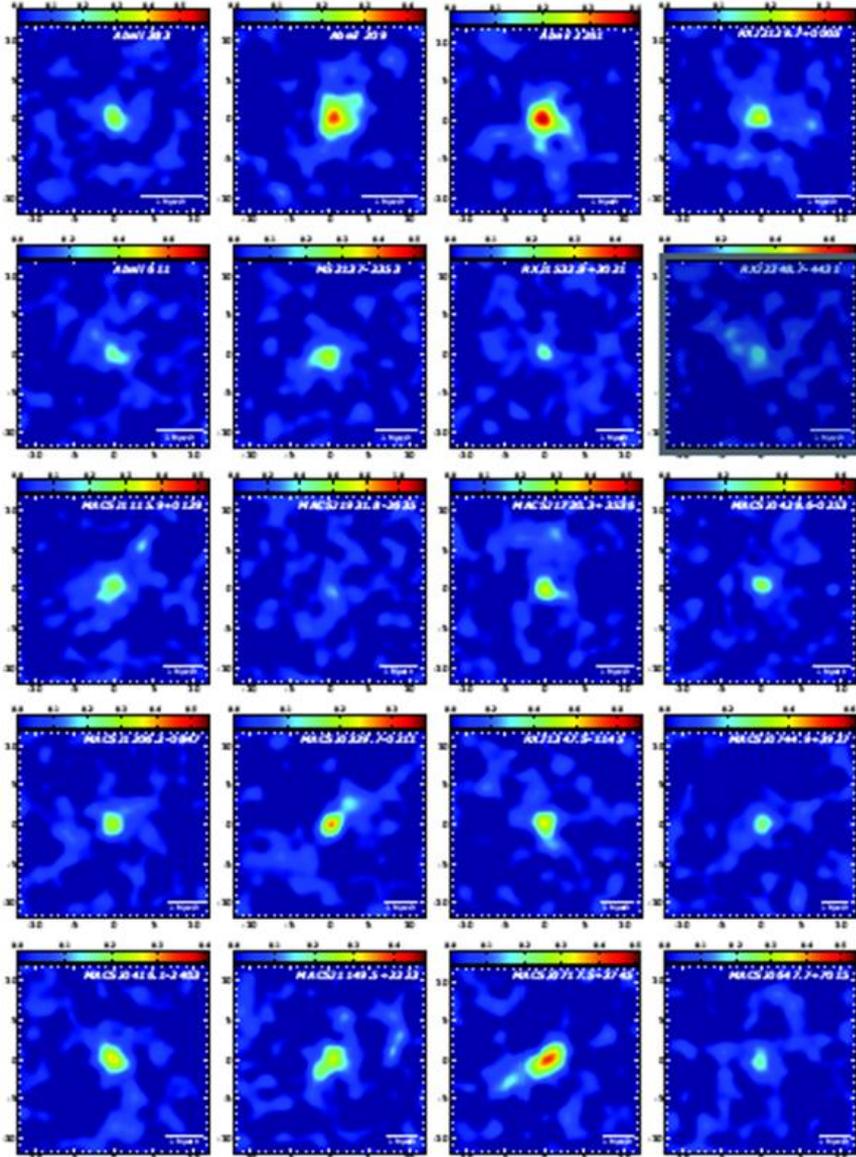
PI. Marc Postman (STScI)

## Major science goals, targeting

- 1. 20 X-ray-selected relaxed high-mass clusters**
  - Establish the equilibrium cluster density profile
  - Test LCDM predictions of the concentration-mass relation
- 2. 5 high-magnification clusters**
  - Search for and study magnified high- $z$  ( $z > 8$ ) galaxies

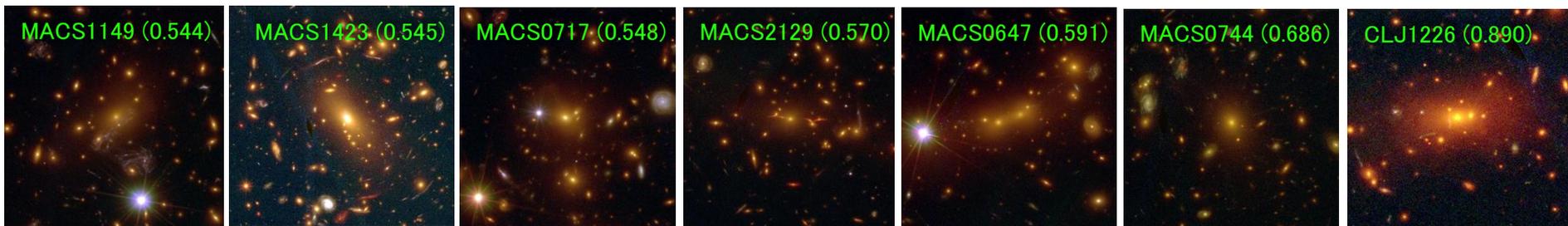
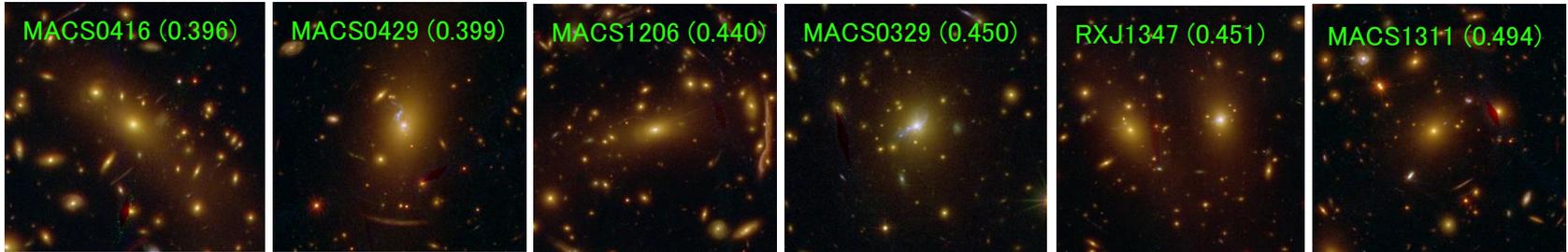
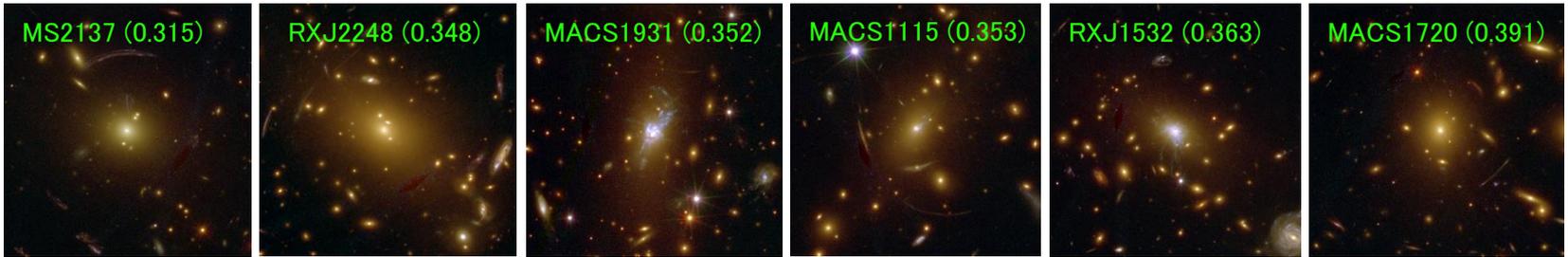


# CLASH Subaru Weak-lensing Dataset



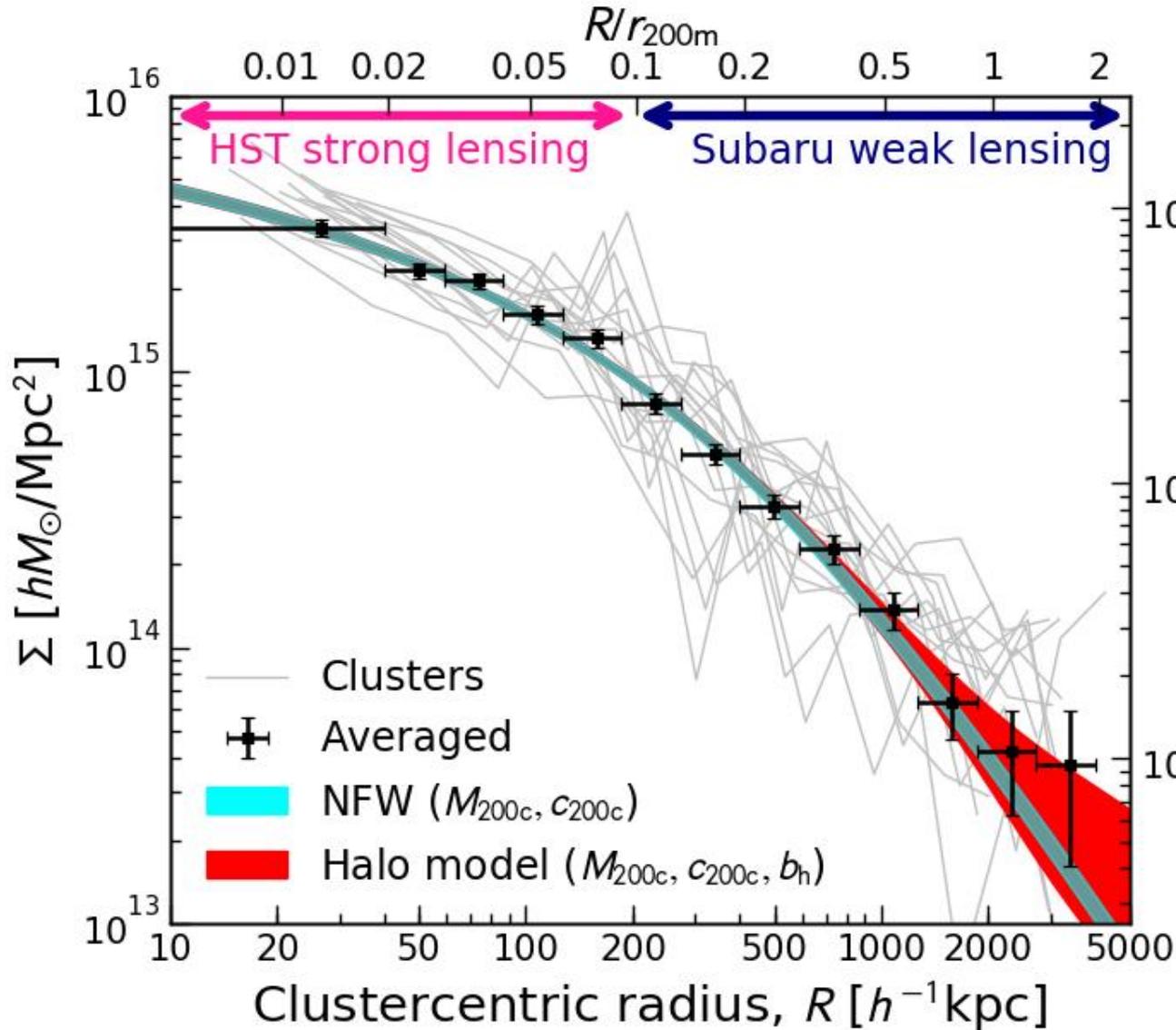


# CLASH *HST* Strong-lensing Dataset





# Results: Ensemble Mass Density Profile



Convergence,  $\kappa$

$$c_{200c} := \frac{R_{200c}}{r_s} = 3.79^{+0.30}_{-0.28}$$

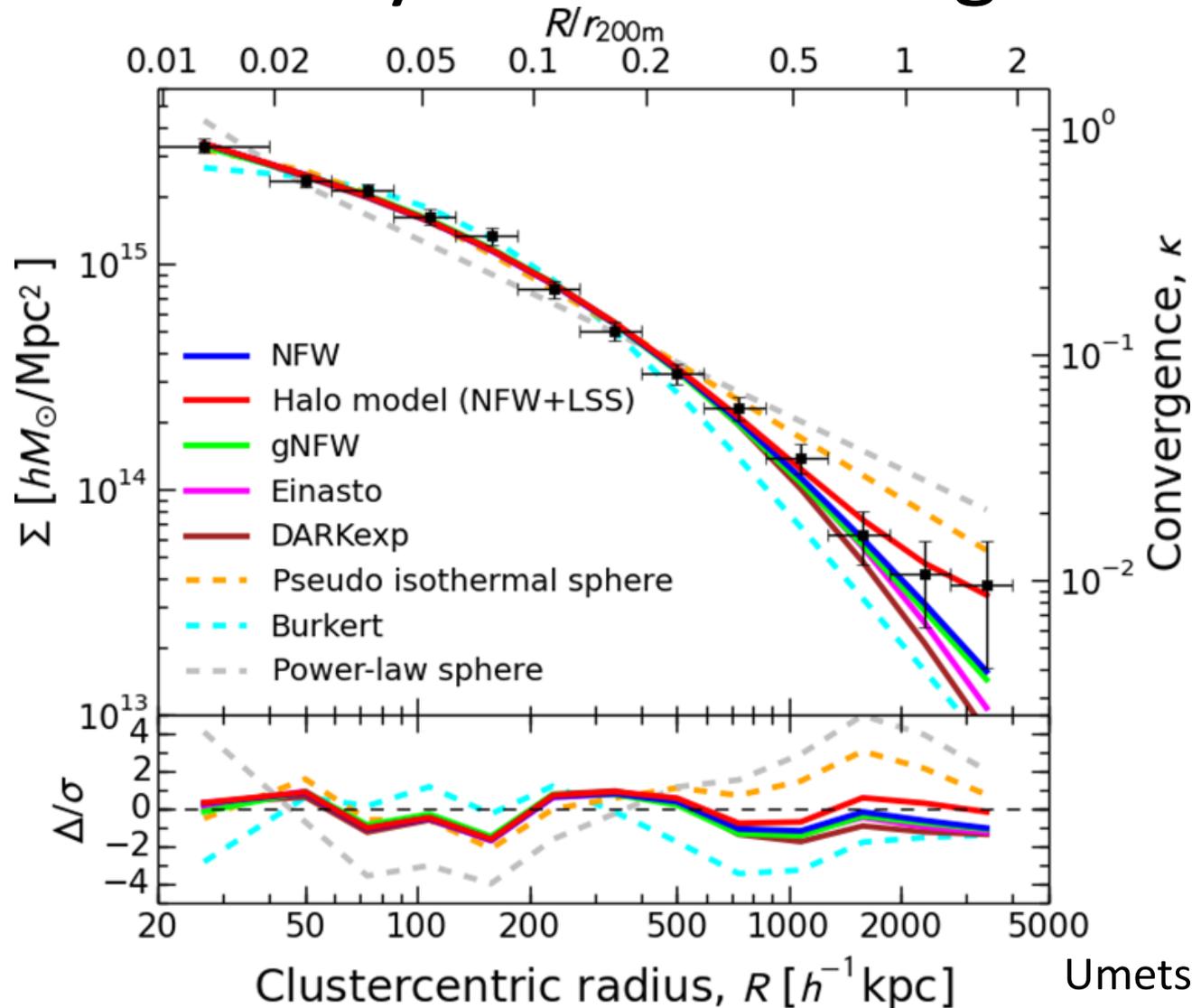
$$M_{200c} = 1.4^{+0.1}_{-0.1} \times 10^{15} M_{\text{sun}}$$

$$\langle z \rangle \approx 0.34$$

Umetsu et al. 2016

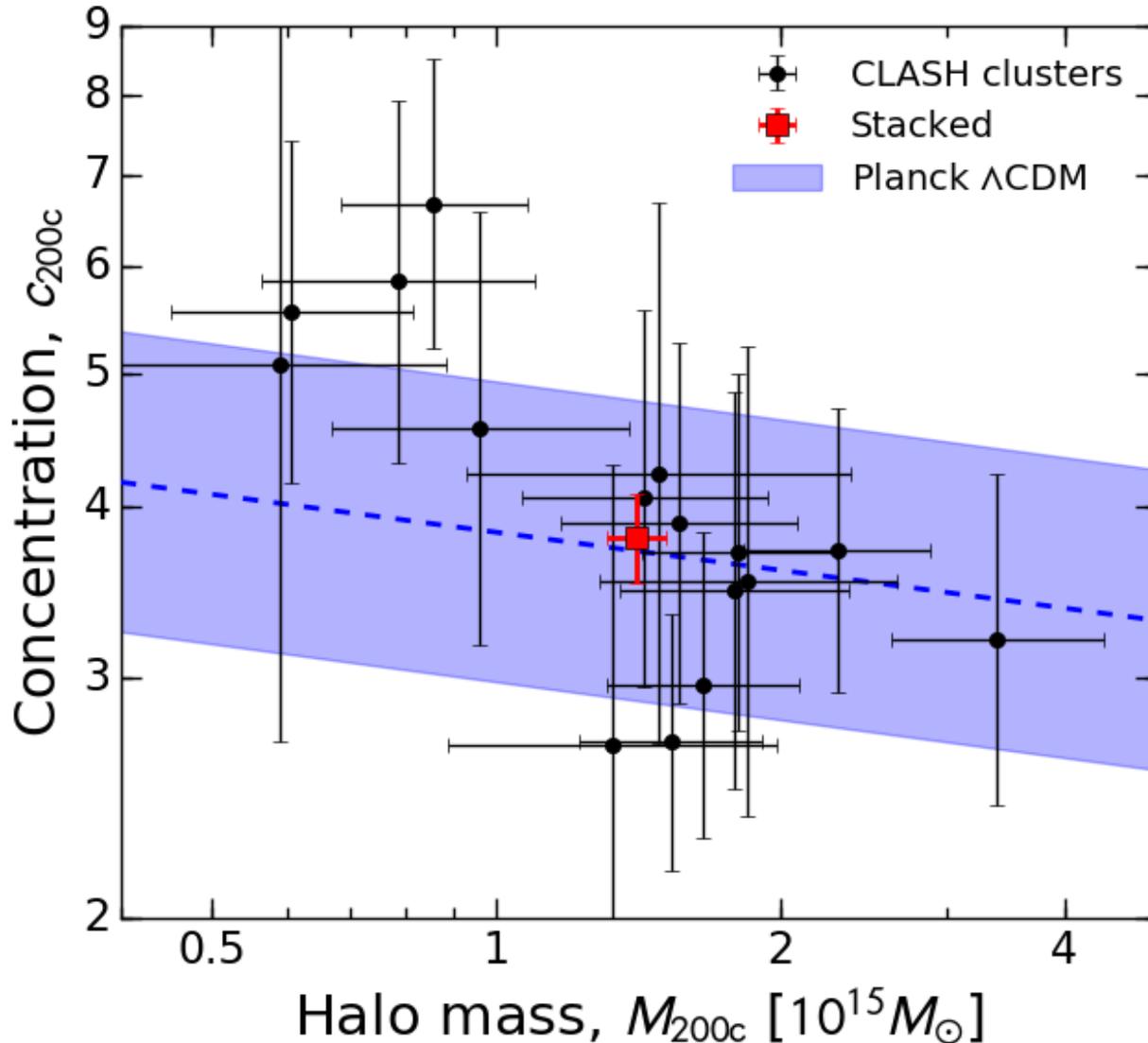


# Cuspy outward steepening profiles favored by CLASH lensing data





# Results: Concentration–Mass Relation



## Stacked CLASH lensing

$$c_{200c} = 3.79^{+0.30}_{-0.28}$$

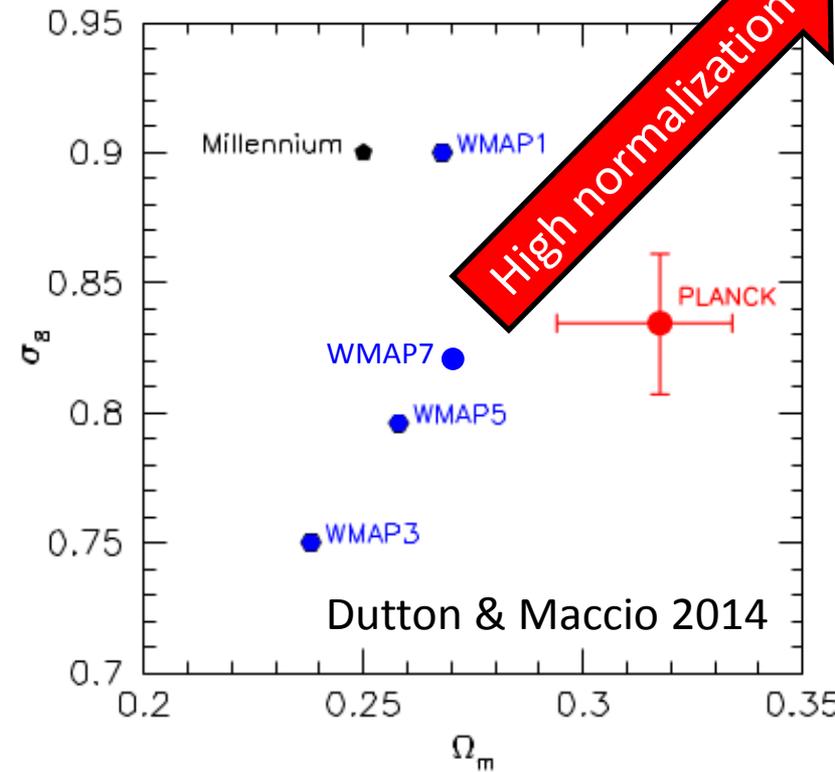
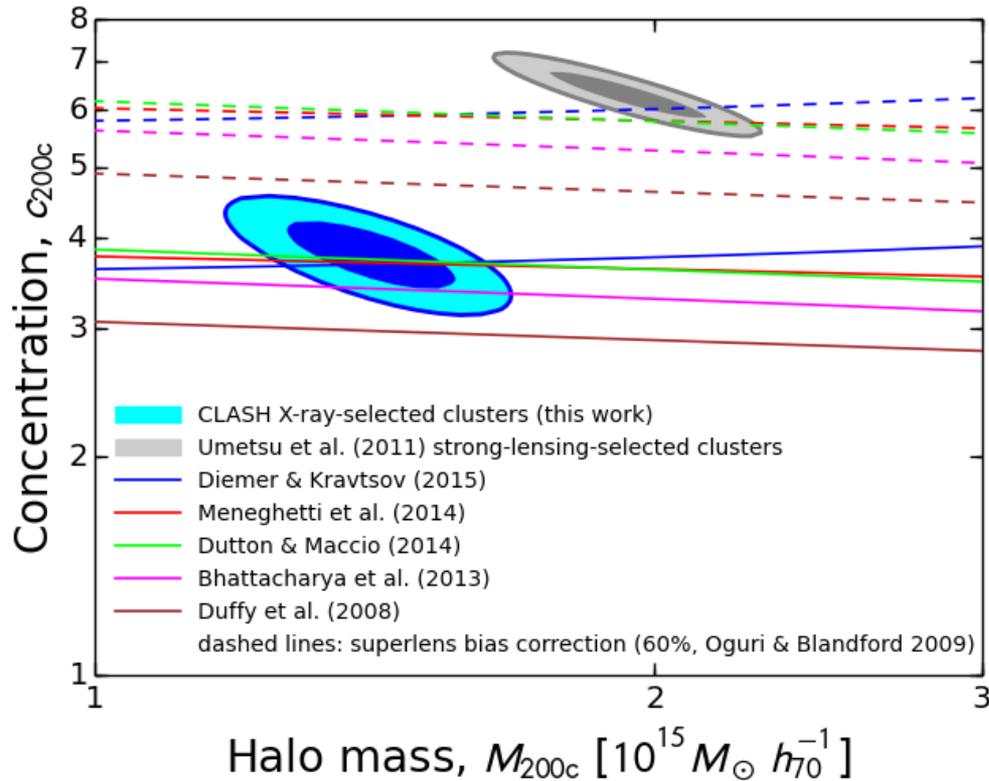
$$\text{at } M_{200c} = 1.4^{+0.1}_{-0.1} \times 10^{15} M_{\text{sun}}$$

Consistent with  $c$ - $M$  relations calibrated for recent cosmologies (WMAP7 and later)



# CLASH vs. Superlens Clusters

- 16 **lensing-unbiased** CLASH clusters (Umetsu+16)
- 4 **superlens** clusters with Einstein radius  $>30''$  (Umetsu+11b)



Higher normalization LCDM cosmology (WMAP7 and later) + predicted 60% superlens correction can explain superlens mass profiles!

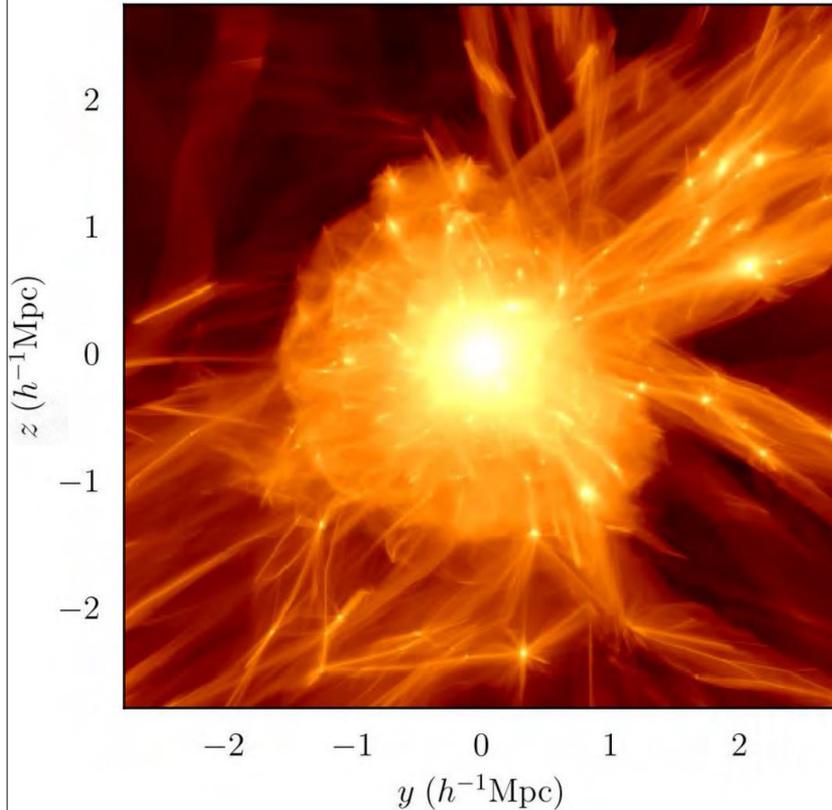
# **CLASH Lensing Constraints on the Splashback Radius of Galaxy Clusters**

Umetsu & Diemer 2017, *ApJ*, 836, 231

# Splashback radius, $R_{sp}$ : Physical halo boundary

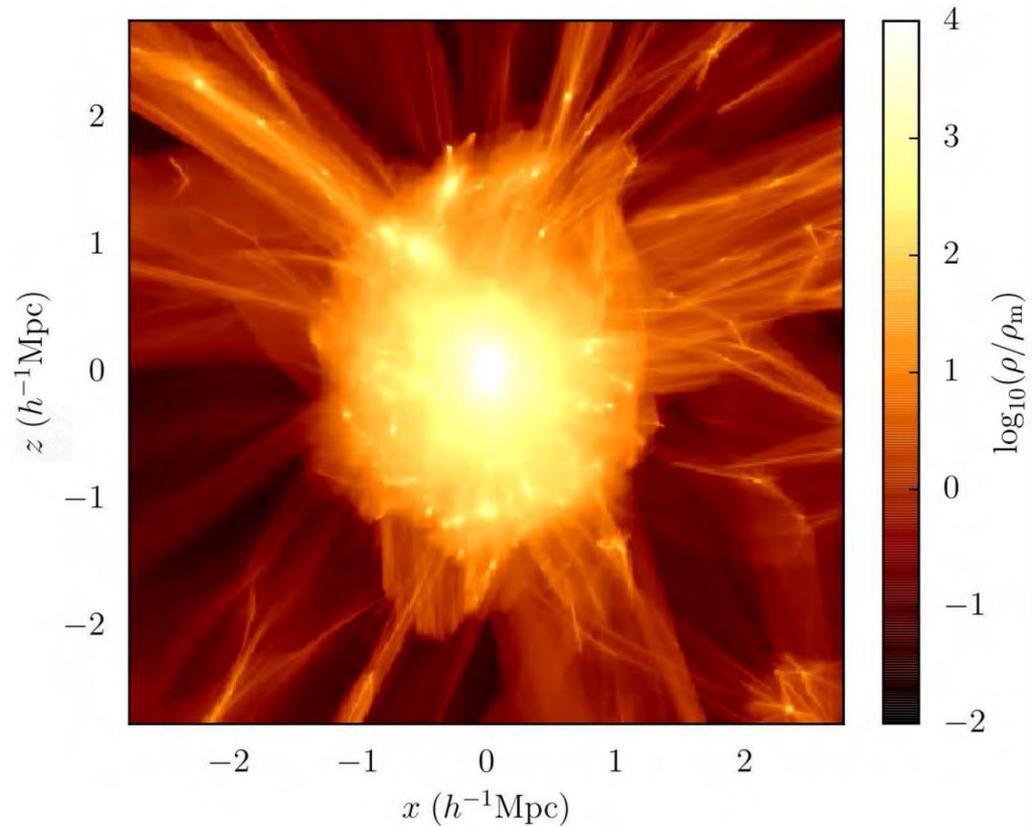
## Slow accreting halos

$$R_{sp} \gg R_{200m}$$



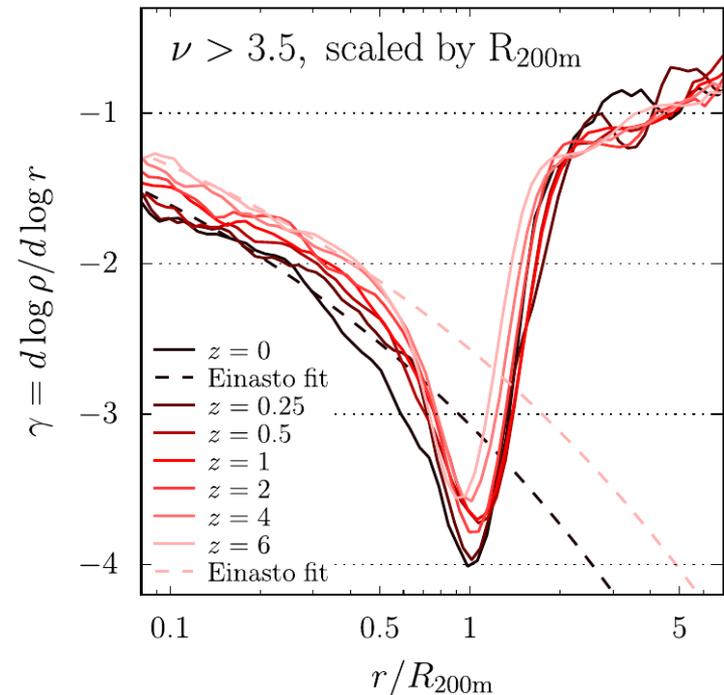
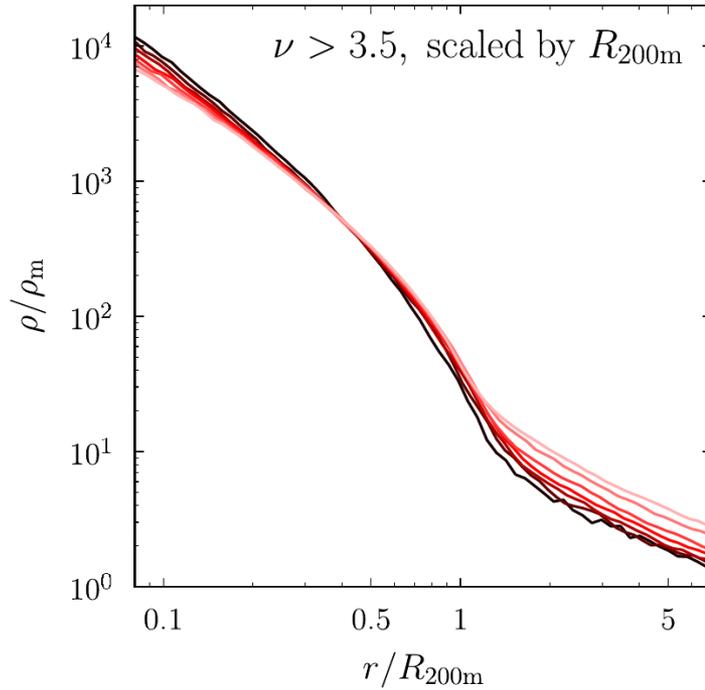
## Fast accreting halos

$$R_{sp} \sim R_{200m}$$



# Splashback feature in real space

Steepest “3D” gradient point as splashback radius  $R_{sp}$



*N*-body simulations (Diemer & Kravtsov 14, DK14)

## Practical issues

- CLASH spans a factor of  $\sim 5$  (1.7) in mass (radius), so that sharp gradient feature is washed out when stacked in physical length units.
- In 2D, the splashback feature is weakened by projection of shallow 2-halo term

# Solution: Parametric forward modeling of “scaled” cluster lensing profiles

Mass distribution around halos in  $\Lambda$ CDM (DK14)

$$\Delta\rho(r) = \rho(r) - \rho_m = \rho_{\text{inner}} \times f_{\text{trans}} + \rho_{\text{outer}}$$

**A scaled version of DK14 density profile (Umetsu & Diemer 17)**

$$\Delta\rho(r = r_\Delta x) = \mathcal{N} \left\{ \exp \left[ -\frac{2}{\alpha} c_\Delta^\alpha (x^\alpha - 1) \right] \left[ 1 + \left( \frac{x}{\tau_\Delta} \right)^\beta \right]^{-\gamma/\beta} + \frac{B_\Delta}{\epsilon_\Delta + x^{s_e}} \right\}$$
$$\propto f_{\text{inner}}(x) f_{\text{trans}}(x) + f_{\text{outer}}(x),$$

$$y(x) := \frac{\Sigma(R = r_\Delta x)}{\Sigma(r_\Delta)}$$

specified by  $\mathbf{p} = \{c_\Delta, \alpha, \tau_\Delta, B_\Delta, s_e, \beta, \gamma\}$ .

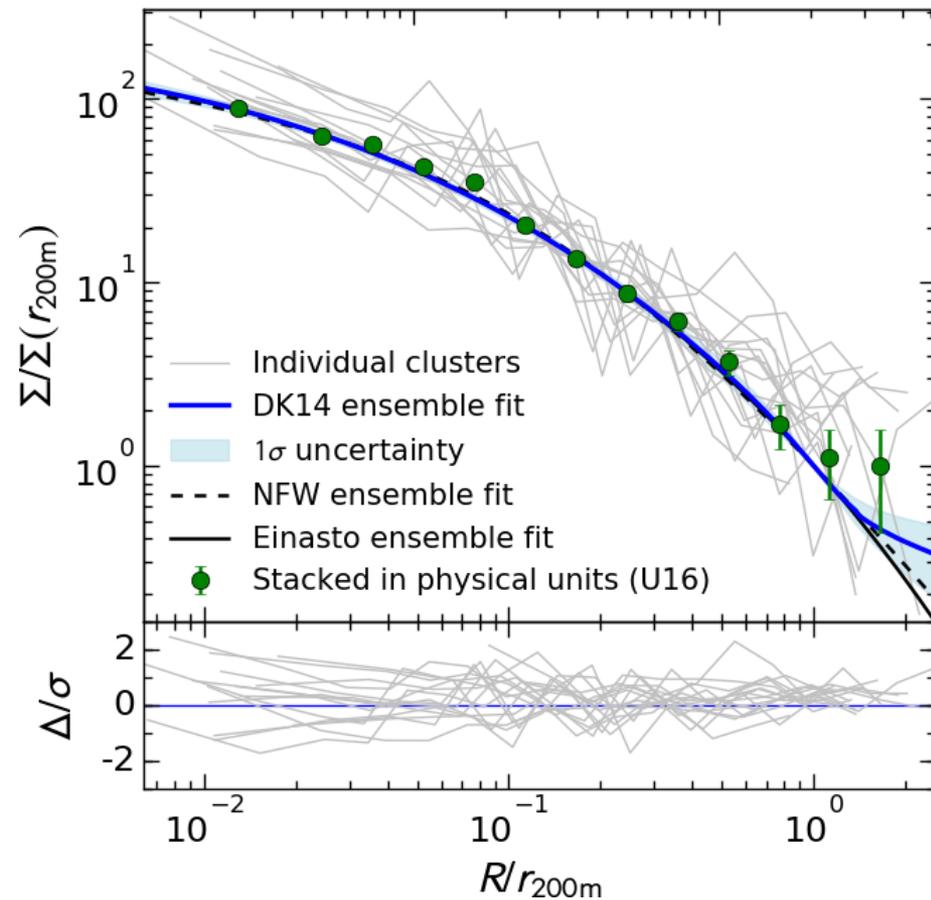
We marginalize over nuisance shape parameters ( $s_e, \beta, \gamma$ ) using “generic” priors found from  $N$ -body simulations of DK14



# Results: CLASH scaled density profiles

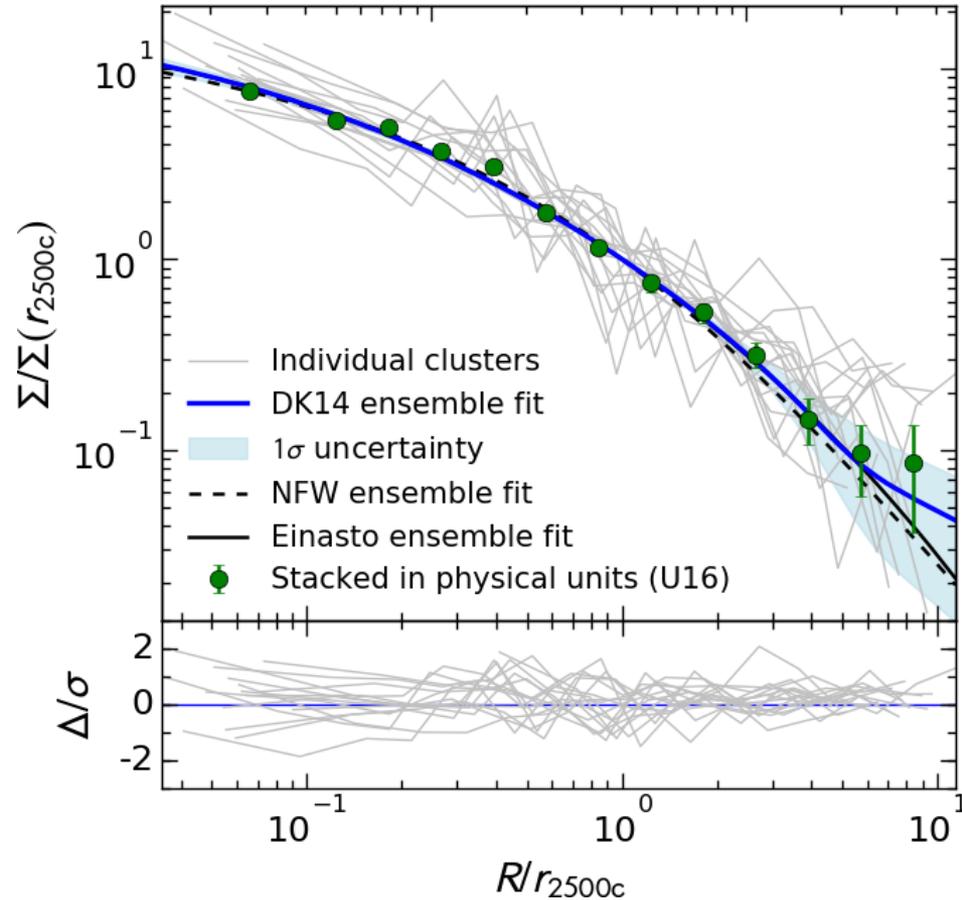
$$r_{\Delta} = r_{200m}$$

$R$  [physical  $h^{-1}$  kpc]  
 $10^2$   $10^3$



$$r_{\Delta} = r_{2500c} \sim 0.2r_{200m}$$

$R$  [physical  $h^{-1}$  kpc]  
 $10^2$   $10^3$

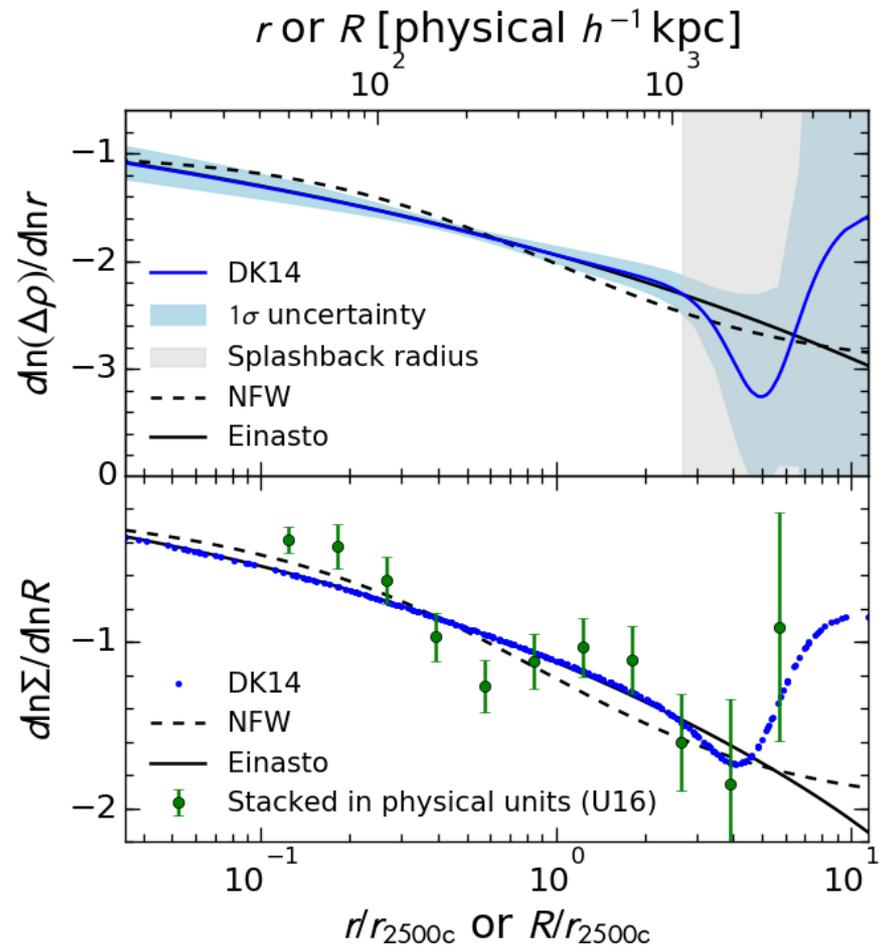
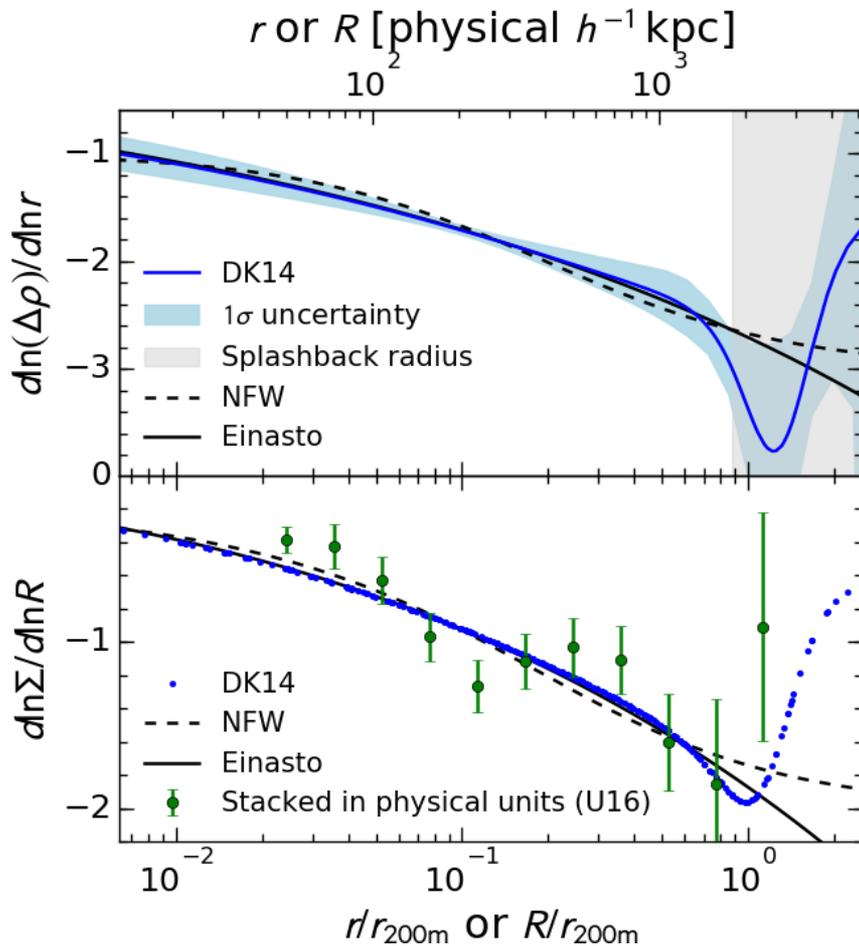




# Results: CLASH logarithmic density gradient

$$r_{\Delta} = r_{200m}$$

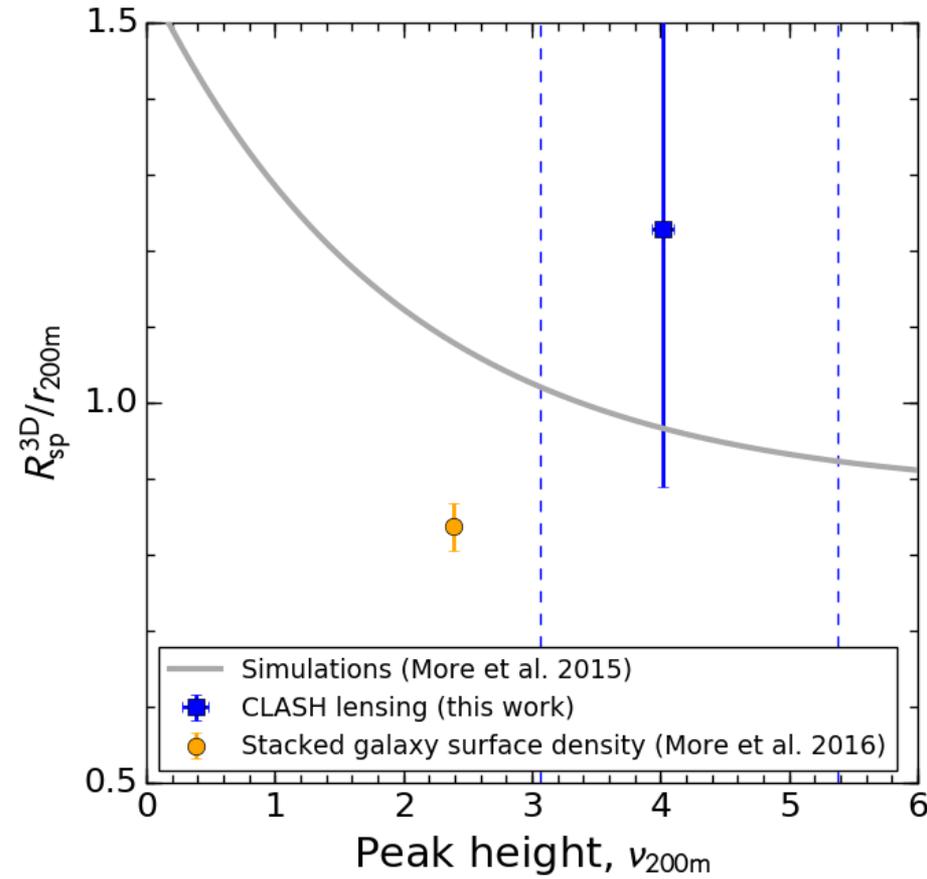
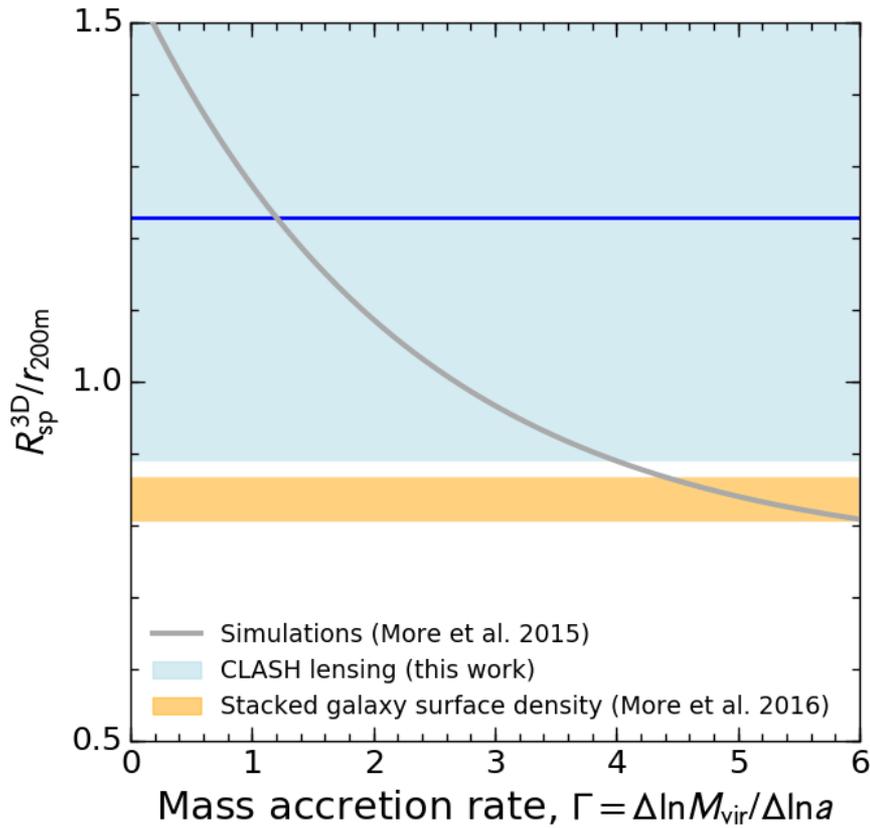
$$r_{\Delta} = r_{2500c} \sim 0.2r_{200m}$$





# First lensing constraints on $R_{\text{sp}}$

$$R_{\text{sp}}^{3\text{D}} / r_{200\text{m}} = 1.23^{+2.33}_{-0.34} \Rightarrow \Gamma := \frac{\Delta \ln M_{\text{vir}}}{\Delta \ln a} < 4.0 (1\sigma)$$

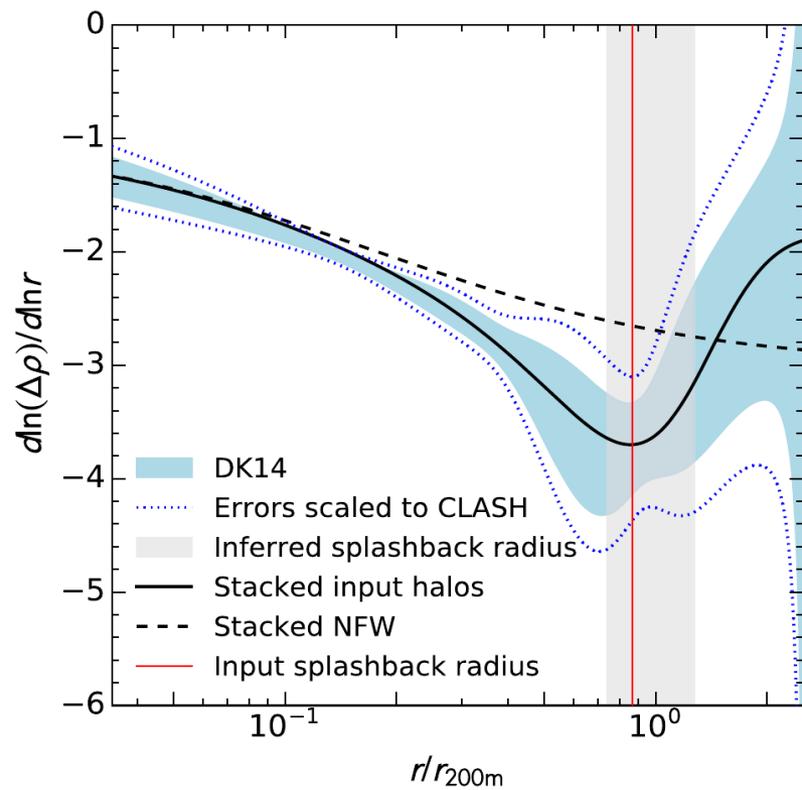
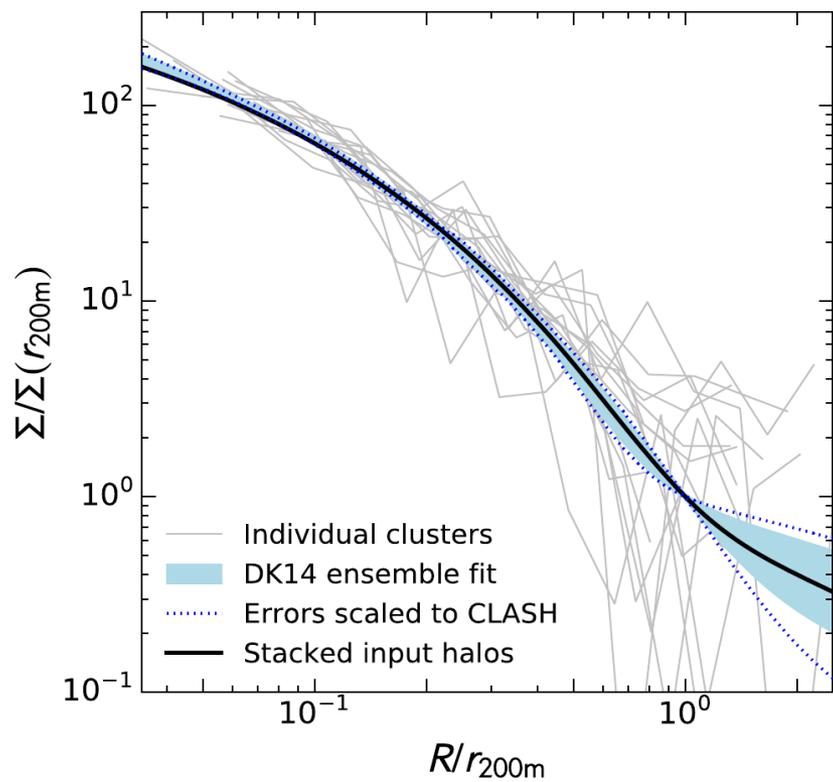


CLASH data consistent with a representative range of MAR

# Next steps?

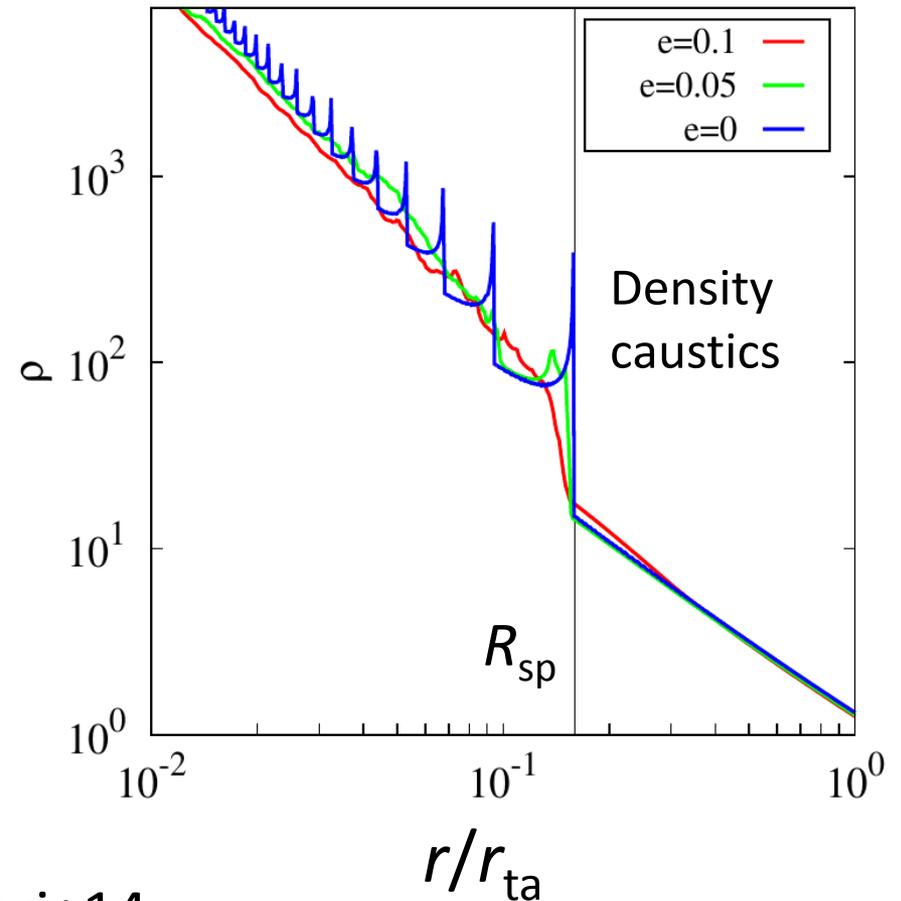
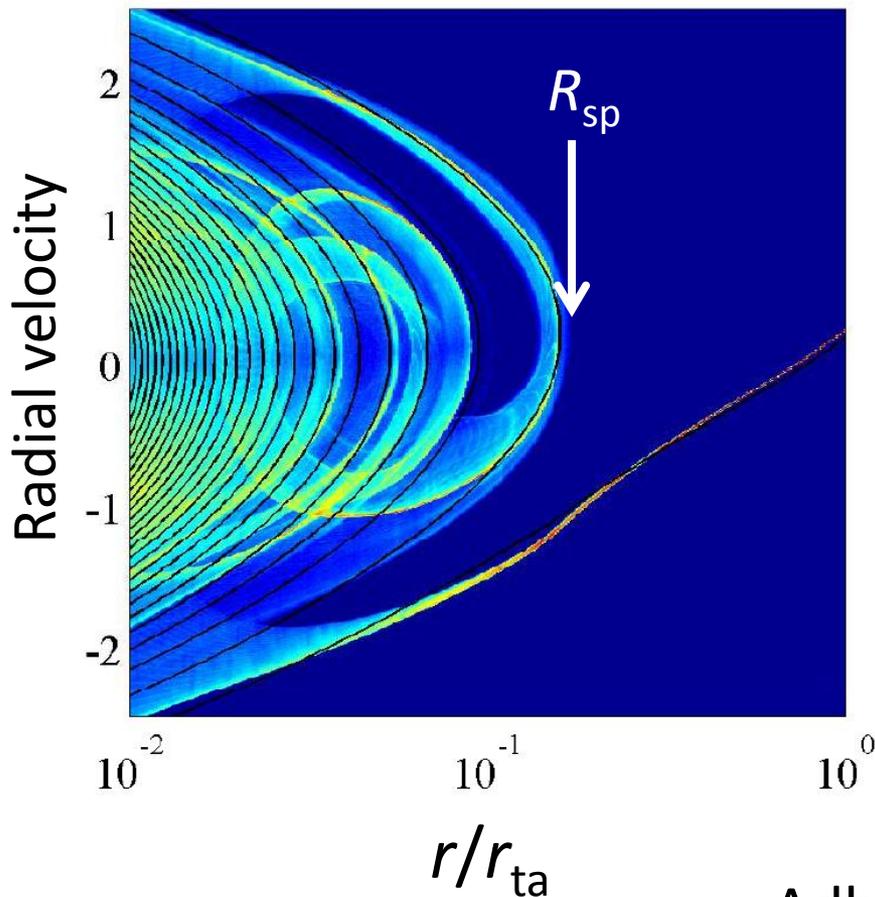
- Exploring low mass clusters/groups, higher- $z$  systems ( $z > 1$ ) with HSC-SSP (1400 deg<sup>2</sup>)
- Lensing “detection” of  $R_{sp}$  using improved statistics with HSC-SSP Large statistics of merging clusters with HSC-SSP.
- BCG-cluster-LSS connection: tidal effects, alignments, assembly histories of dark matter halos

# Supplemental Slides

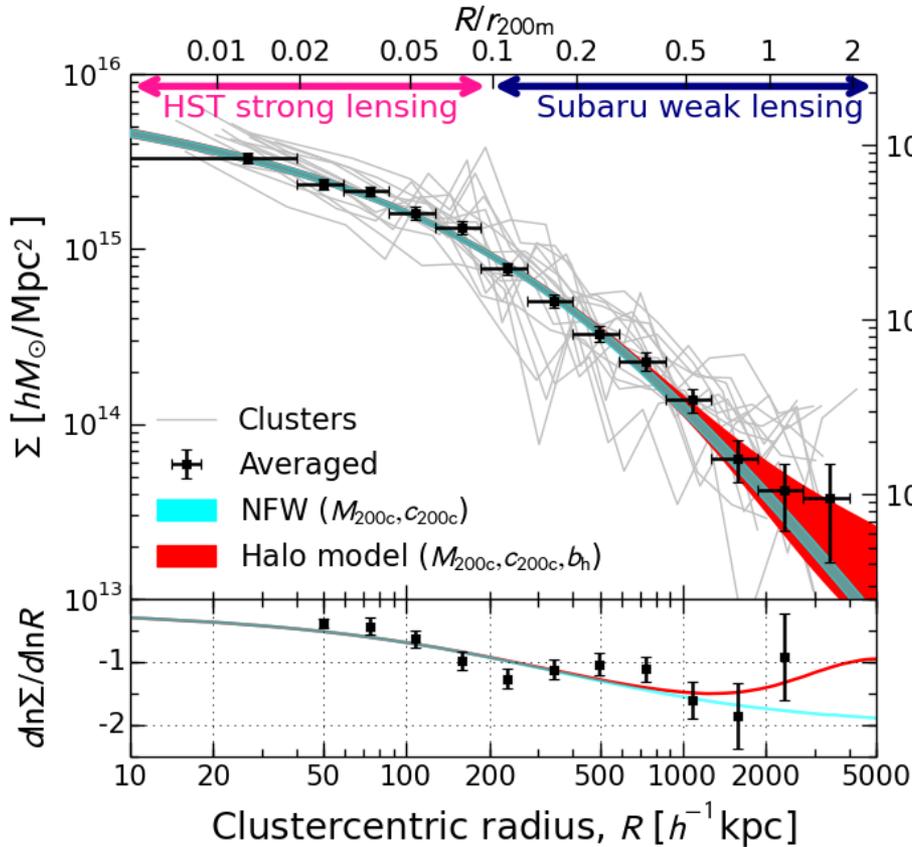


# Splashback radius, $R_{sp}$ : Physical halo boundary

*Outermost caustic of material reaching its first apocentric passage*



# Splashback in CLASH lensing data?



**CLASH X-ray regular subsample**  
prevalently composed of relaxed  
clusters (70%; Meneghetti+14)

$$\langle M_{200\text{m}} \rangle = (1.3 \pm 0.1) \times 10^{15} h^{-1} M_{\text{sun}}$$

$$\langle v_{200\text{m}} \rangle = 4.0 \pm 0.1$$

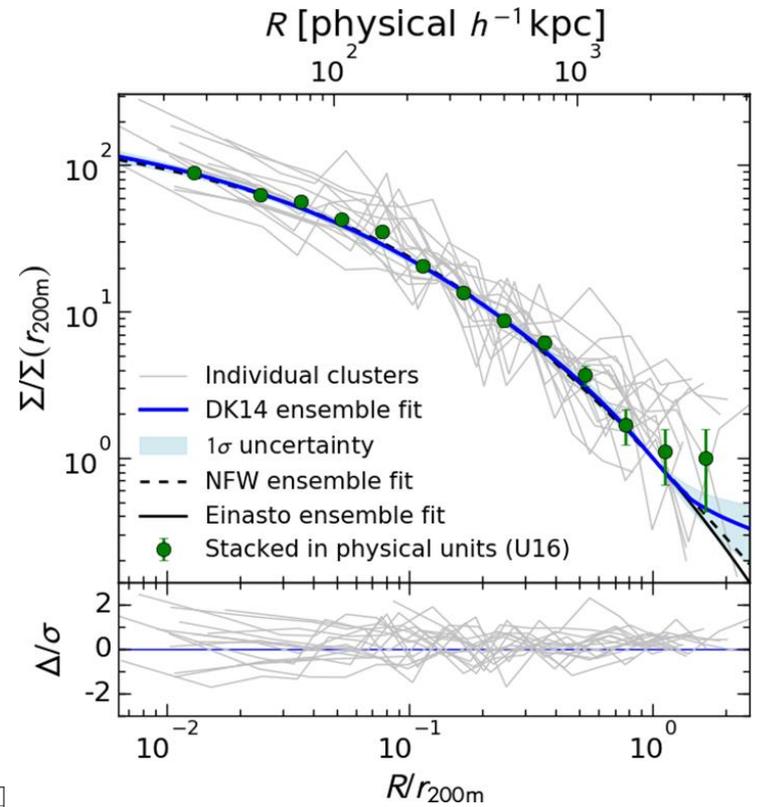
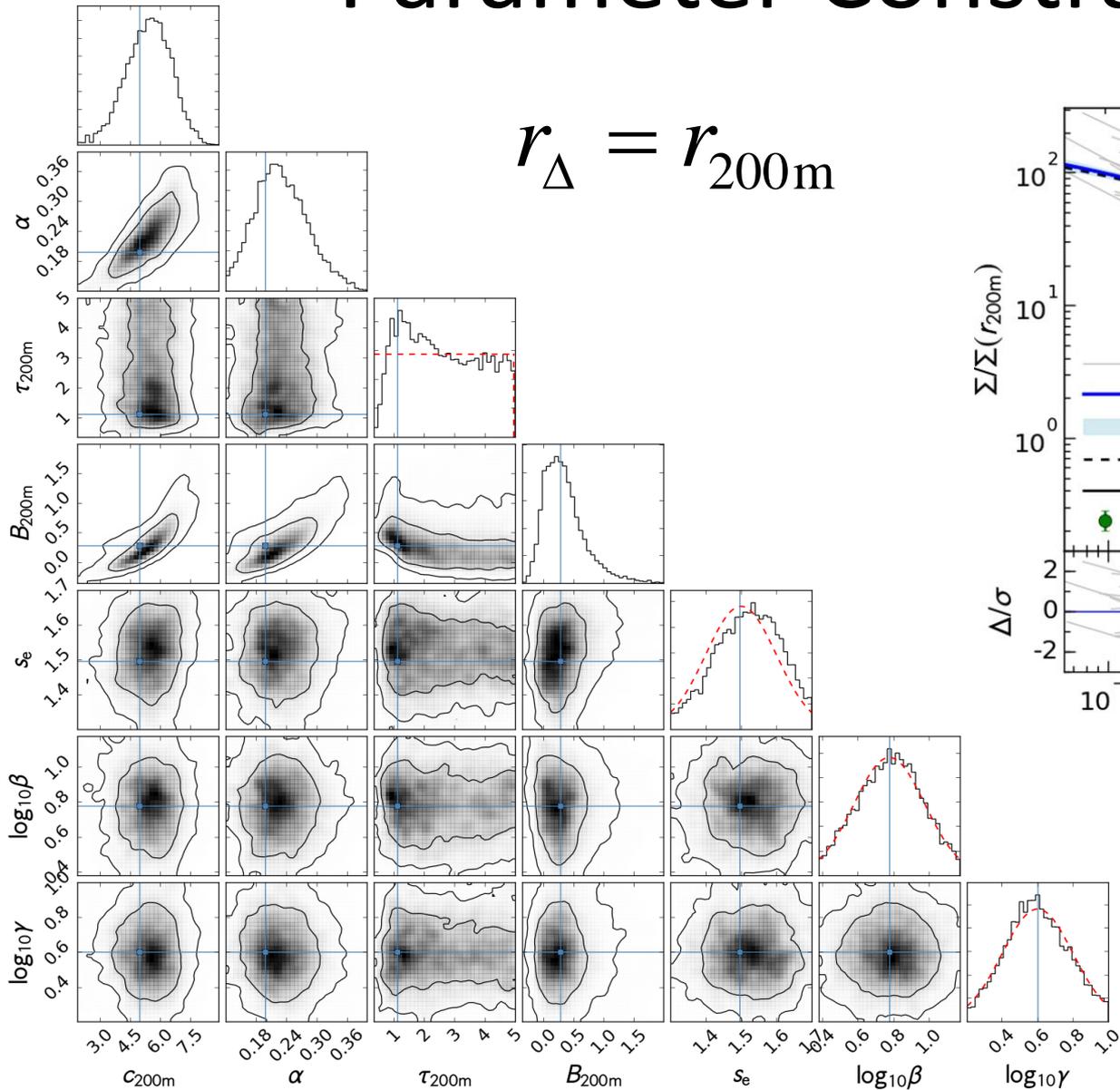
16 clusters with  $\langle z \rangle \cong 0.34$

Umetsu+16, *ApJ*, 821, 116

- CLASH spans a factor of  $\sim 5$  (1.7) in mass (radius), so that sharp gradient feature is washed out when stacked in physical units.
- How to extract  $R_{\text{sp}}$  from coarsely binned ensemble profiles?

# Parameter Constraints

$$r_{\Delta} = r_{200m}$$

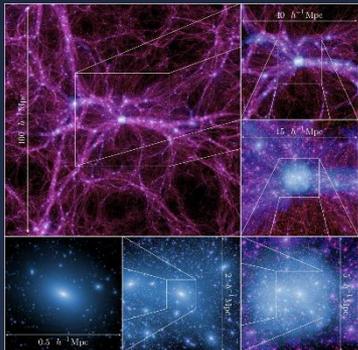




# CLASH: Observational + Theory Efforts



**Wide-field Subaru/Suprime-Cam imaging** (0.4 - 0.9  $\mu\text{m}$ ) plays a unique role in complementing deep *HST* imaging of cluster cores (Umetsu+14, *ApJ*, 795, 163)



**MUSIC-2** (hydro + *N*-body re-simulation) provides an accurate characterization of CLASH sample with testable predictions (Meneghetti+14, *ApJ*, 797, 34)



# **CLASH: Joint Analysis of Strong-lensing, Weak-lensing Shear and Magnification Data for 20 CLASH Galaxy Clusters**

Umetsu, Gruen, Merten, Donahue, & Postman 2016, *ApJ*, 821, 116

See also other CLASH ensemble analysis papers:

- Umetsu et al. 2014, *ApJ*, 795, 163 (Weak lensing shear + magnification)
- Zitrin et al. 2015, *ApJ*, 801, 44 (Strong lensing)
- Merten et al. 2015, *ApJ*, 806, 4 (Strong lensing + weak shear)
- Donahue et al. 2014, *ApJ*, 794, 136 (X-ray *Chandra* & *XMM*)
- Meneghetti et al. 2014, *ApJ*, 797, 34 (theoretical predictions for CLASH)



# Ensemble Calibration of Cluster Masses

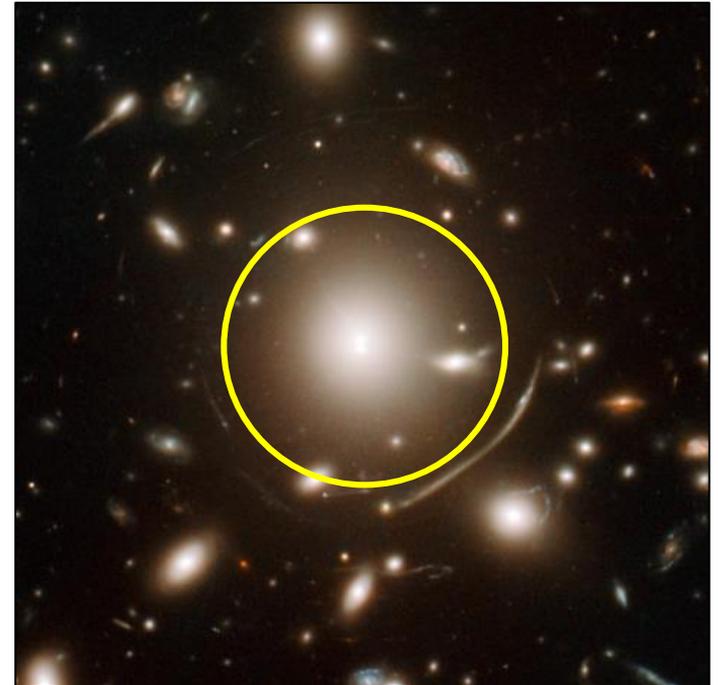
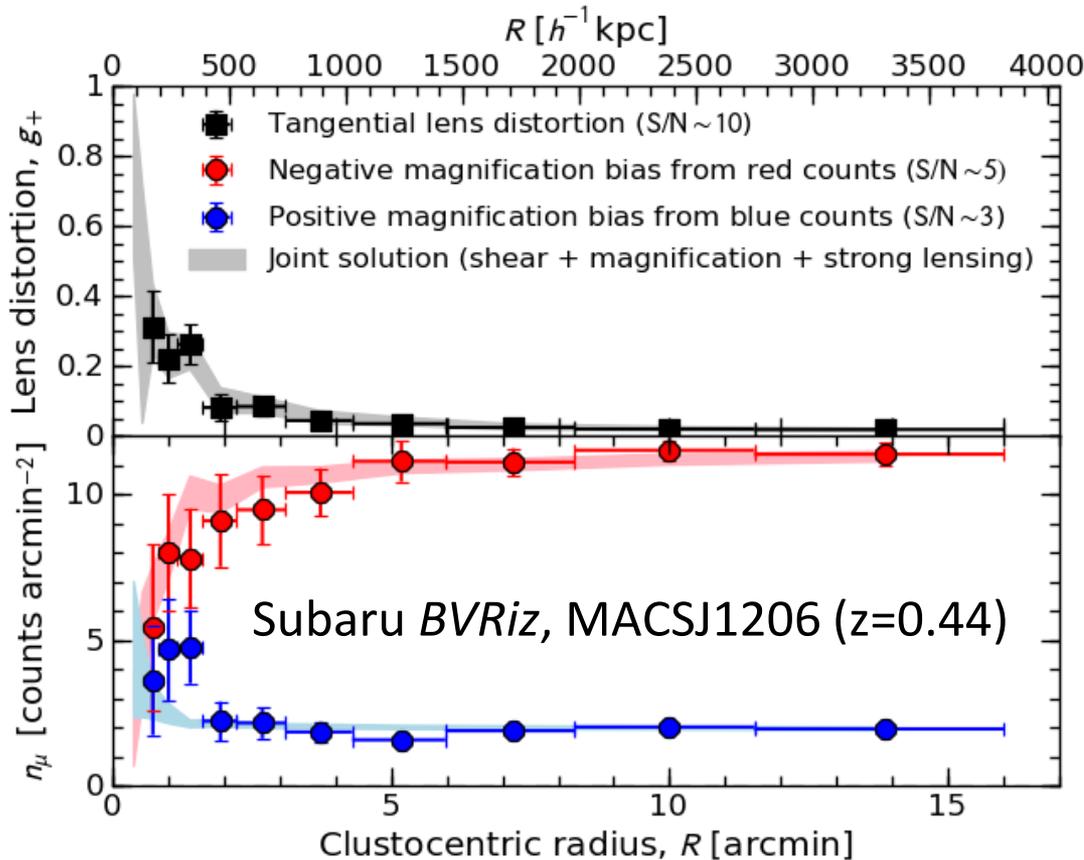
# CLUMI+: Multi-probe Lensing Analysis

Umetsu 2013, *ApJ*, 769, 13

Combining strong-lensing, weak-lensing shear and magnification

$$\{M_{2D,i}\}_{i=1}^{N_{SL}}, \{\langle g_{+,i} \rangle\}_{i=1}^{N_{WL}}, \{\langle n_{\mu,i} \rangle\}_{i=1}^{N_{WL}}.$$

$$P(\Sigma|WL, SL) \propto P(WL, SL|\Sigma)P(\Sigma) = P(n_{\mu}|\Sigma)P(g_{+}|\Sigma)P(M_{2D}|\Sigma)P(\Sigma)$$



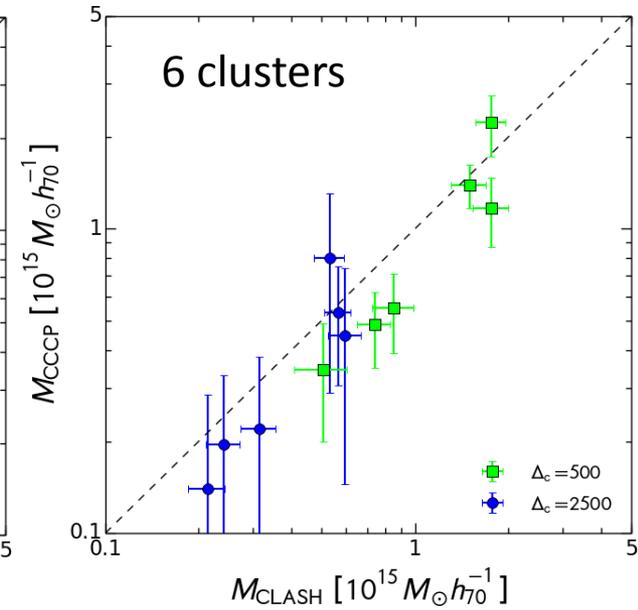
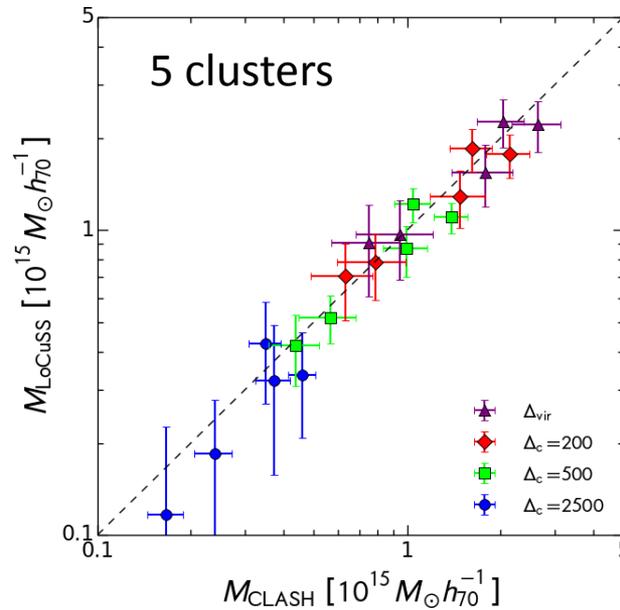
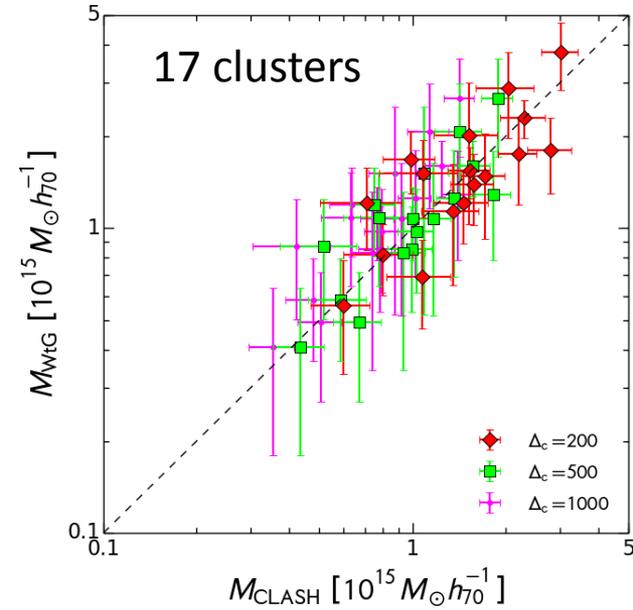


# Results (3): Ensemble Mass Calibration

**WtG** [Subaru/S-Cam]  
(Applegate+14)

**LoCuSS** [Subaru/S-Cam]  
(Okabe & Smith 16)

**CCCP** [CFHT]  
(Hoekstra+15)



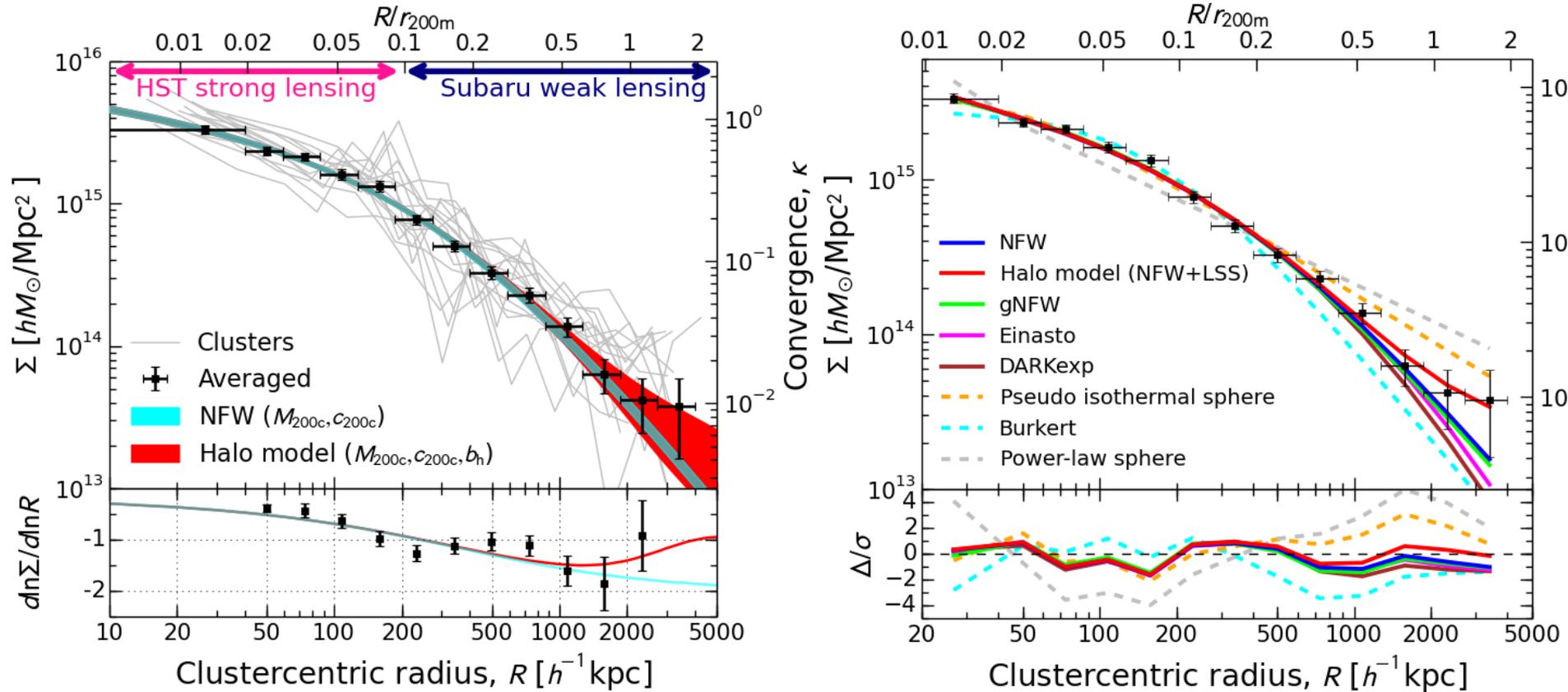
$$\begin{aligned} \langle M_{\text{WtG}} / M_{\text{CLASH}} \rangle &= 1.03 \pm 0.09 \quad (\Delta = 200) \\ &= 1.07 \pm 0.12 \quad (\Delta = 500) \\ &= 1.07 \pm 0.12 \quad (\Delta = 1000) \end{aligned}$$

$$\begin{aligned} \langle M_{\text{LoCuSS}} / M_{\text{CLASH}} \rangle &= 1.00 \pm 0.15 \quad (\Delta = \Delta_{\text{vir}}) \\ &= 0.98 \pm 0.13 \quad (\Delta = 200) \\ &= 0.93 \pm 0.10 \quad (\Delta = 500) \\ &= 0.84 \pm 0.22 \quad (\Delta = 2500) \end{aligned}$$

$$\begin{aligned} \langle M_{\text{CCCP}} / M_{\text{CLASH}} \rangle &= 0.84 \pm 0.10 \quad (\Delta = 500) \\ &= 0.91 \pm 0.24 \quad (\Delta = 2500) \end{aligned}$$



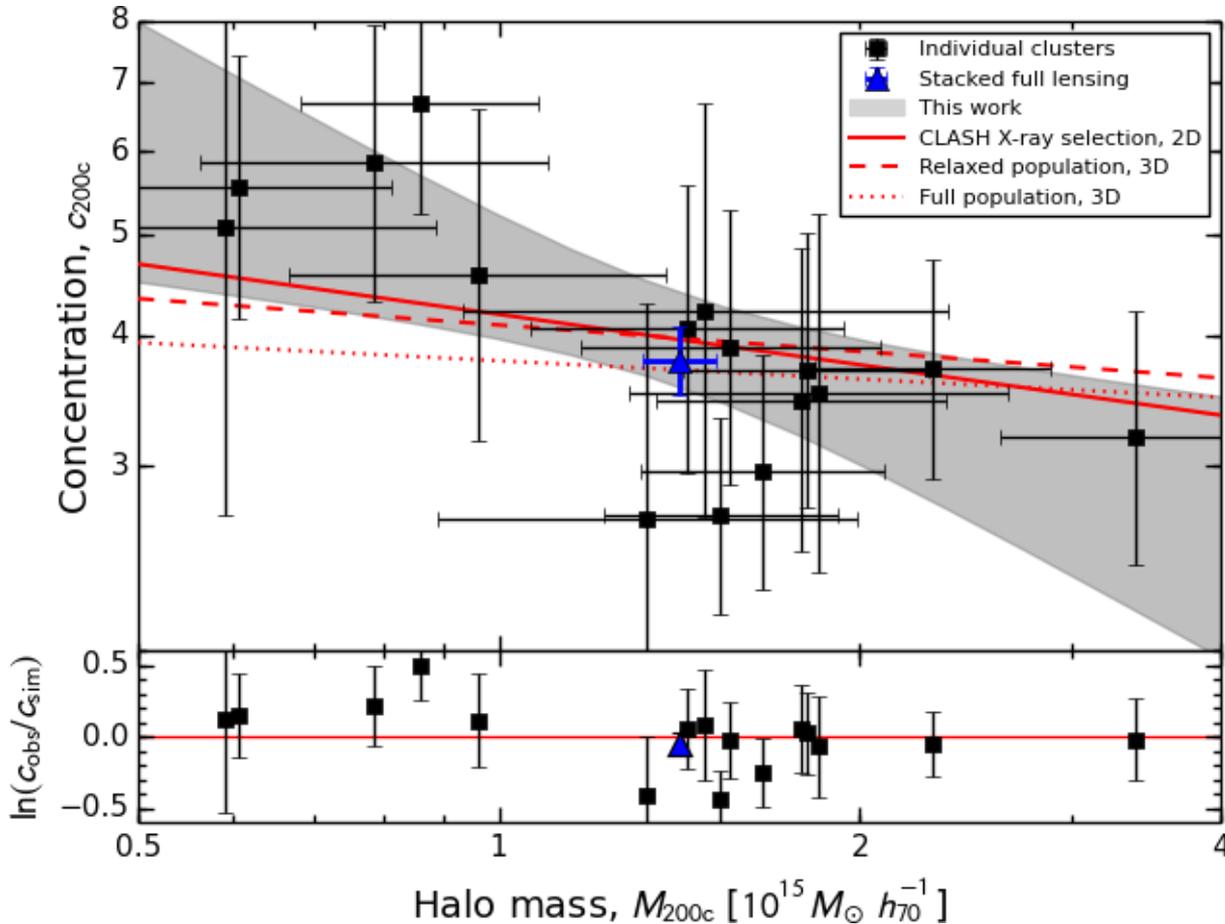
# Results (1): Ensemble Mass Profile



- 33 $\sigma$  detection of ensemble mass profile from  $R \sim 0.01R_{vir}$  to  $2R_{vir}$
- Consistent with cuspy, steepening density profiles (NFW, Einasto, DARKexp)
- Cored (Burkert, pseudo-isothermal) and power-law models are disfavored
- Cuspy models with truncation +  $\Lambda$ CDM 2-halo term ( $b_h \sim 9.3$ ) give improved fits



# Results (2): Concentration—Mass Relation



**Predicted for CLASH  
(Meneghetti+14):**

$$\langle c_{200c} \rangle = 3.9,$$

$$3 \leq c_{200c} \leq 6,$$

$$\text{slope} = -0.16$$

$$\sigma(\ln c_{200c}) = 0.16$$

**Observed (this work):**

$$c_{200c} |_{z=0.34} = 3.95 \pm 0.35$$

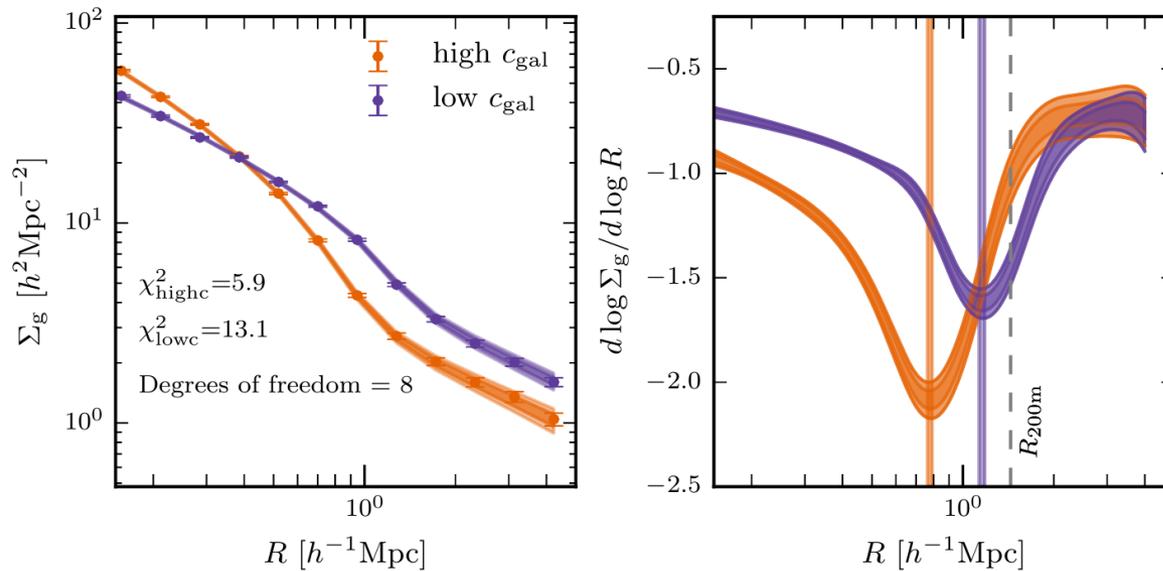
$$\text{at } M_{200c} = 10^{15} M_{\text{sun}} / h,$$

$$\text{slope} = -0.44 \pm 0.19$$

$$\sigma(\ln c_{200c}) = 0.13 \pm 0.06$$

Normalization, slope, & scatter are all consistent with  $\Lambda$ CDM (WMAP7 and later) within errors when the CLASH selection function based on X-ray morphological regularity and projection effects are taken into account.

# Splashback in surface number density of SDSS cluster galaxies (S. More+16)

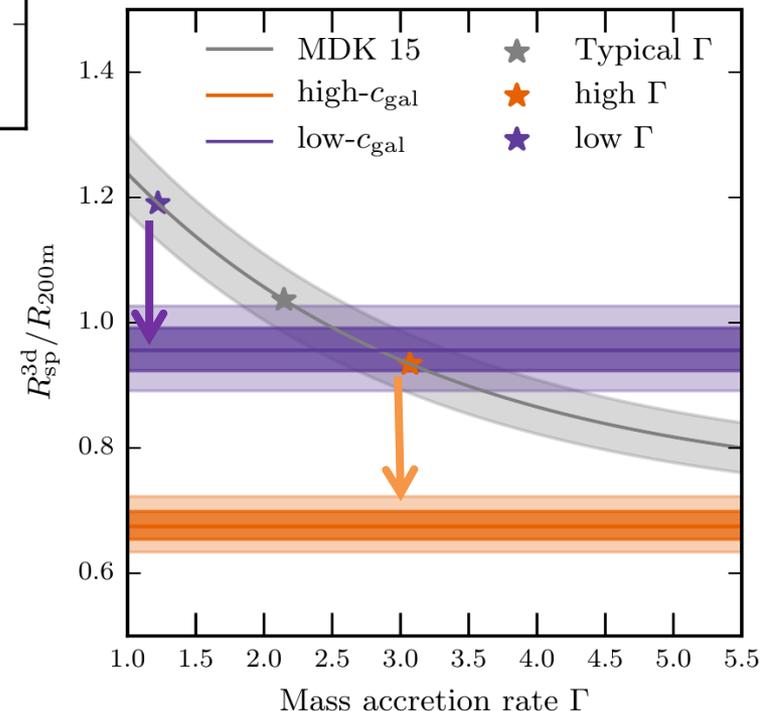


$$\langle M_{200m} \rangle \cong 0.19 \times 10^{15} h^{-1} M_{\text{sun}}$$

$$\langle v_{200m} \rangle \cong 2.4$$

$$\langle z \rangle \cong 0.24$$

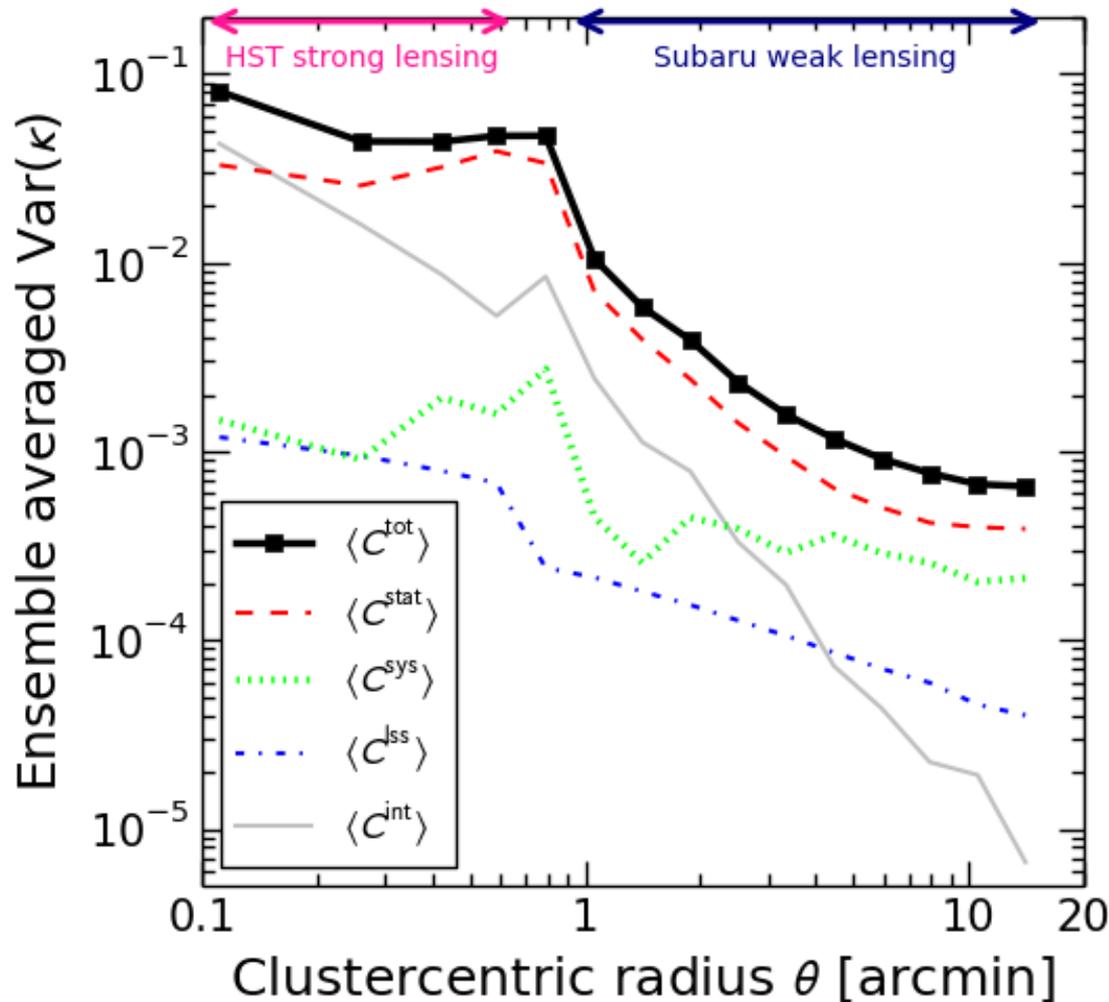
- Splashback feature clearly detected using “galaxies”, instead of “mass”, in both cluster subsamples.
- But the observed  $R_{\text{sp}}(\text{gal})/R_{200m}(\text{WL})$  values are *significantly smaller* than predicted!





# Ensemble-averaged Error Budget

Diagonal elements ( $C_{ii}$ ) averaged over all CLASH clusters



Residual mass-sheet uncertainty

$$\langle C_{\text{sys}} \rangle_{ii} \sim \text{const.} \sim (0.02)^2$$

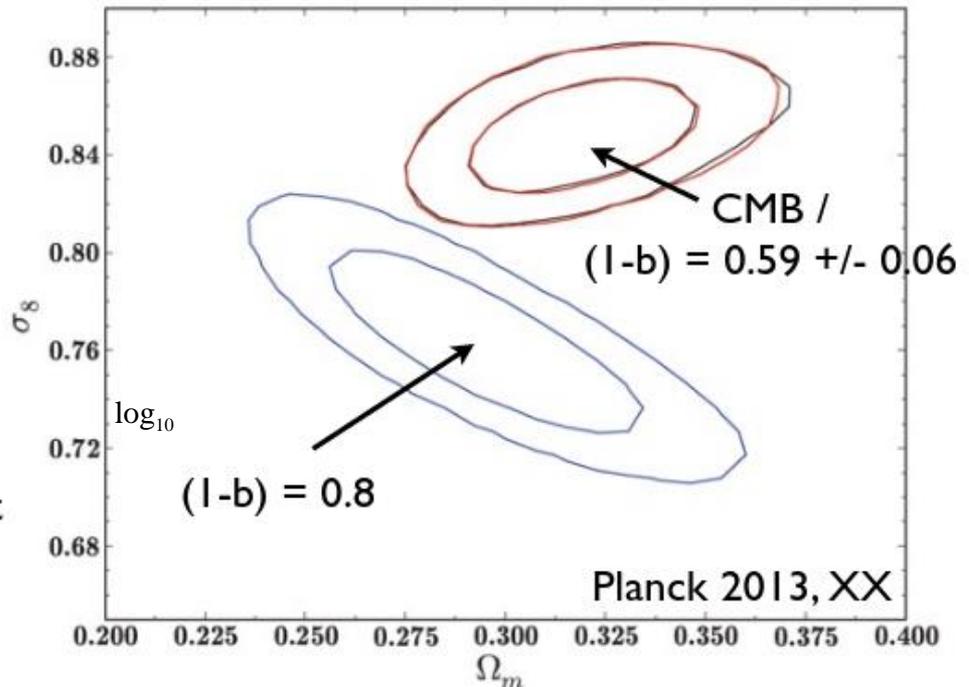
Intrinsic profile variations due to triaxiality, substructure, and  $c$ - $M$  scatter (Gruen+15)

$$\langle C_{\text{int}} \rangle_{ii} \approx (0.2)^2 K_i^2$$

# Planck13 CMB vs. Cluster Cosmology

$b=0.2?? - 0.4??$

- Planck:  $3\sigma$  tension between SZ cluster counts and CMB cosmology
- assumes  $M_{\text{Planck}} / M_{\text{true}} = (1-b) = 0.8$
- calibrated with XMM hydrostatic masses (Arnaud et al. 2010) + simulations



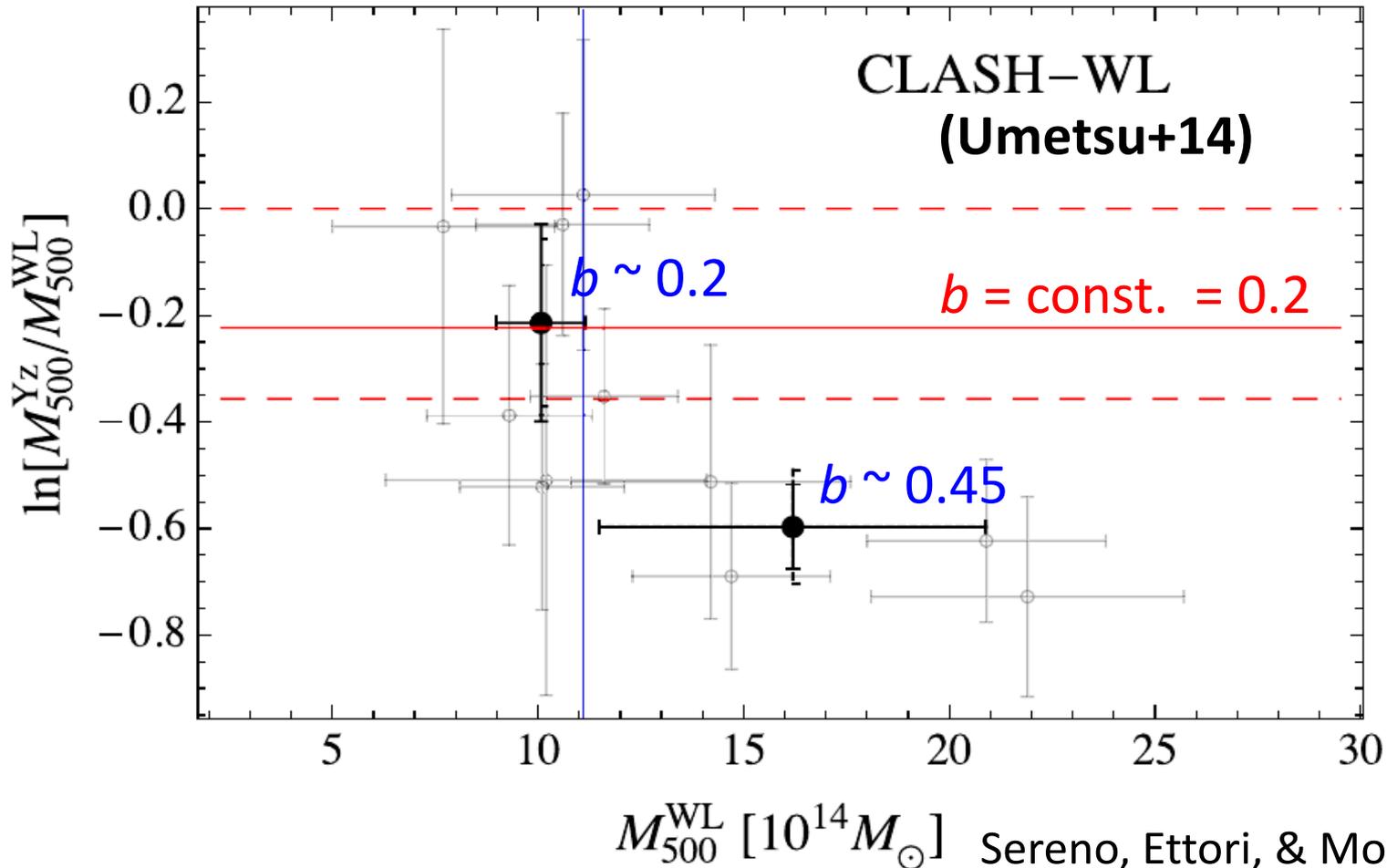
suggested explanations:

- **mass bias underestimated** (and no accounting for uncertainties)
- $2.9\sigma$  detection of neutrino masses:  $\Sigma m_\nu = (0.58 \pm 0.20) \text{ eV}$   
(Planck+WMAPpol+ACT+BAO:  $\Sigma m_\nu < 0.23 \text{ eV}$ , 95% CL)



# Comparison with *Planck* Masses – Not so simple

Mass-dependent bias (20-45%) observed for *Planck*-SZE mass estimates

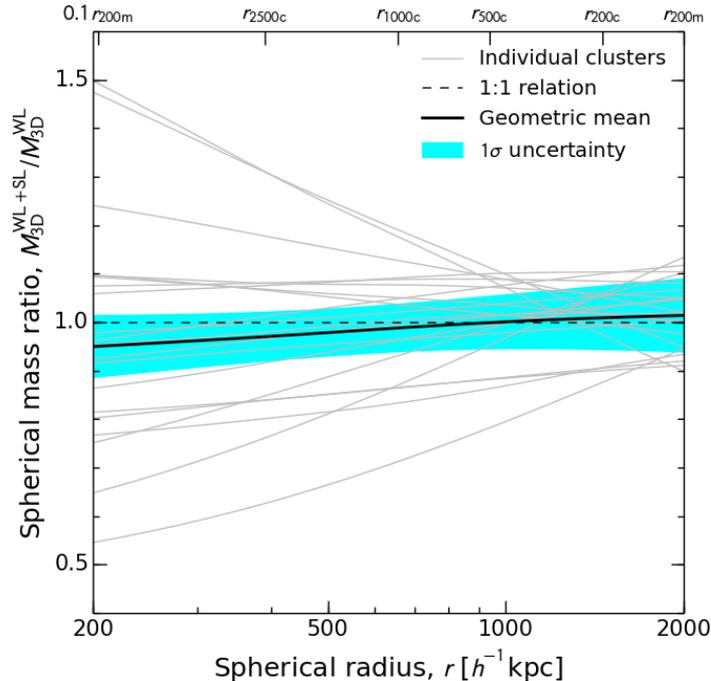


Sereno, Ettori, & Moscardini 15,  
CoMaLit II (arXiv:1407.7869)



# CLASH Lensing: Internal Consistency

$M_{3D}(<r)$  for  $N=20$  clusters de-projected assuming spherical NFW model



**WL-only (U14) and WL+SL (U16)  
are consistent within 5% at  $r =$   
[200, 2000] kpc/h**

Umetsu+16, *ApJ*, 821, 116

## CLASH ensemble mass calibration uncertainty

- Statistical uncertainty with  $N=20$ :  $28\%/\sqrt{20} = 6.3\%$
- Systematic uncertainty: 5.6% [5% shear calibration, 2% dilution]
- Mass modeling bias (dev from NFW, orientation bias): 3%
- Total calibration uncertainty: 9%

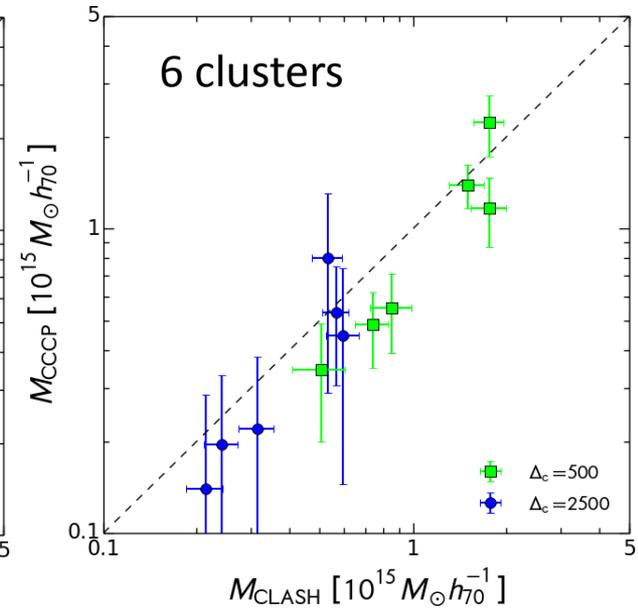
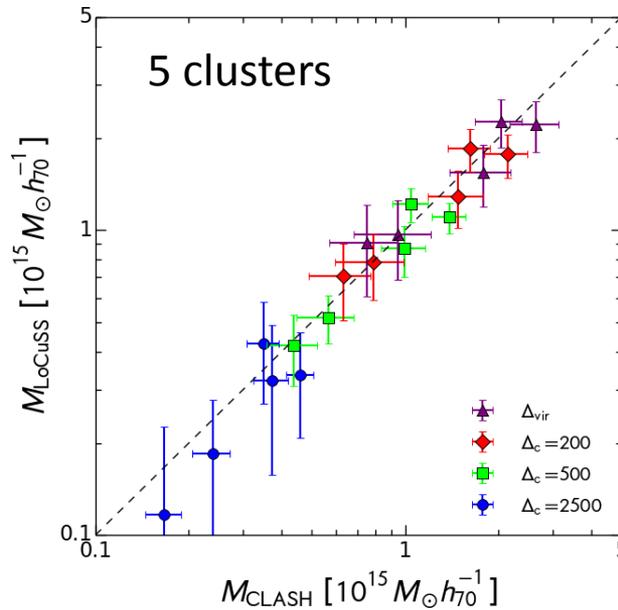
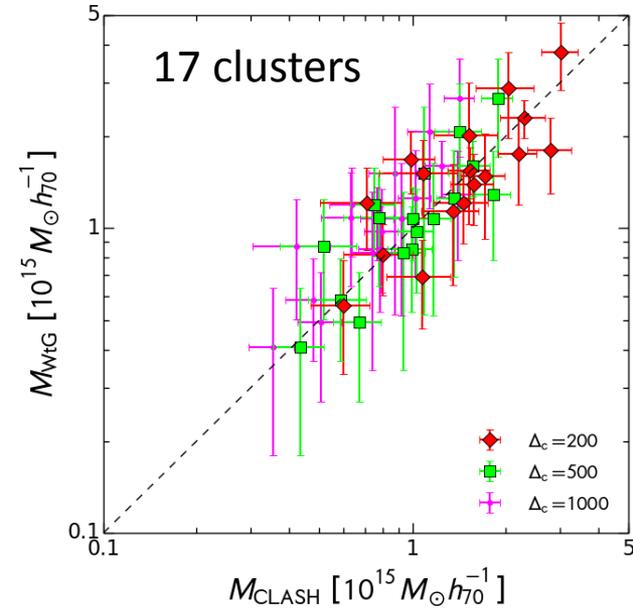


# Comparisons with Other WL Surveys

**WtG [Subaru]**  
(Applegate+14)

**LoCuSS [Subaru]**  
(Okabe & Smith 15)

**CCCP [CFHT]**  
(Hoekstra+15)



$$\begin{aligned} \langle M_{\text{WtG}} / M_{\text{CLASH}} \rangle &= 1.03 \pm 0.09 \quad (\Delta = 200) \\ &= 1.07 \pm 1.12 \quad (\Delta = 500) \\ &= 1.07 \pm 1.12 \quad (\Delta = 1000) \end{aligned}$$

$$\begin{aligned} \langle M_{\text{LoCuSS}} / M_{\text{CLASH}} \rangle &= 1.00 \pm 0.15 \quad (\Delta = \Delta_{\text{vir}}) \\ &= 0.98 \pm 0.13 \quad (\Delta = 200) \\ &= 0.93 \pm 0.10 \quad (\Delta = 500) \\ &= 0.84 \pm 0.22 \quad (\Delta = 2500) \end{aligned}$$

$$\begin{aligned} \langle M_{\text{CCCP}} / M_{\text{CLASH}} \rangle &= 0.84 \pm 0.10 \quad (\Delta = 500) \\ &= 0.91 \pm 0.24 \quad (\Delta = 2500) \end{aligned}$$

Umetsu+16, *ApJ*,  
821, 116



# Comparison of Best-fit Models

Acceptable fits:  $p$  values (PTE)  $> 0.05$

**Table 4**  
Best-fit models for the stacked mass profile of the CLASH X-ray-selected subsample

Model	$M_{200c}$ ( $10^{14} M_{\odot} h_{70}^{-1}$ )	$c_{200c}$	Shape/structural parameters	$b_h$	$\chi^2/\text{dof}$	PTE <sup>a</sup>	Notes
NFW	$14.4^{+1.1}_{-1.0}$	$3.76^{+0.29}_{-0.27}$	$\gamma_c = 1$	—	11.3/11	0.419	No truncation
gNFW	$14.1^{+1.1}_{-1.1}$	$4.04^{+0.53}_{-0.52}$	$\gamma_c = 0.85^{+0.22}_{-0.31}$	—	10.9/10	0.366	No truncation
Einasto	$14.7^{+1.1}_{-1.1}$	$3.53^{+0.36}_{-0.39}$	$\alpha_E = 0.232^{+0.042}_{-0.038}$	—	11.7/10	0.306	No truncation
DARKexp- $\gamma^b$	$14.5^{+1.2}_{-1.1}$	$3.53^{+0.42}_{-0.42}$	$\phi_0 = 3.90^{+0.41}_{-0.45}$	—	13.5/10	0.198	No truncation
Pseudo isothermal	—	—	$V_c = 1762^{+40}_{-39}$ km/s, $r_c = 69^{+7}_{-7}$ kpc	—	23.6/11	0.015	No truncation
Burkert	$11.6^{+0.8}_{-0.8}$	—	$r_{200c}/r_0 = 8.81^{+0.42}_{-0.41}$	—	29.9/11	0.002	No truncation
Power-law sphere	$12.5^{+0.8}_{-0.8}$	—	$\gamma_c = 1.78^{+0.02}_{-0.02}$	—	93.5/11	0.000	No truncation
Halo model <sup>c</sup> :							
NFW+LSS (i)	$14.1^{+1.0}_{-1.0}$	$3.79^{+0.30}_{-0.28}$	$\gamma_c = 1$	9.3	10.9/11	0.450	$\Lambda$ CDM $b_h(M)$ scaling
NFW+LSS (ii)	$14.4^{+1.4}_{-1.3}$	$3.74^{+0.33}_{-0.30}$	$\gamma_c = 1$	$7.4^{+4.6}_{-4.7}$	10.8/10	0.377	$b_h$ as a free parameter
Einasto+LSS (i)	$14.3^{+1.1}_{-1.1}$	$3.69^{+0.36}_{-0.42}$	$\alpha_E = 0.248^{+0.051}_{-0.047}$	9.3	10.7/10	0.385	$\Lambda$ CDM $b_h(M)$ scaling
Einasto+LSS (ii)	$14.5^{+1.9}_{-1.6}$	$3.65^{+0.47}_{-0.61}$	$\alpha_E = 0.245^{+0.061}_{-0.053}$	$8.7^{+5.3}_{-5.6}$	10.6/9	0.301	$b_h$ as a free parameter
DARKexp+LSS (i)	$14.2^{+1.2}_{-1.1}$	$3.64^{+0.44}_{-0.46}$	$\phi_0 = 3.89^{+0.51}_{-0.54}$	9.3	11.7/10	0.308	$\Lambda$ CDM $b_h(M)$ scaling
DARKexp+LSS (ii)	$14.0^{+1.8}_{-1.6}$	$3.69^{+0.53}_{-0.57}$	$\phi_0 = 3.85^{+0.57}_{-0.61}$	$10.1^{+4.9}_{-5.1}$	11.6/9	0.235	$b_h$ as a free parameter

<sup>a</sup> Probability to exceed the observed  $\chi^2$  value.

<sup>b</sup> We use Dehnen–Tremaine  $\gamma$ -models with the central cusp slope  $\gamma_c = 3 \log_{10} \phi_0 - 0.65$  ( $1.7 \leq \phi_0 \leq 6$ ) as an analytic fitting function for the DARKexp density profile.

<sup>c</sup> For halo model predictions, we decompose the total mass overdensity  $\Delta\rho(r) = \rho(r) - \bar{\rho}_m$  as  $\Delta\rho = f_t \rho_h + \rho_{2h}$  where  $\rho_h(r)$  is the halo density profile,  $\rho_{2h}(r) = \bar{\rho}_m b_h \xi_m^L(r)$  is the two-halo term, and  $f_t(r) = (1 + r^2/r_t^2)^{-2}$  describes the steepening of the density profile in the transition regime around the truncation radius  $r_t$ , which is assumed to be  $r_t = 3r_{200c}$ .

Umetsu+16, arXiv:1507.04385

- Consistent with cuspy density profiles (NFW, Einasto, DARKexp)
- Cuspy models that include  $\Lambda$ CDM 2-halo term ( $b_h \sim 9.3$ ) give improved fits



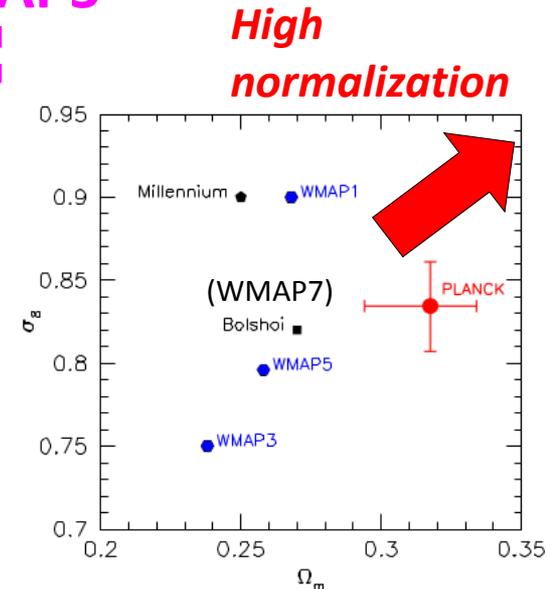
# Comparison with LCDM $c(M)$ models

Umetsu+16,  
arXiv:1507.04385

**Table 5**  
Comparison of measured and predicted concentrations for the CLASH X-ray-selected subsample

Author	Sample	3D/2D	Function <sup>a</sup>	$c^{(obs)}/c^{(pred)}$ Average <sup>c</sup>	$\sigma^d$	$\chi^2$	PTE <sup>b</sup>
<b>Theory:</b>							
Duffy et al. (2008)	full	3D	$c-M$	$1.331 \pm 0.108$	0.334	22.6	0.046
Duffy et al. (2008)	relaxed	3D	$c-M$	$1.165 \pm 0.094$	0.290	13.6	0.399
Prada et al. (2012)	full	3D	$c-\nu$	$0.733 \pm 0.065$	0.244	24.6	0.026
Bhattacharya et al. (2013)	full	3D	$c-\nu$	$1.169 \pm 0.095$	0.292	14.1	0.369
Bhattacharya et al. (2013)	relaxed	3D	$c-\nu$	$1.131 \pm 0.092$	0.277	12.4	0.494
Dutton & Macciò (2014)	full	3D	$c-M$	$1.061 \pm 0.086$	0.262	10.4	0.659
Meneghetti et al. (2014)	full	3D	$c-M$	$1.061 \pm 0.089$	0.279	10.2	0.675
Meneghetti et al. (2014)	relaxed	3D	$c-M$	$0.990 \pm 0.083$	0.249	9.2	0.760
Diemer & Kravtsov (2015)	full (median)	3D	$c-\nu$	$1.021 \pm 0.083$	0.330	14.4	0.349
Diemer & Kravtsov (2015)	full (mean)	3D	$c-\nu$	$1.060 \pm 0.086$	0.326	13.8	0.391
Meneghetti et al. (2014)	full	2D	$c-M$	$1.087 \pm 0.092$	0.336	13.5	0.413
Meneghetti et al. (2014)	relaxed	2D	$c-M$	$1.040 \pm 0.086$	0.283	10.8	0.628
Meneghetti et al. (2014)	CLASH	2D	$c-M$	$0.988 \pm 0.078$	0.227	9.6	0.730
<b>Observations:</b>							
Merten et al. (2015)	CLASH	2D	$c-M$	$1.133 \pm 0.087$	0.209	9.2	0.754

WMAP5



<sup>a</sup>  $c-M$ : power-law  $c(M, z)$  relation;  $c-\nu$ : halo concentration given as a function of peak height  $\nu(M, z)$ .

<sup>b</sup> Probability to exceed the measured  $\chi^2$  value assuming the standard  $\chi^2$  probability distribution function.

<sup>c</sup> Weighted geometric average of observed-to-predicted concentration ratios.

<sup>d</sup> Standard deviation of the distribution of observed-to-predicted concentration ratios.

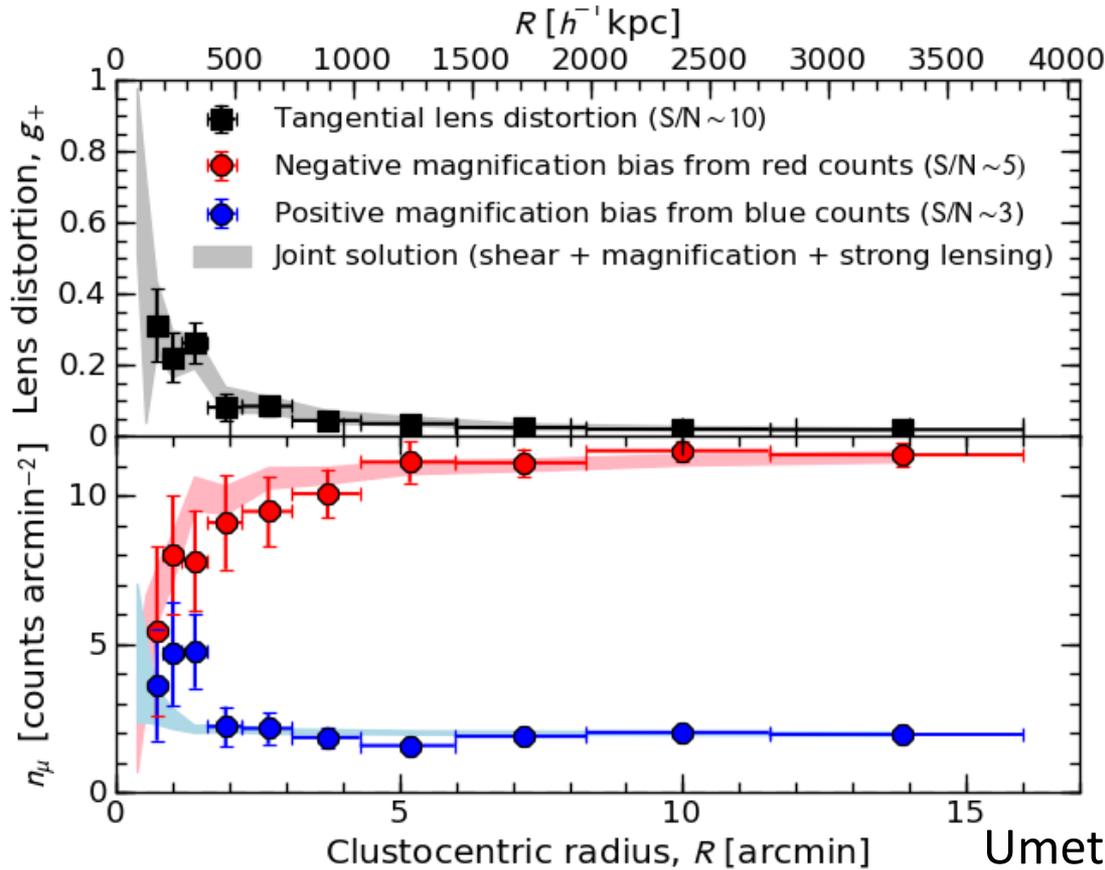
- Consistent with models that are calibrated for more recent cosmologies (WMAP7 and later)
- Better agreement is achieved when selection effects (overall degree of relaxation) are taken into account

# Multi-probe Lensing Approach

## Combining azimuthally-averaged strong and weak lensing observables

$$\{M_{2D,i}\}_{i=1}^{N_{SL}}, \{\langle g_{+,i} \rangle\}_{i=1}^{N_{WL}}, \{\langle n_{\mu,i} \rangle\}_{i=1}^{N_{WL}} \quad M_{2D}(< R) = \int_{|\mathbf{R}'| < R} \Sigma(\mathbf{R}') d^2 R'$$

$$P(\boldsymbol{\kappa} | \text{WL,SL}) \propto P(\text{WL,SL} | \boldsymbol{\kappa}) P(\boldsymbol{\kappa}) = P(\mathbf{g}_+ | \boldsymbol{\kappa}) P(\mathbf{n}_\mu | \boldsymbol{\kappa}) P(\mathbf{M}_{2D} | \boldsymbol{\kappa}) P(\boldsymbol{\kappa})$$



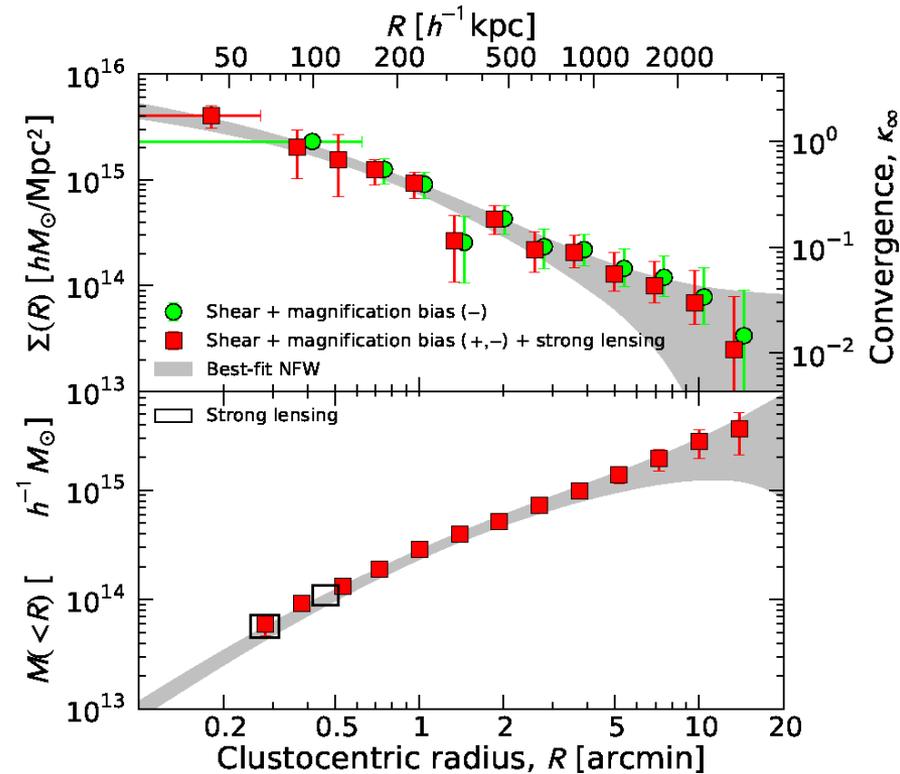
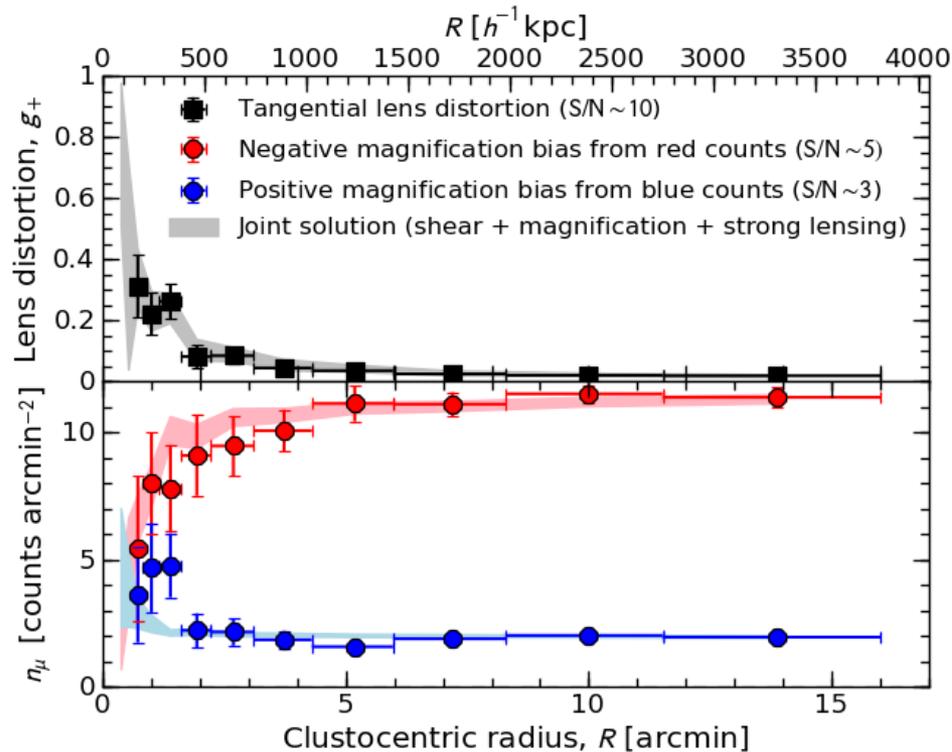
# Multi-probe Lensing Approach

Combining azimuthally-averaged strong and weak lensing observables

$$\{M_{2D,i}\}_{i=1}^{N_{SL}}, \{\langle g_{+,i} \rangle\}_{i=1}^{N_{WL}}, \{\langle n_{\mu,i} \rangle\}_{i=1}^{N_{WL}}.$$

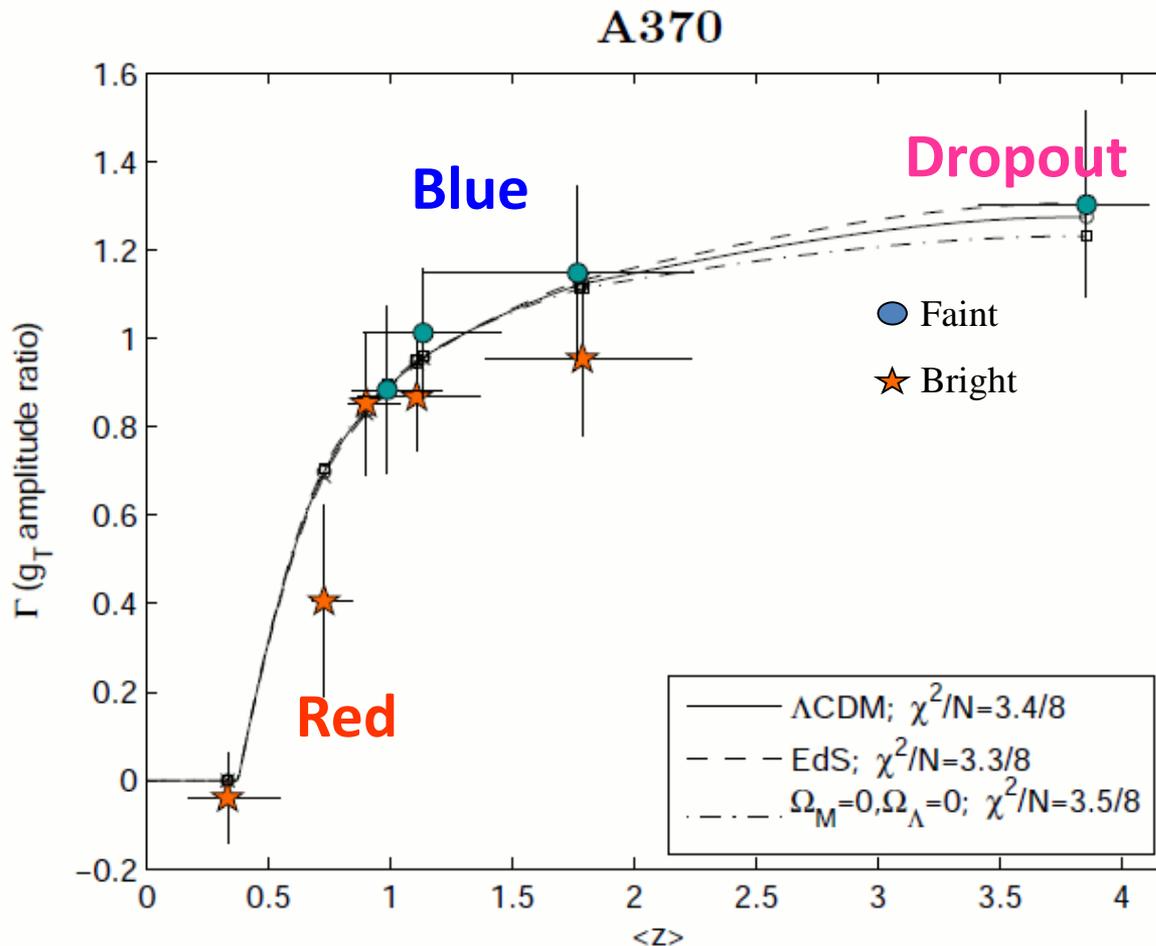
$$M_{2D}(< R) = \int_{|\mathbf{R}'| < R} \Sigma(\mathbf{R}') d^2 R'$$

$$P(\boldsymbol{\kappa} | \text{WL,SL}) \propto P(\text{WL,SL} | \boldsymbol{\kappa}) P(\boldsymbol{\kappa}) = P(\mathbf{g}_+ | \boldsymbol{\kappa}) P(\mathbf{n}_\mu | \boldsymbol{\kappa}) P(M_{2D} | \boldsymbol{\kappa}) P(\boldsymbol{\kappa})$$



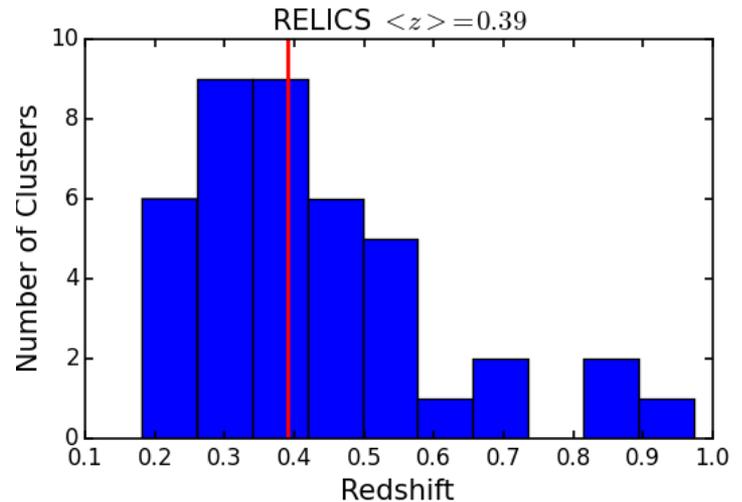
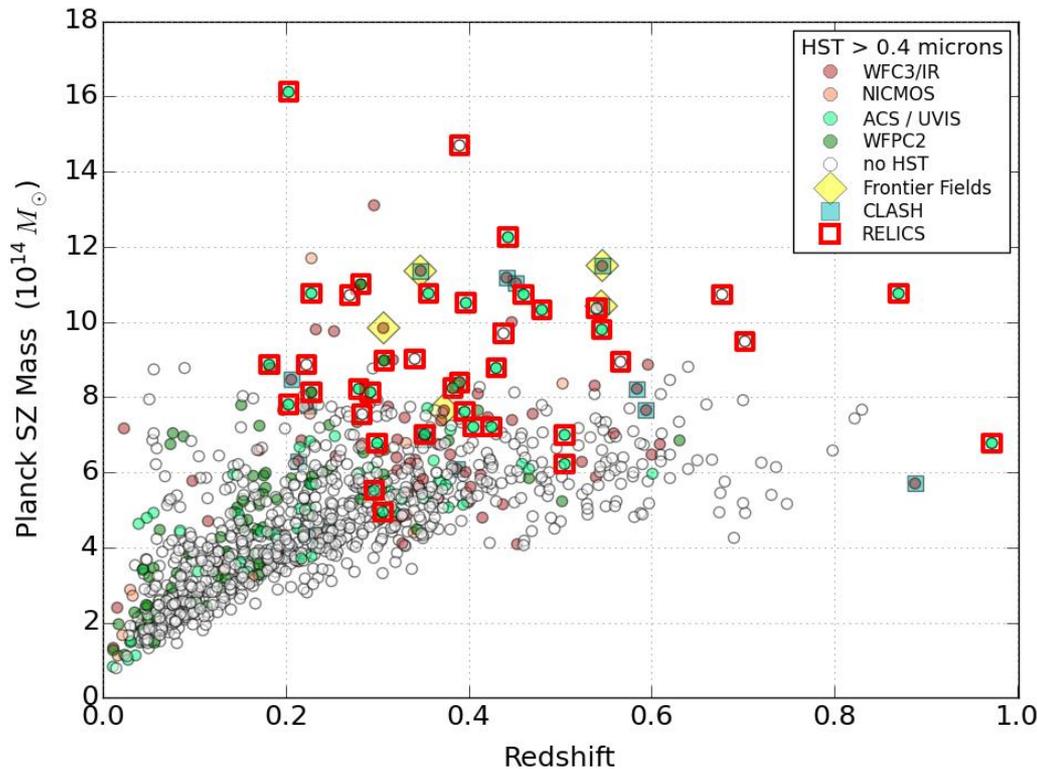
# Shear strength as function of $z$ (KSB+)

First detection of WL distance vs. redshift relation!!!



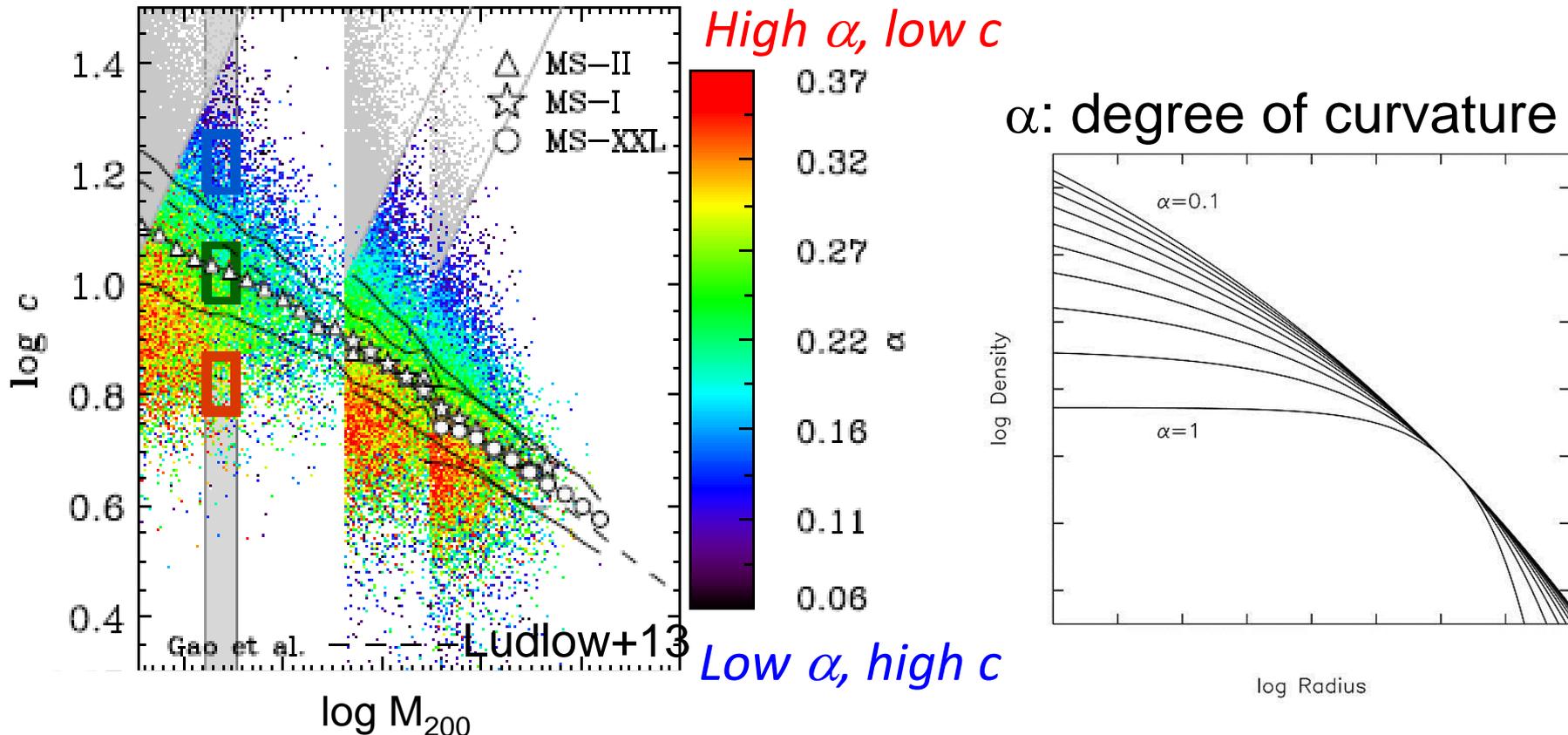
# Reionization Lensing Cluster Survey (RELICS)

Newly approved 190-orbit *HST* survey (7 ACS/WFC3 filters) of 41 high-mass clusters primarily selected from the *Planck* survey (P.I. Dan Coe; Oct 2015 – Apr 2017)



<http://hstrelics.weebly.com>

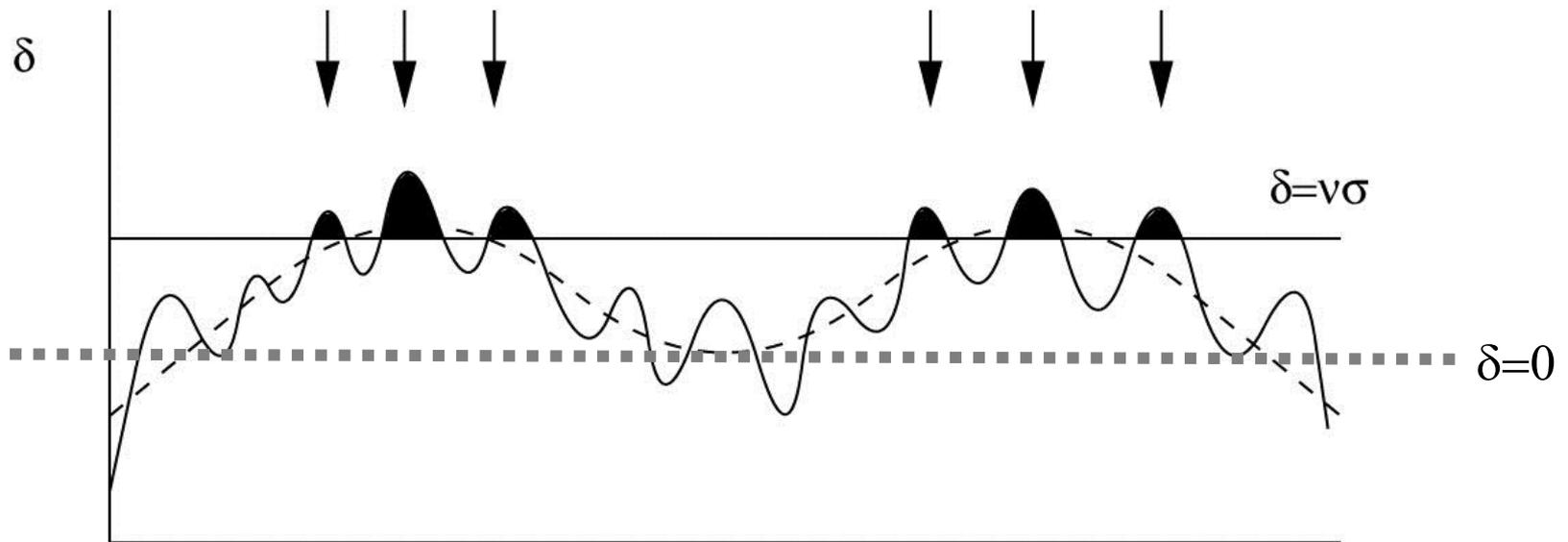
# Intrinsic Scatter in $c(M)$ : Mass Assembly Histories (MAH)



- Scatter is due to another DoF ( $\alpha$ ), related to MAH (Ludlow+13)
- Larger values of  $\alpha$  correspond to halos that have been assembled more rapidly than the NFW curve
- Halos with average  $c_{200}$  have the NFW-equivalent  $\alpha \sim 0.18$

# Key Predictions of nonlinear structure formation models

## (3) Halo bias: surrounding large-scale structure



$$\delta(\mathbf{x}) := \frac{\rho - \bar{\rho}}{\bar{\rho}} = \int \frac{d^3k}{(2\pi)^3} \tilde{\delta}(\mathbf{k}) e^{i\mathbf{k}\cdot\mathbf{x}} \quad \mathbf{x}$$

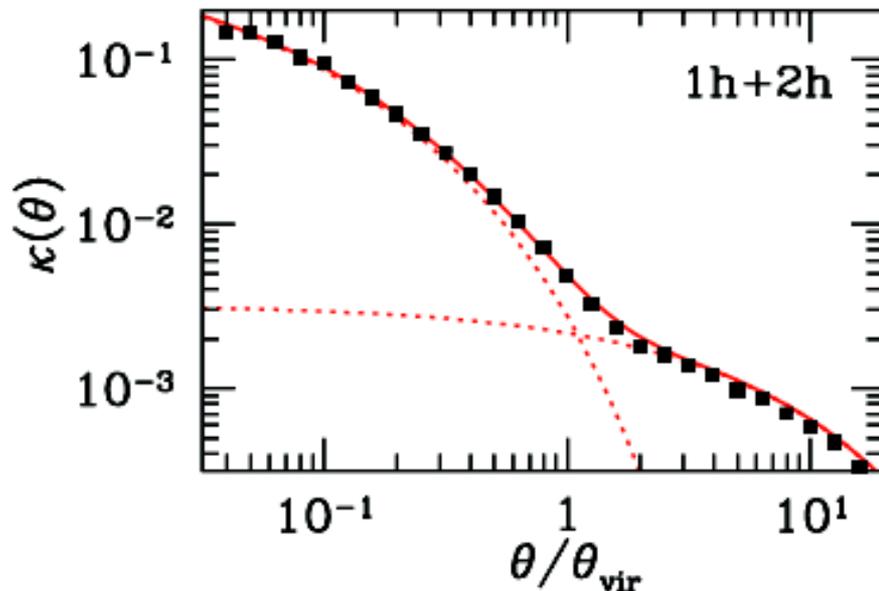
$$\langle \tilde{\delta}(\mathbf{k}) \tilde{\delta}(\mathbf{k}') \rangle = (2\pi)^3 \delta_D^3(\mathbf{k} + \mathbf{k}') P(k)$$

# Shear doesn't see mass sheet

Averaged lensing profiles in/around LCDM halos (Oguri & Hamana 11)

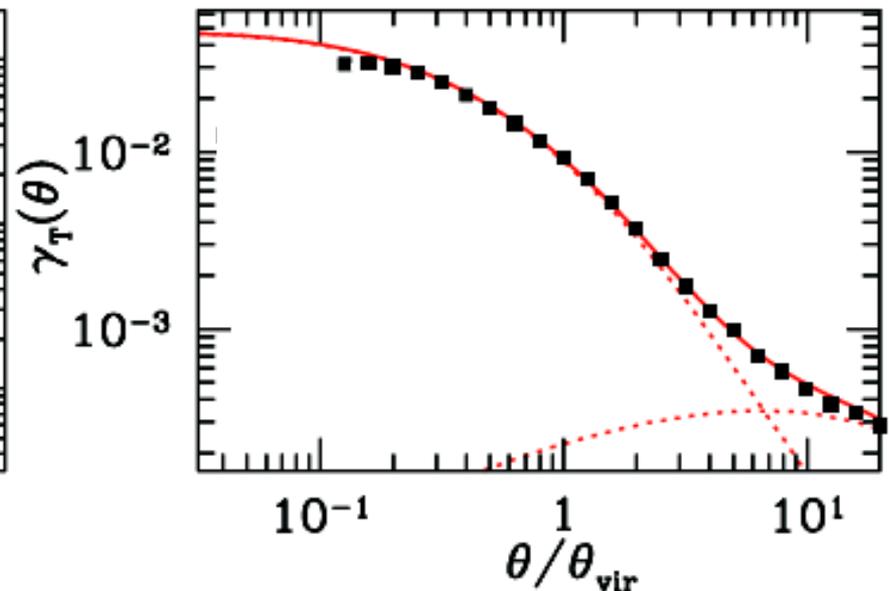
Total

$$\kappa = \Sigma(R) / \Sigma_c$$



Modulated

$$\gamma_+ = \Delta\Sigma(R) / \Sigma_c$$

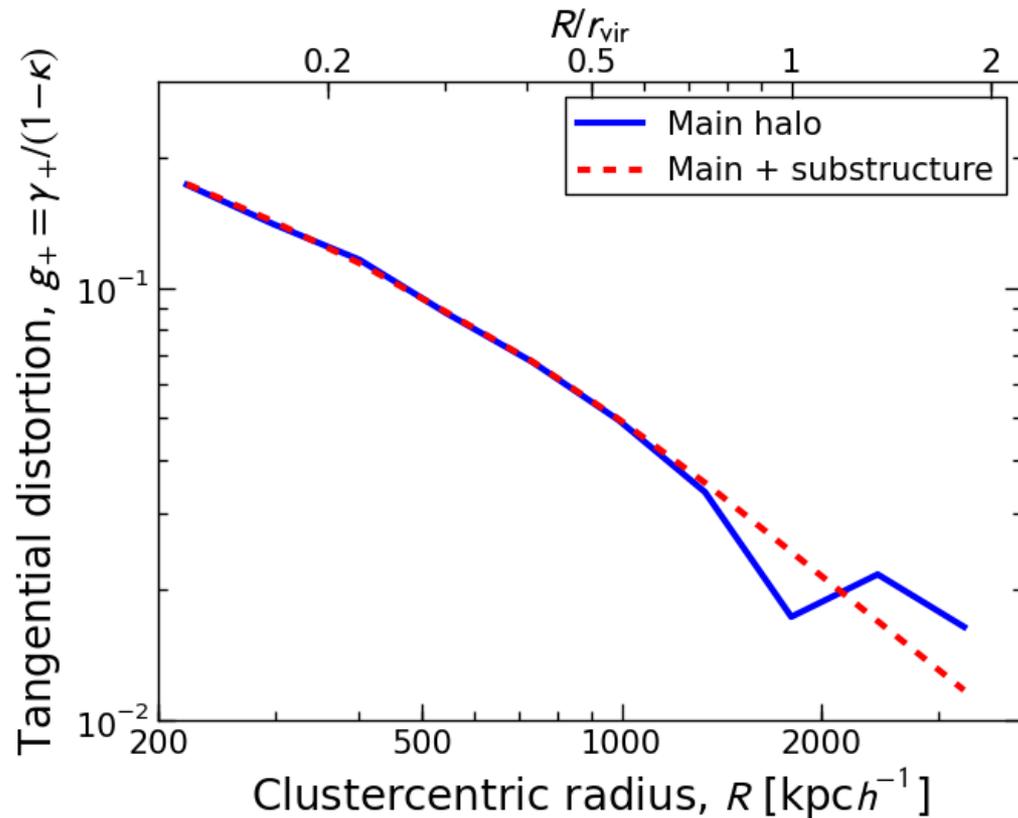
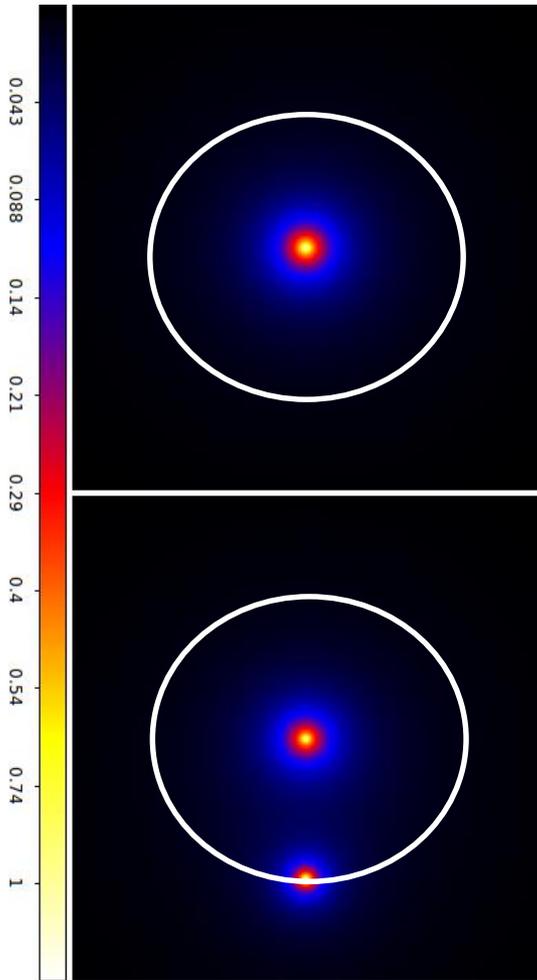


- Tangential shear is a powerful probe of **1-halo term**, or **intra-halo structure**.
- Shear alone cannot recover absolute mass, known as **mass-sheet degeneracy**:

$\gamma$  remains unchanged by  $\kappa \rightarrow \kappa + \text{const.}$

# Non-local substructure effect

A substructure at  $R \sim r_{\text{vir}}$  of the main halo, modulating  $\Delta\Sigma(R) = \Sigma(< R) - \Sigma(R)$



Known 5%-10% negative bias in mass estimates from tangential-shear fitting, inherent to rich substructure in outskirts (Rasia+12)



# Averaged Halo Density Profile $\Sigma(R)$

Stacking lensing signals of individual clusters by

$$\langle\langle \Sigma \rangle\rangle = \left( \sum_n \mathcal{W}_n \right)^{-1} \left( \sum_n \mathcal{W}_n \Sigma_n \right),$$

*Summing over clusters ( $n=1, 2, \dots$ )*

with individual “sensitivity” matrix

$$(\mathcal{W}_n)_{ij} \equiv \Sigma_{(c, \infty)n}^{-2} (C_n^{-1})_{ij},$$

defined with total covariance matrix

$$C = C^{\text{stat}} + C^{\text{sys}} + C^{\text{lss}} + C^{\text{int}},$$

**With “trace-approximation”, averaging (stacking) is interpreted as**

$$\langle\langle M_\Delta \rangle\rangle = \frac{\sum_n \text{tr}(\mathcal{W}_n) M_{\Delta,n}}{\sum_n \text{tr}(\mathcal{W}_n)}$$

Umetsu et al. 2014,  
*ApJ*, 795, 163



# Concentration—Mass Scaling Relation

Consider a power-law scaling relation of the form:

$$c_{200c} = 10^\alpha \left( \frac{M_{200c}}{M_{\text{piv}}} \right)^\beta \left( \frac{1+z}{1+z_{\text{piv}}} \right)^\gamma,$$

with pivot mass and redshift  $M_{\text{piv}} = 10^{15} M_{\text{sun}} / h$ ,  $z_{\text{piv}} = 0.34$

Define new independent ( $X$ ) and dependent ( $Y$ ) variables:

$$Y \equiv \log_{10} \left[ \left( \frac{1+z}{1+z_{\text{piv}}} \right)^{-\gamma} c_{200c} \right], \quad Y(X) = \alpha + \beta X$$
$$X \equiv \log_{10} (M_{200c} / M_{\text{piv}}).$$

Redshift slope  $\gamma$  is fixed to the theoretical prediction for the CLASH sample,  $\gamma = -0.668$  (Meneghetti+14)



# Bayesian Regression Analysis

We take into account

- Covariance between observed  $M$  and  $c$
- Intrinsic scatter in  $c$
- Non-uniformity in mass probability distribution  $P(\log M)$

**Conditional probability**  $P(y|x)$  with  $(x,y) = \text{observed } (X,Y)$

$$\ln \mathcal{P}(\mathbf{y}|\mathbf{x}) = -\frac{1}{2} \sum_n \left[ \ln (2\pi\sigma_n^2) + \left( \frac{y_n - \langle y_n|x_n \rangle}{\sigma_n} \right)^2 \right], \quad (35)$$

where  $\langle y_n|x_n \rangle$  and  $\sigma_n^2 \equiv \text{Var}(y_n|x_n)$  are the conditional mean and variance of  $y_n$  given  $x_n$ , respectively:

$$\begin{aligned} \langle y_n|x_n \rangle &= \alpha + \beta\mu + \frac{\beta\tau^2 + C_{xy,n}}{\tau^2 + C_{xx,n}}(x_n - \mu), \\ \sigma_n^2 &= \beta^2\tau^2 + \sigma_{Y|X}^2 + C_{yy,n} - \frac{(\beta\tau^2 + C_{xy,n})^2}{\tau^2 + C_{xx,n}}, \end{aligned} \quad (36)$$

where  $\sigma_{Y|X}$  is the intrinsic scatter in the  $Y-X$  relation;



# Marginalized Posterior Distributions

$$c_{200c} = 10^\alpha \left( \frac{M_{200c}}{M_{\text{piv}}} \right)^\beta \left( \frac{1+z}{1+z_{\text{piv}}} \right)^\gamma$$

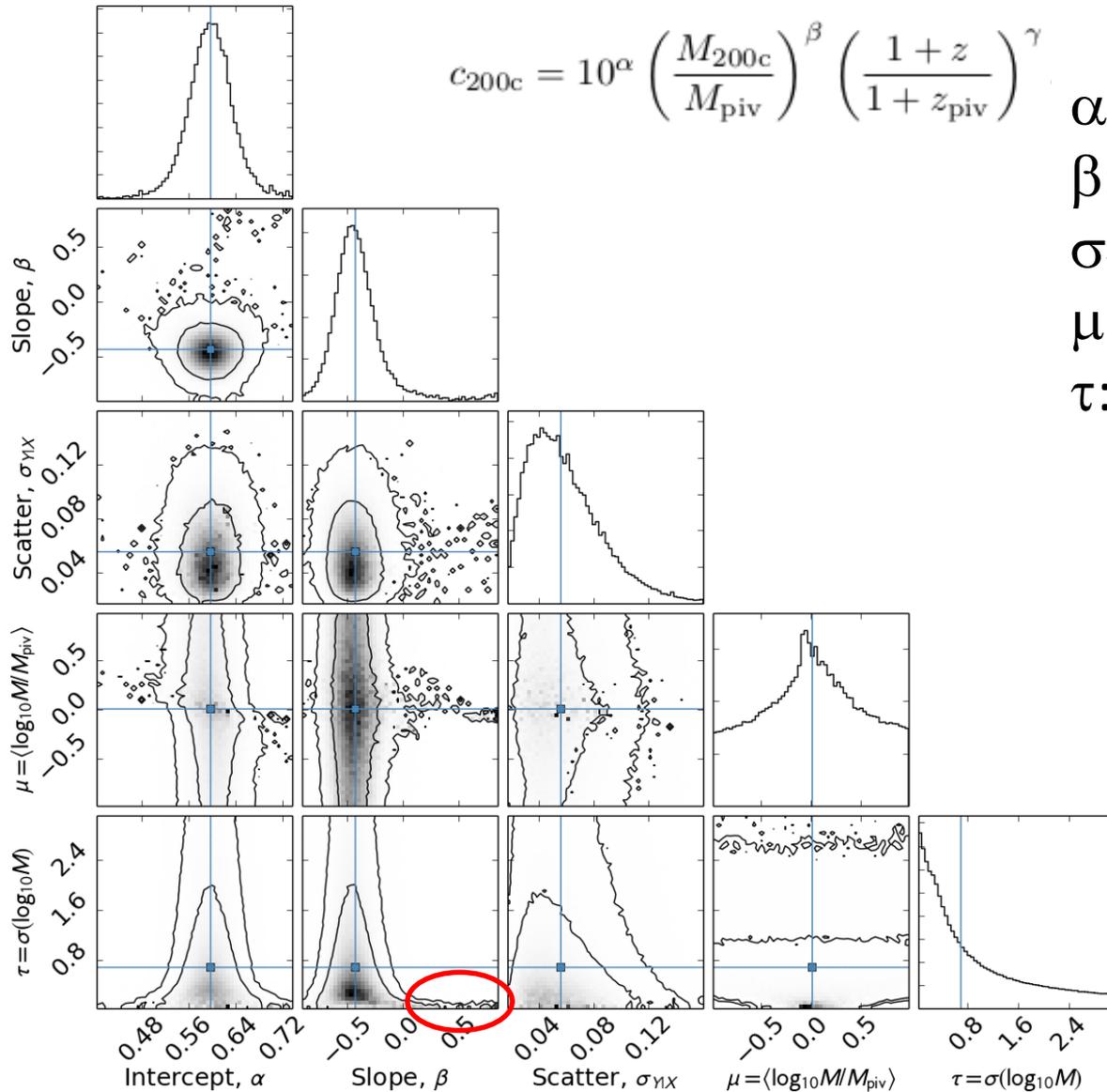
$\alpha$ : intercept

$\beta$ : slope

$\sigma_{Y|X}$ : scatter

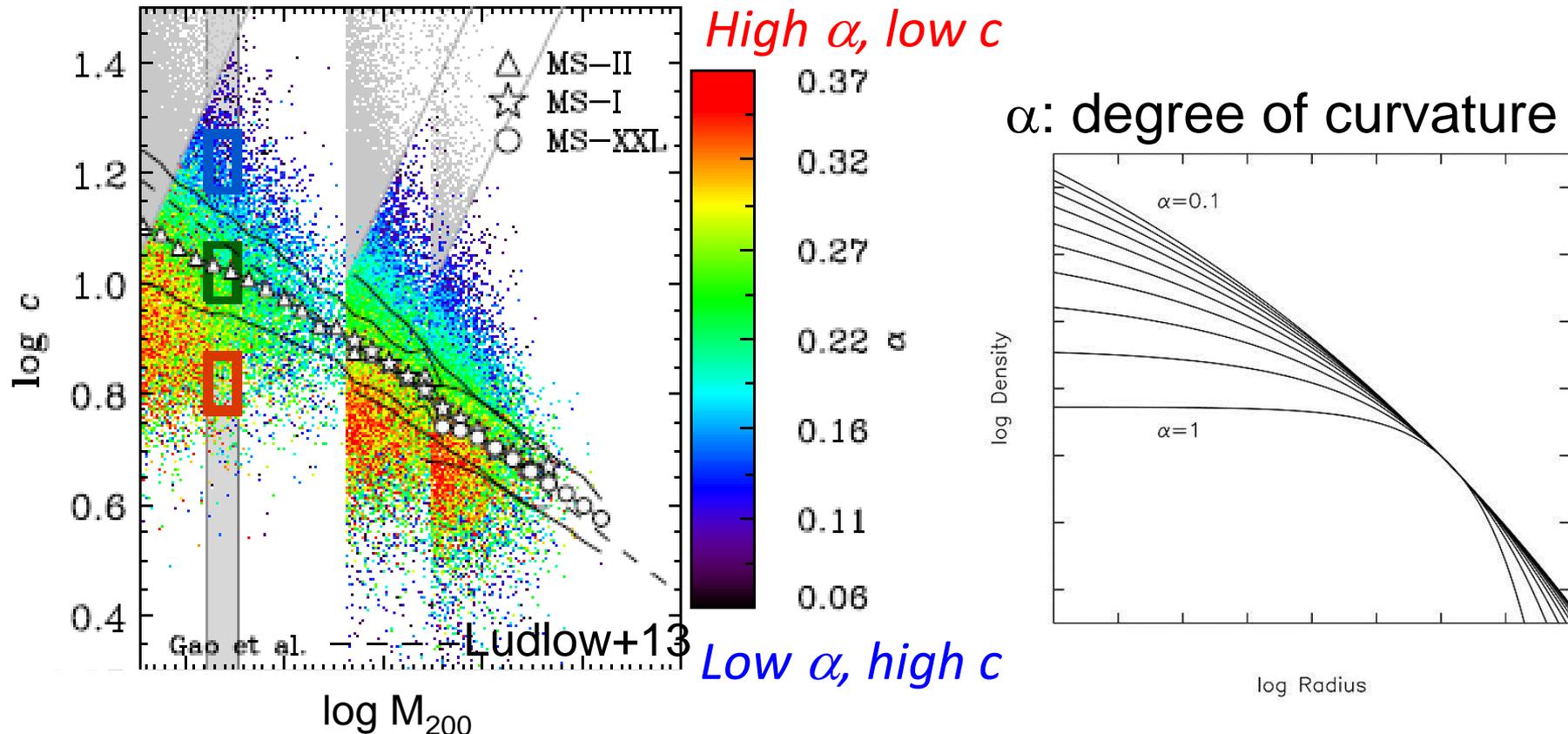
$\mu$ : Gaussian mean of  $P(\ln M)$

$\tau$ : Gaussian width of  $P(\ln M)$



High  $\beta$  tail associated with small  $\tau$ : i.e., localized  $P(\ln M)$

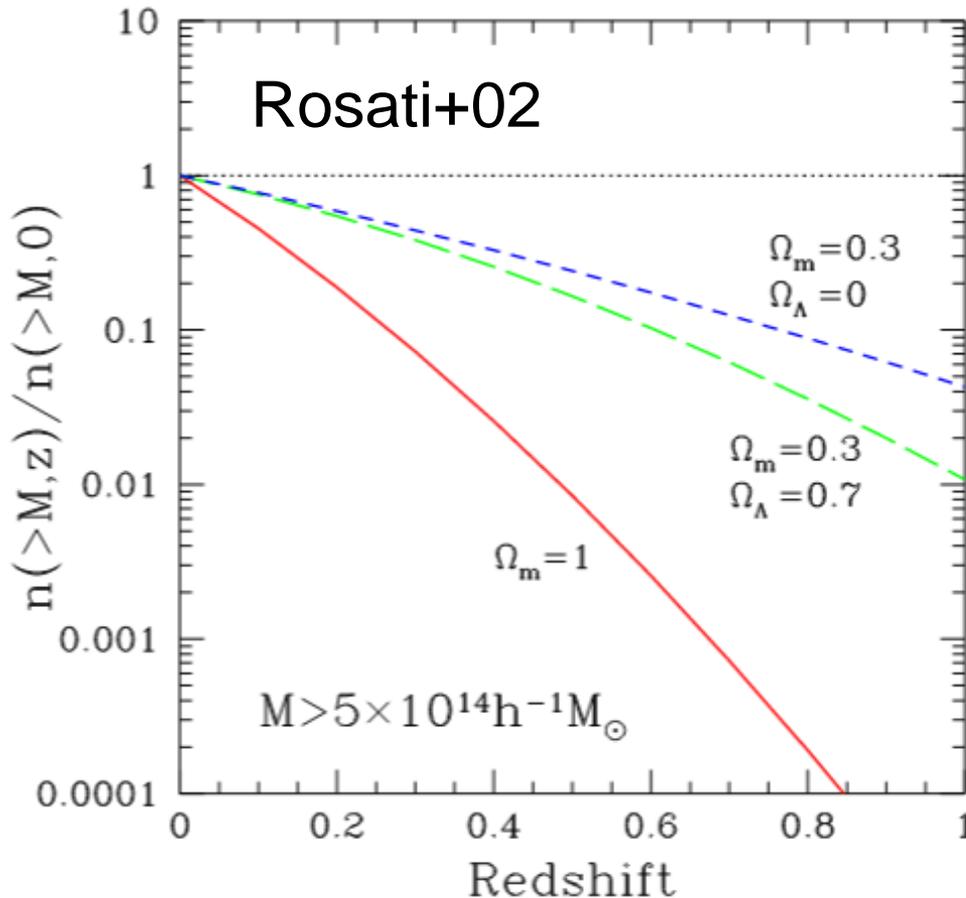
# Intrinsic Scatter in $c(M)$ : Mass Assembly Histories



- Scatter is due to another dof ( $\alpha$ ), related to MAH (Ludlow+13)
- Larger values of  $\alpha$  correspond to halos that have been assembled more rapidly than the NFW curve
- Halos with average  $c_{200c}$  have the NFW-equivalent  $\alpha \sim 0.18$

# Cluster Counts as Cosmological Probe

$$\frac{dN(> M_{\text{lim}}, z)}{d\Omega dz} = \int_{M_{\text{lim}}}^{\infty} dM \frac{dV(z)}{d\Omega dz} \frac{d^2 n}{dV dM}(M, z)$$



**Comoving volume element**

$$\frac{d^2 V}{dz d\Omega} = \frac{cr^2[\chi(z)]}{H(z)}, \quad \chi(z) = \int_0^z \frac{dz'}{H(z')}$$

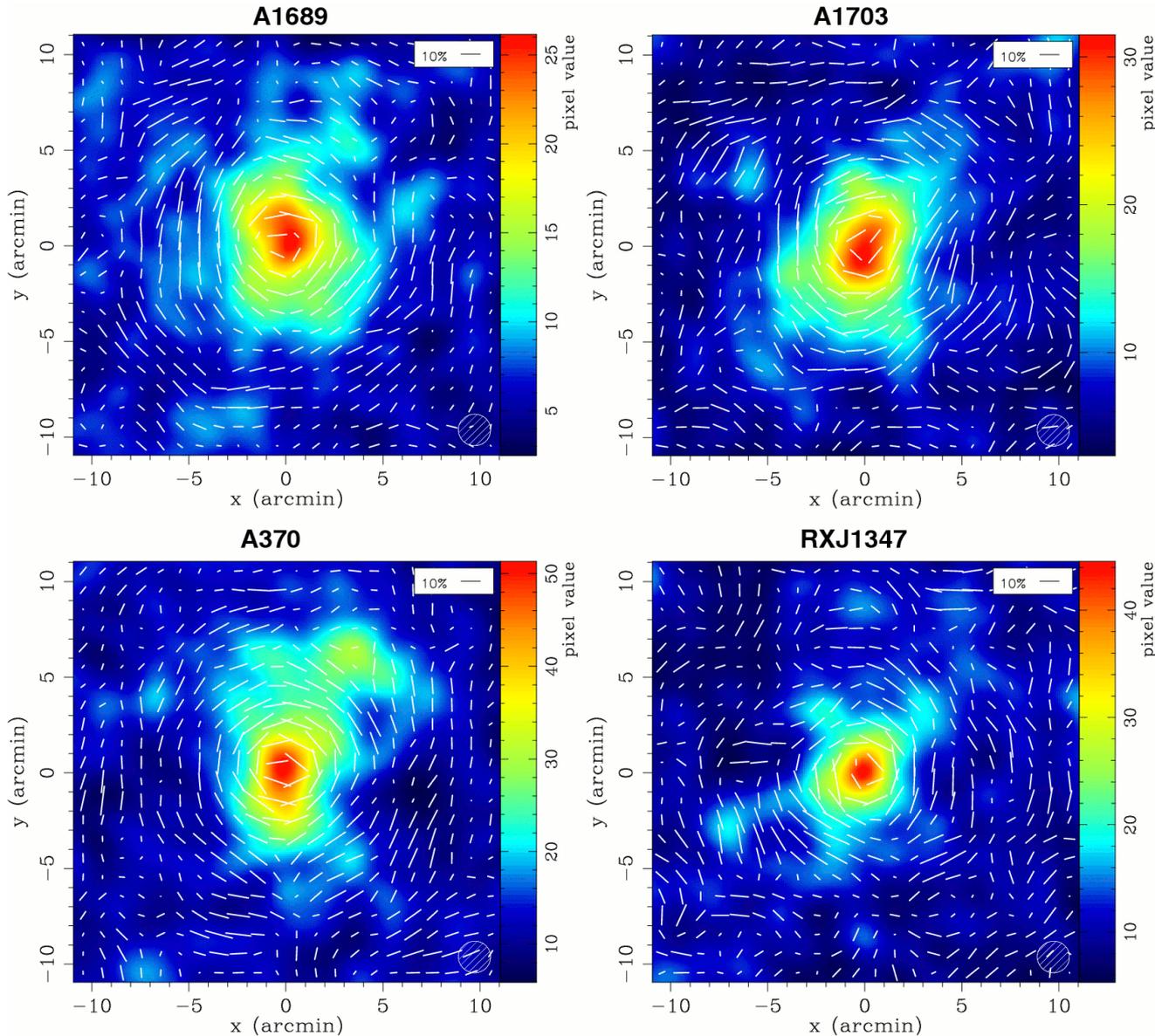
**Halo mass function**

$$\frac{d^2 n}{dV dM}(M, z) \propto \exp\left[-\frac{\nu^2}{2}\right]$$

$$\nu \equiv \frac{\delta_c(z)}{\sigma(M, z)} \approx \frac{1.69}{D_+(z)\sigma(M)} \sim 3 \text{ for clusters}$$

Cluster counts are exponentially sensitive to cosmology AND **cluster mass calibration!!!**

# Weak shear fields around high-mass clusters

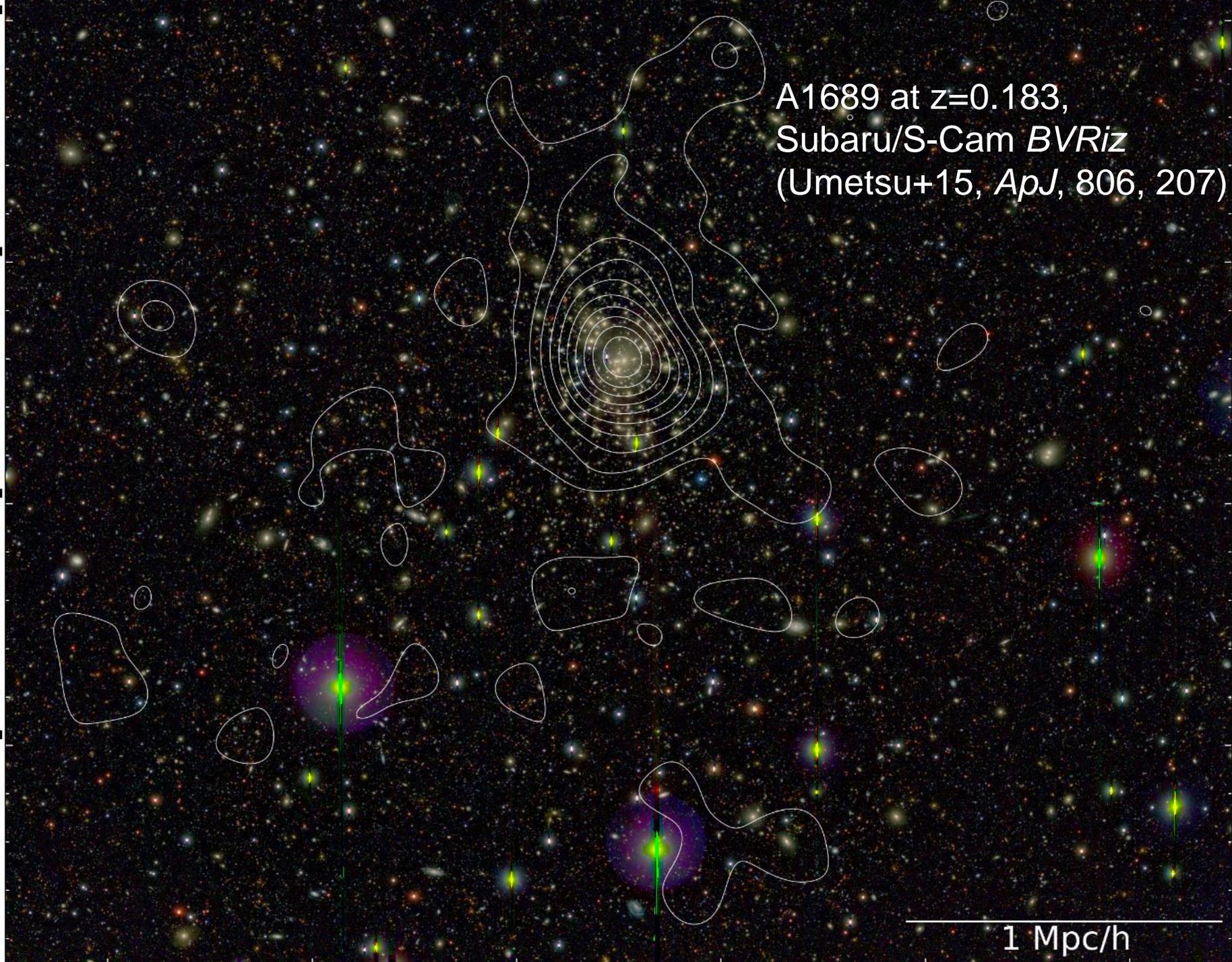


Map: **RS galaxies**  
Whiskers: **shear**

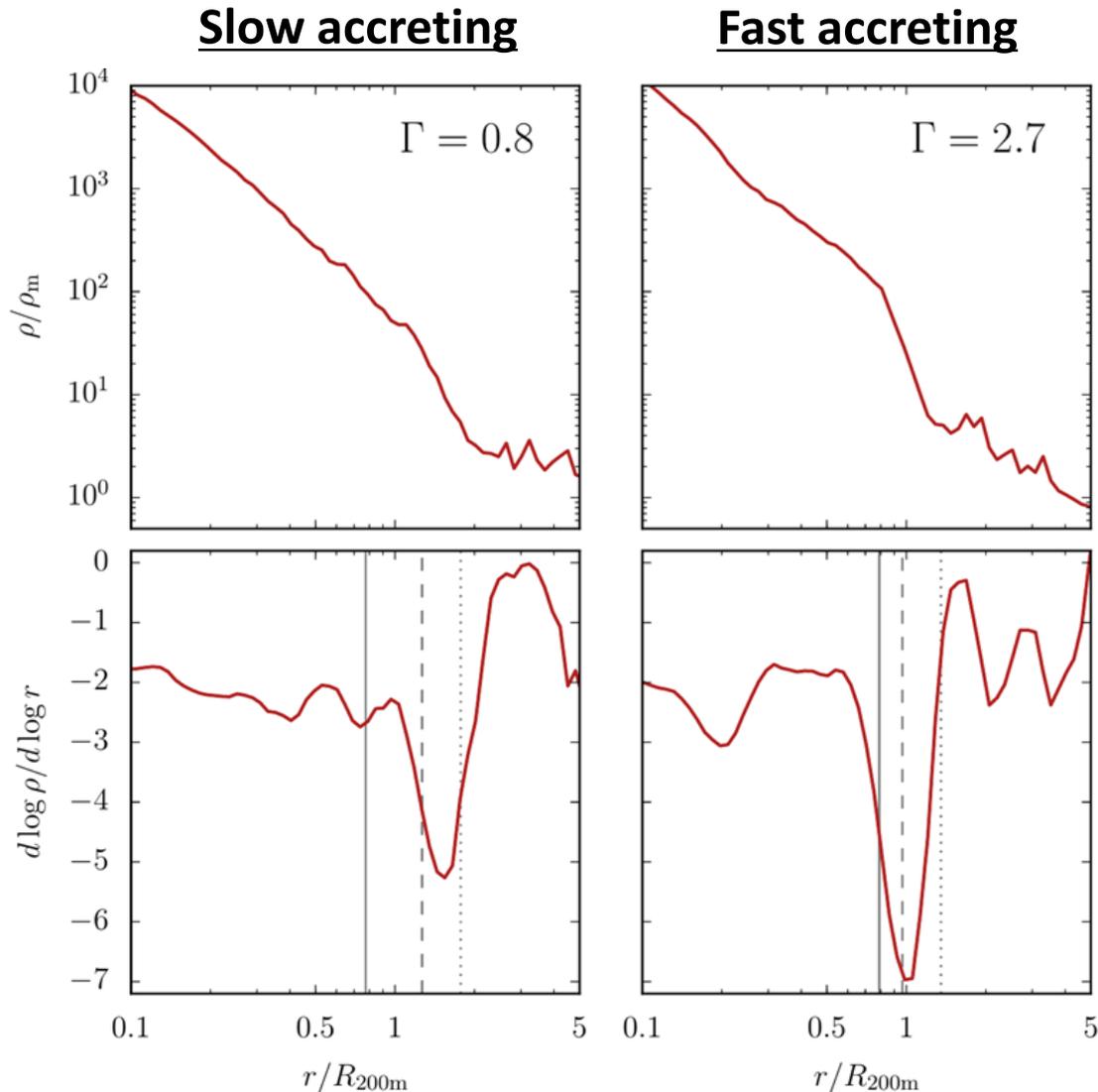
Subaru/S-Cam  
archival data

Broadhurst,  
Umetsu,  
Medezinski+08,  
*ApJL*, 685, L9

A1689 at  $z=0.183$ ,  
Subaru/S-Cam *BVRiz*  
(Umetsu+15, *ApJ*, 806, 207)



# Splashback radius depends on halo mass accretion rate, $\Gamma := \Delta(\ln M_{\text{vir}}) / \Delta(\ln a)$ (contd.)



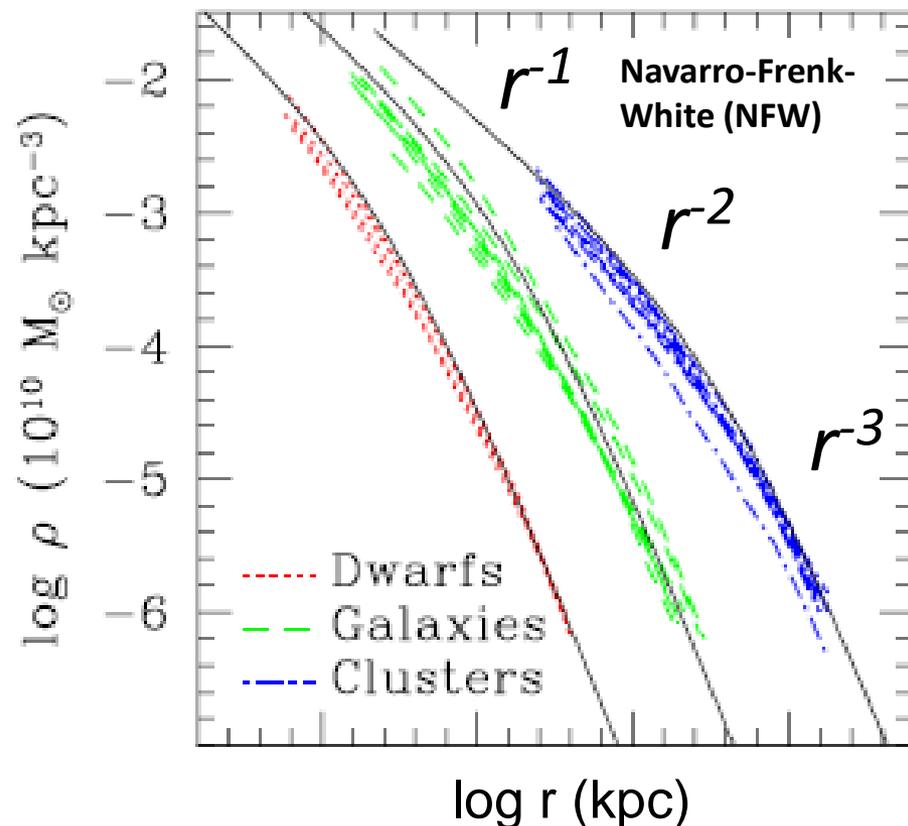
N-body simulations in  
LCDM

More, Diemer, &  
Kravtsov 15

# (1) Quasi-universal DM density profiles

Spherically-averaged density profiles  $\rho_h(r)$  of collisionless DM halos from numerical simulations  $\rho_h(r) \sim \rho_s f(r/r_s; \alpha)$

Cuspy, outwardly-steepening density profiles



*Theoretical models:*

- **DARKexp** (Hjorth & Williams 10): Statistical mechanical arguments to describe the distribution of particle energies in finite, self-gravitating, collisionless systems with isotropic orbits.
- **Pontzen & Governato 13**: Maximum-entropy arguments to derive the phase-space distribution for an end product of violent relaxation
- **Adhikari, Dalal, & Chamberlain 14**: outskirts steepening (splashback radius) associated with first apocentric passage after accretion



# CLASH X-ray-selected subsample optimized for mass-profile analysis

- **High-mass clusters with smooth X-ray morphology**

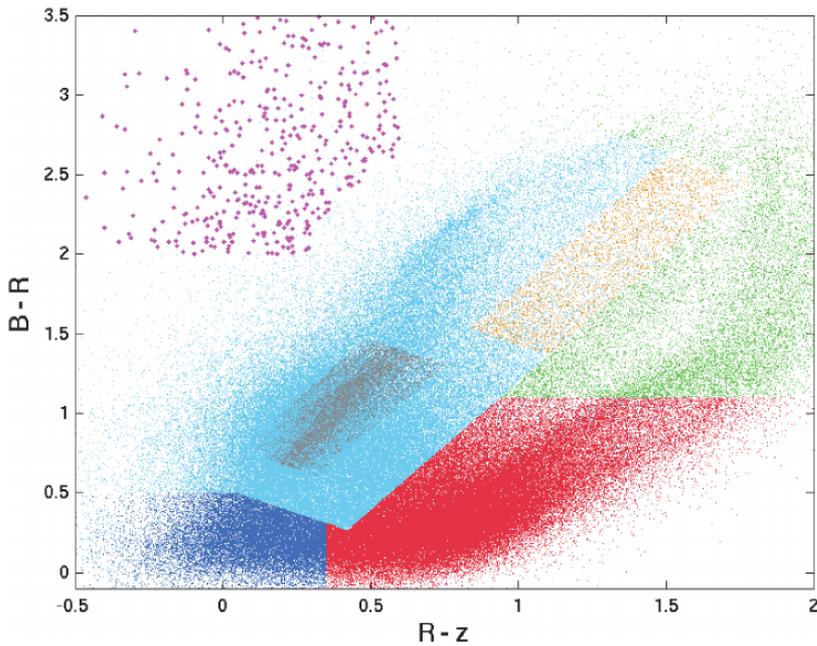
- $T_x > 5\text{keV}$  ( $6e14M_{\text{sun}} < M_{200c} < 30e14M_{\text{sun}}$ )
- Small BCG -X-ray offset,  $\sigma_{\text{off}} \sim 10\text{kpc}/h$
- Smooth, regular X-ray morphology

- **CLASH theoretical predictions** (Meneghetti+14, *ApJ*, 797, 34)

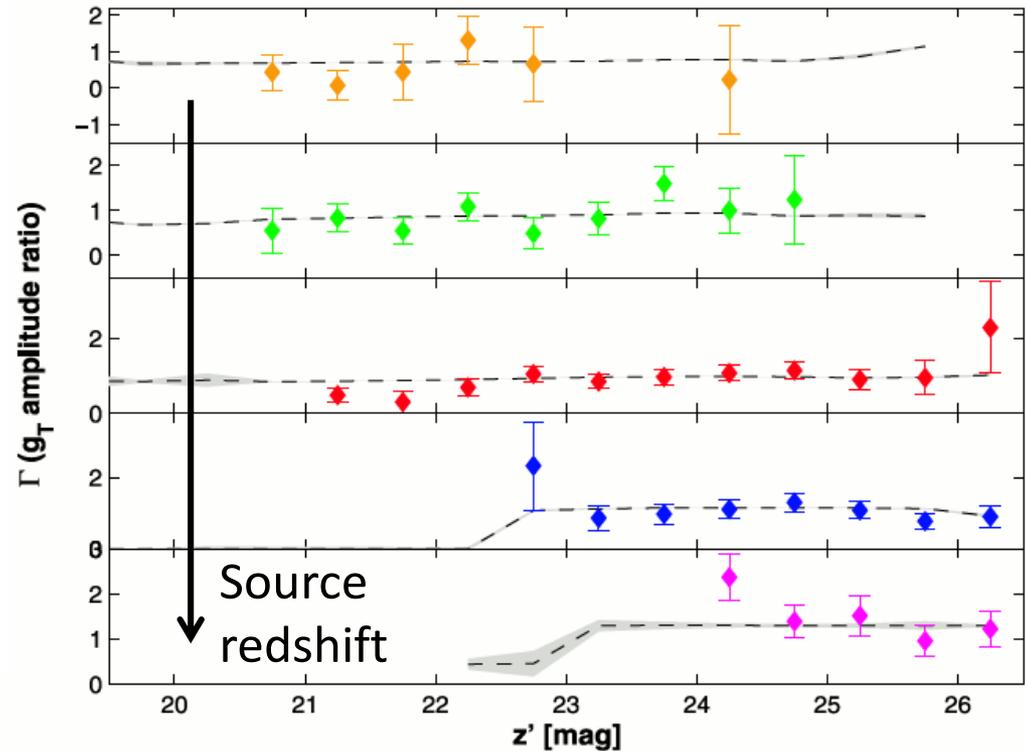
- Composite relaxed (70%) and unrelaxed (30%) clusters
- Mean  $\langle c_{200c} \rangle = 3.9$ ,  $c_{200c} = [3, 6]$
- Small scatter in  $c_{200c}$ :  $\sigma(\ln c_{200c}) = 0.16$
- Largely free of orientation bias ( $\sim 2\%$  in  $\langle M_{3D} \rangle$ )
- 90% of CLASH clusters to have strong-lensing features

# Tangential shear signal

Source selection in Subaru color-color ( $BRz'$ ) space



Subaru WL signal (Abell 370)  $\gamma_+ \propto \frac{D_{LS}}{D_S}$



KSB+ shape pipeline of Umetsu+10 used

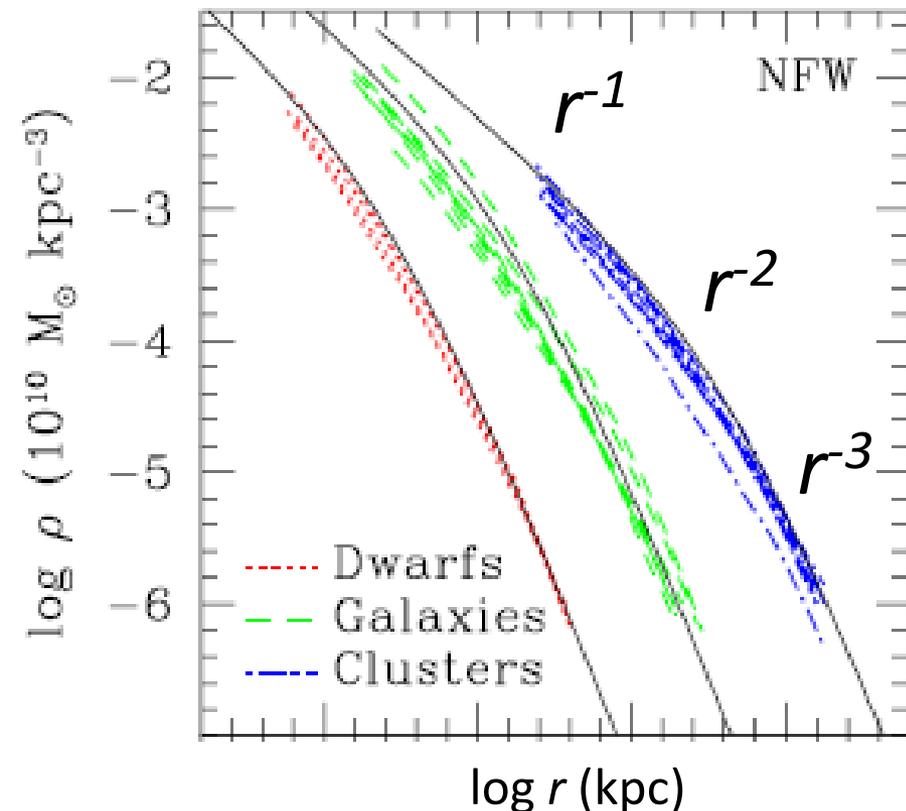
# Key predictions of structure formation models

- (1) DM halo density profile**
- (2) Halo concentration—mass relation**
- (3) Halo bias**

# (1) Quasi-universal DM density profiles

*N*-body simulations of collisionless DM produce cuspy, outwardly steepening density profiles of halos in equilibrium.

Navarro-Frenk-White 96, 97 (NFW)



**Universal? (e.g., NFW profile)**

$$\langle \rho_h \rangle(r) \sim \rho_s f(r/r_s)$$

**Non-universal? (e.g., Einasto profile) – diversity due to additional “degree of freedom”**

$$\langle \rho_h \rangle(r) \sim \rho_s f(r/r_s; \alpha)$$

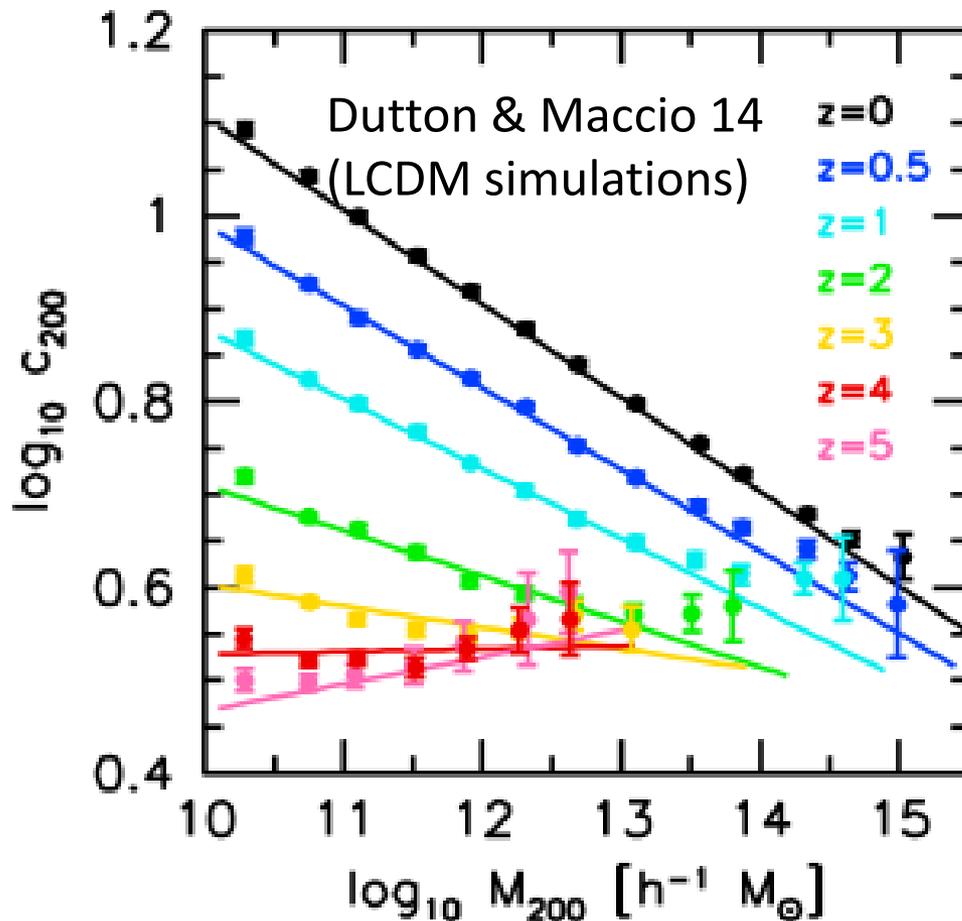
- Velocity anisotropy (Lapi+Cavaliere 09)
- Central potential depth (Hjorth+Williams 10)
- Mass accretion history (Ludlow+13)
- $\langle \alpha_{\text{Einasto}} \rangle = 0.155 + 0.0095 v^2(M)$  (Gao+08)

# Key predictions of structure formation models

- (1) DM halo density profiles**
- (2) Halo concentration—mass relation**
- (3) Halo bias**

## (2) Halo concentration, $c_{\Delta}$

$$c_{200c} \equiv \frac{R_{200c}}{r_s} = \frac{\text{(Outer scale radius)}}{\text{(Inner scale radius)}}$$

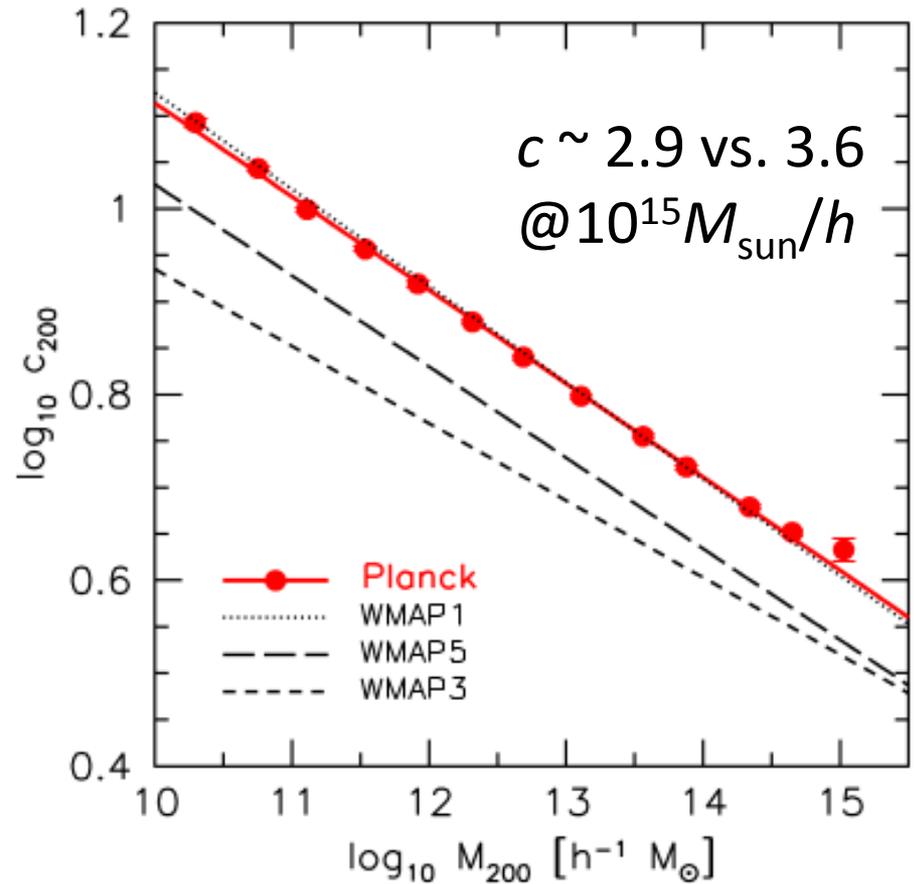
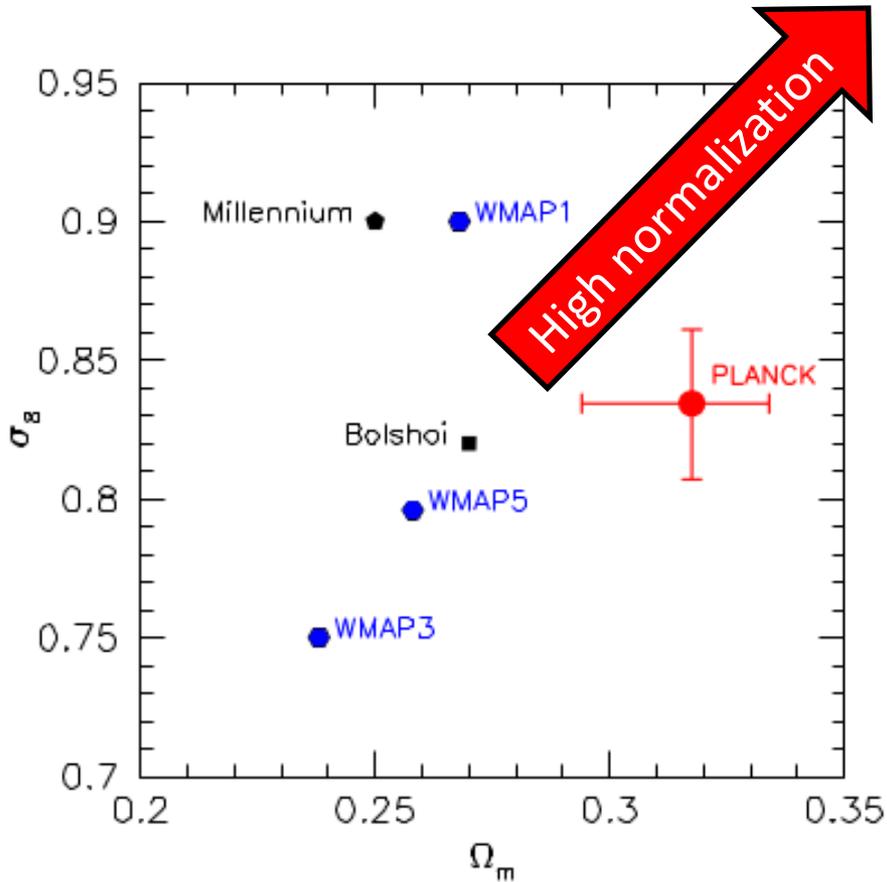


In hierarchical structure formation,  $\langle c \rangle$  is predicted to correlate with  $M$ :

DM halos that are more massive collapse later on average, when the mean background density of the universe is correspondingly lower.

Sizeable intrinsic scatter (at fixed  $M$ )  
 $\sim 30\%$ - $40\%$ , reflecting diversity of mass accretion history & formation epoch.

# Concentration is sensitive to cosmology



# Key predictions of structure formation models

- (1) DM halo density profiles**
- (2) Halo concentration—mass relation**
- (3) Halo bias**

# (3) Halo bias factor, $b_h$

Clustering of matter  
around halos with  $M$ :

$$\xi_{\text{hm}}(r | M) = \frac{\langle \rho_h \rangle(r | M)}{\rho_m} + b_h(M) \xi_{\text{mm}}(r)$$

Correlated matter distribution (2h term)

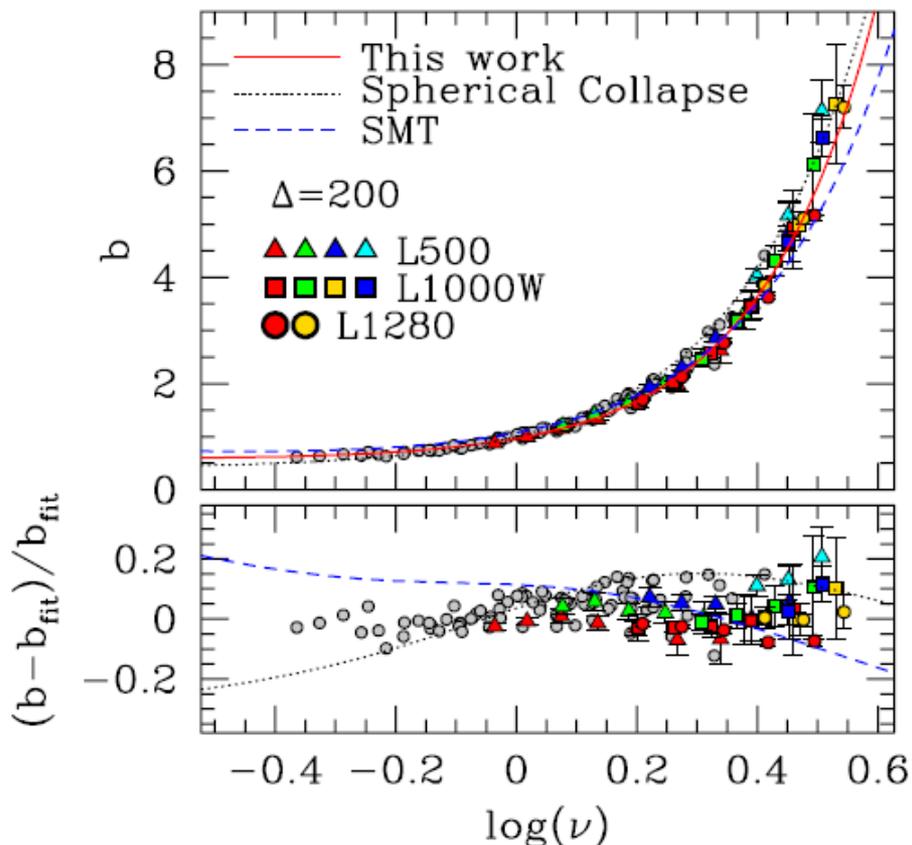
Matter correlation function:

$$\xi_{\text{mm}}(\mathbf{r}) = \text{FT}[P_L(\mathbf{k})] \propto \sigma_8^2$$

Linear halo bias:

$$b_h(v) \approx 1 + \frac{v^2 - 1}{\delta_c}$$

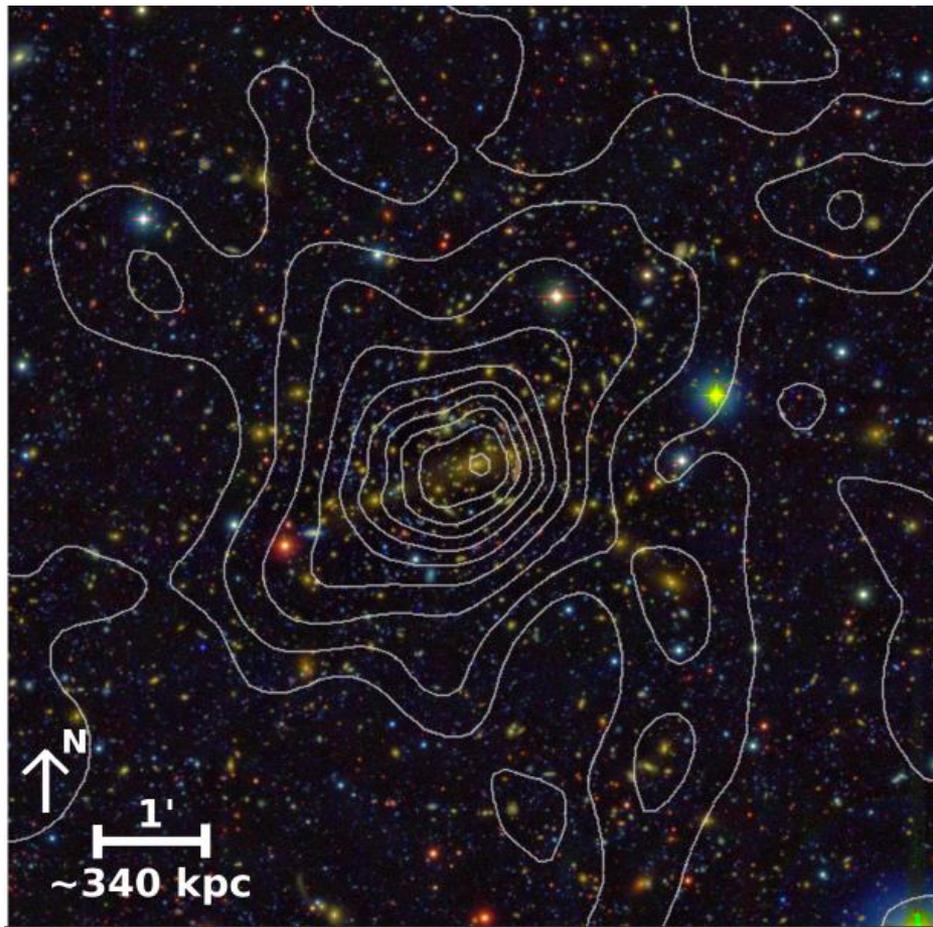
$$v \equiv \frac{\delta_c}{\sigma(M, z)} \sim 3 - 4 \text{ for clusters}$$



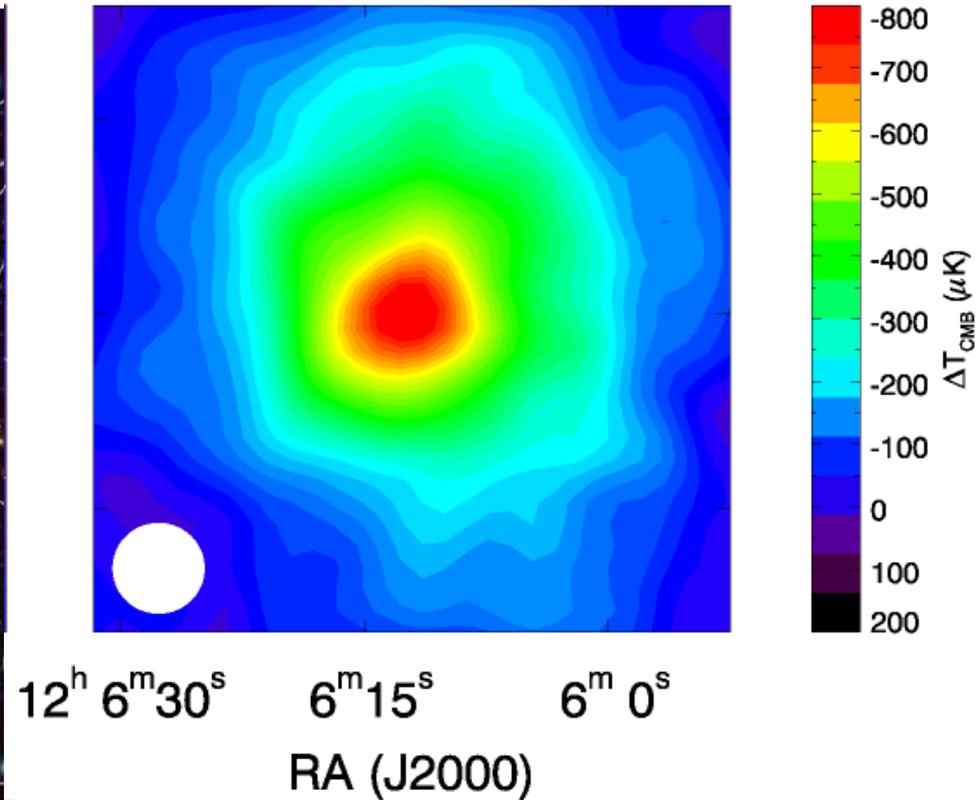
Tinker+10 LCDM simulations

# Clusters of Galaxies

**Optical/NIR**(cluster member galaxies  
and lensed background galaxies)



**Radio/mm** (intracluster plasma)

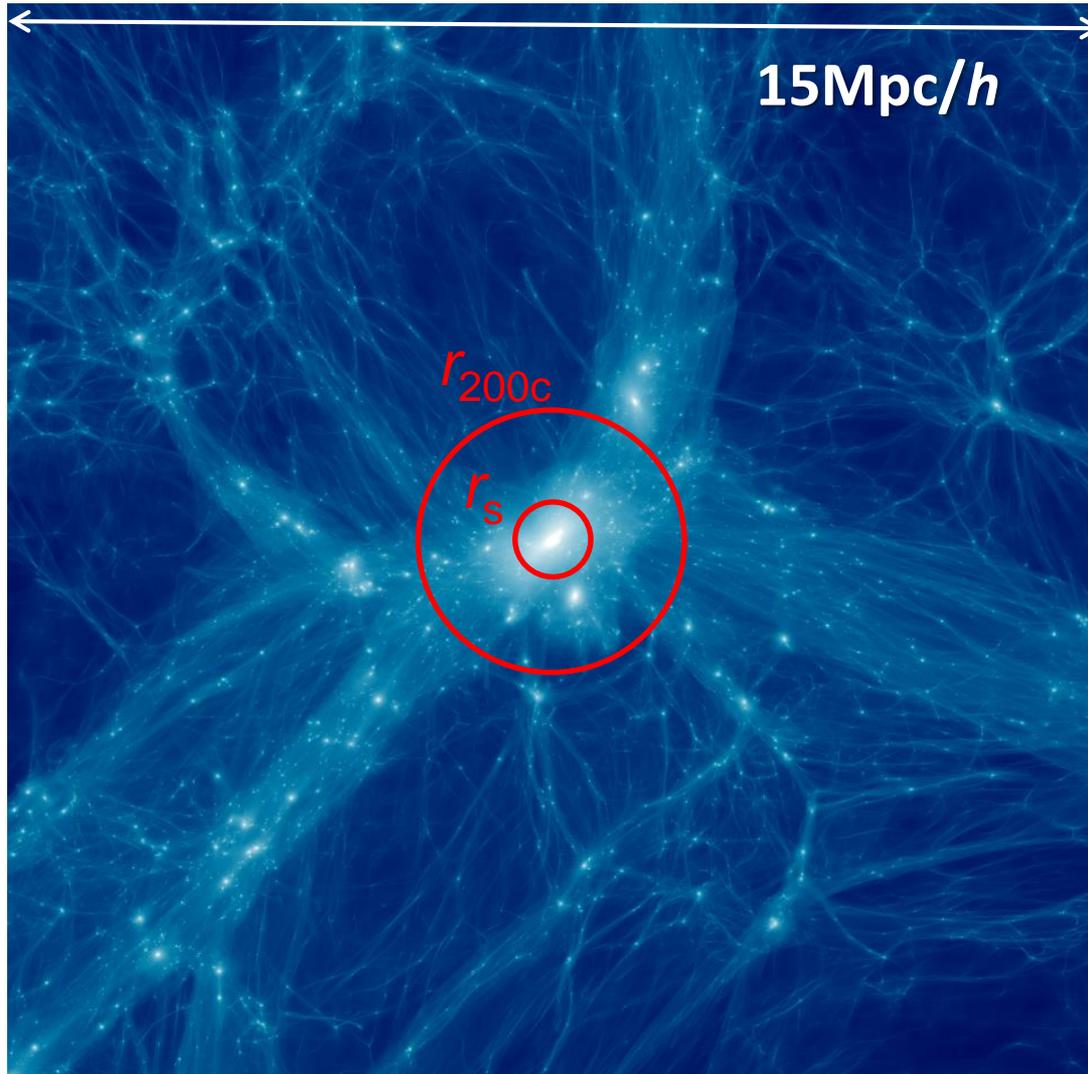


MACS1206 cluster at  $z=0.44$   
(Umetsu+12, *ApJ*, 755, 56)

## 2. Approach

# **Cluster Gravitational Lensing**

# Cluster cosmology: Key ingredients



## Intra-halo structure

Density profile shape,  $\rho(r)$

Halo mass,  $M_{\Delta} = M(<r_{\Delta})$

Concentration,  $c_{\Delta} = r_{\Delta}/r_s$

Splashback radius,  $R_{sp}$

Halo shape

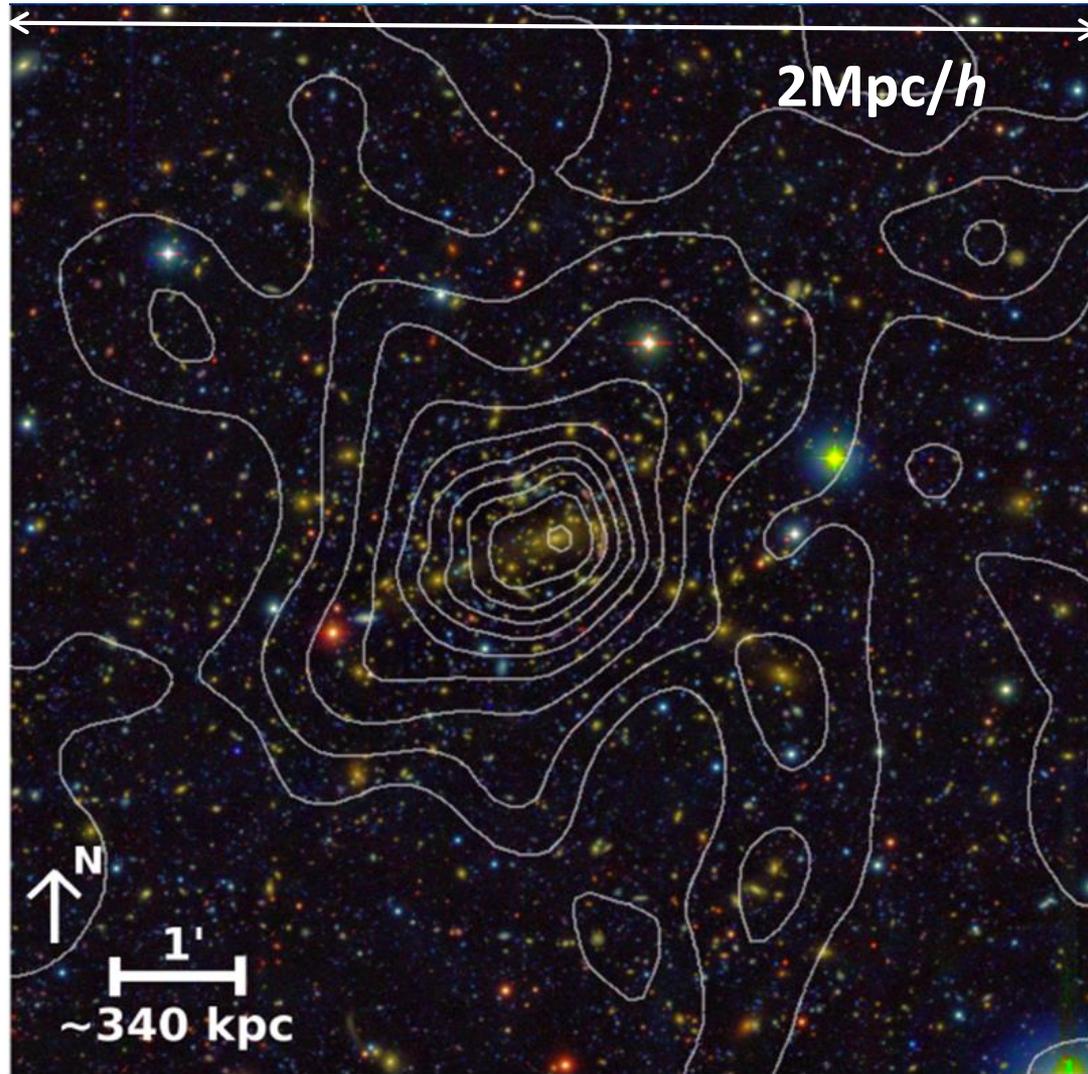
## Surrounding LSS

Halo bias  $b_h$

DM clustering strength,  $\sigma_8$

Assembly bias

# Approach: Gravitational Lensing



## Intra-halo structure

Density profile shape,  $\rho(r)$

Halo mass,  $M_{\Delta} = M(<r_{\Delta})$

Concentration,  $c_{\Delta} = r_{\Delta}/r_s$

Splashback radius,  $R_{sp}$

Halo shape

## Surrounding LSS

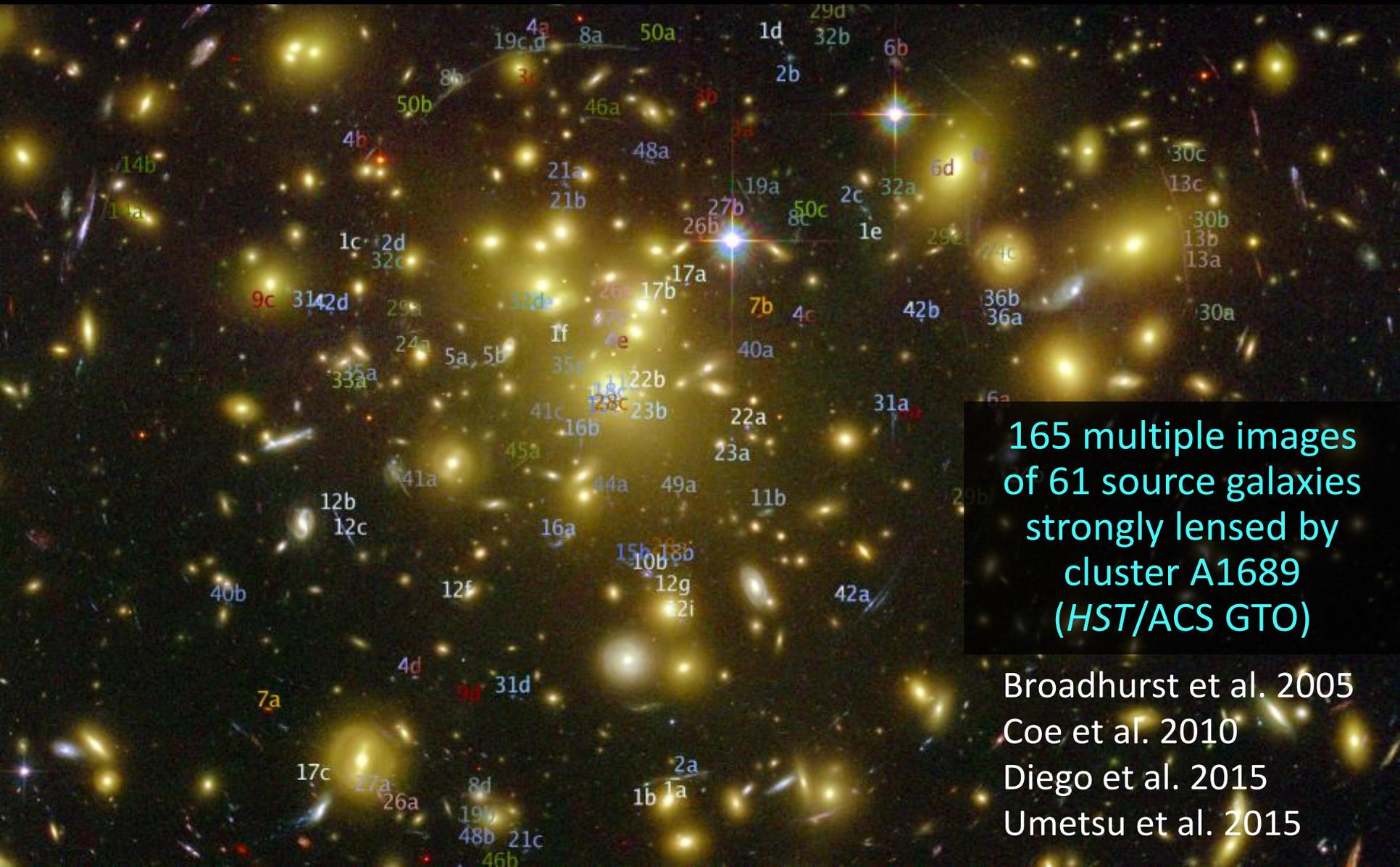
Halo bias  $b_h$

DM clustering strength,  $\sigma_8$

Assembly bias

(Umetsu+12, *ApJ*, 755, 56)

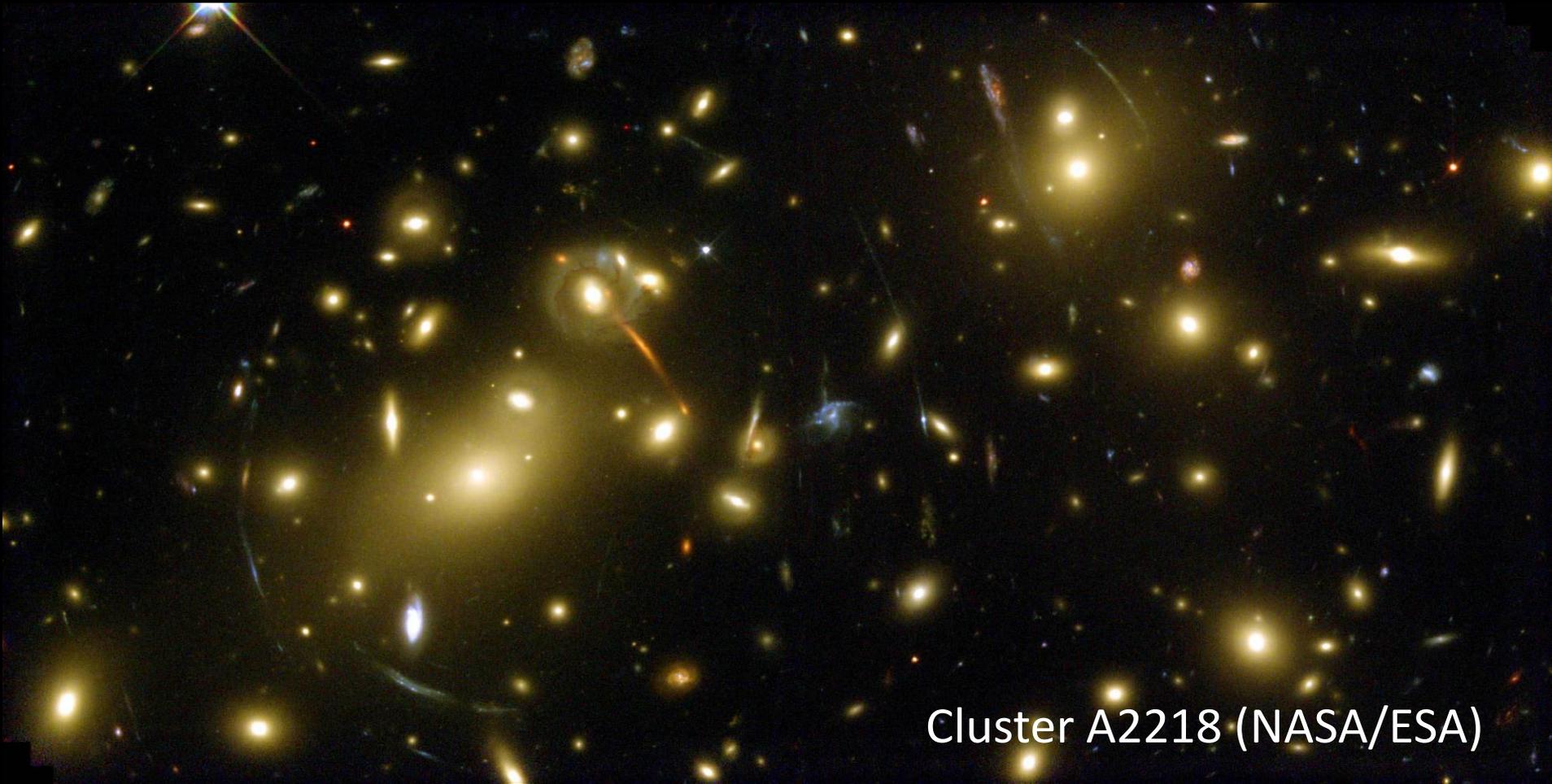
# Multiple Imaging (Strong Lensing)



165 multiple images  
of 61 source galaxies  
strongly lensed by  
cluster A1689  
(*HST/ACS GTO*)

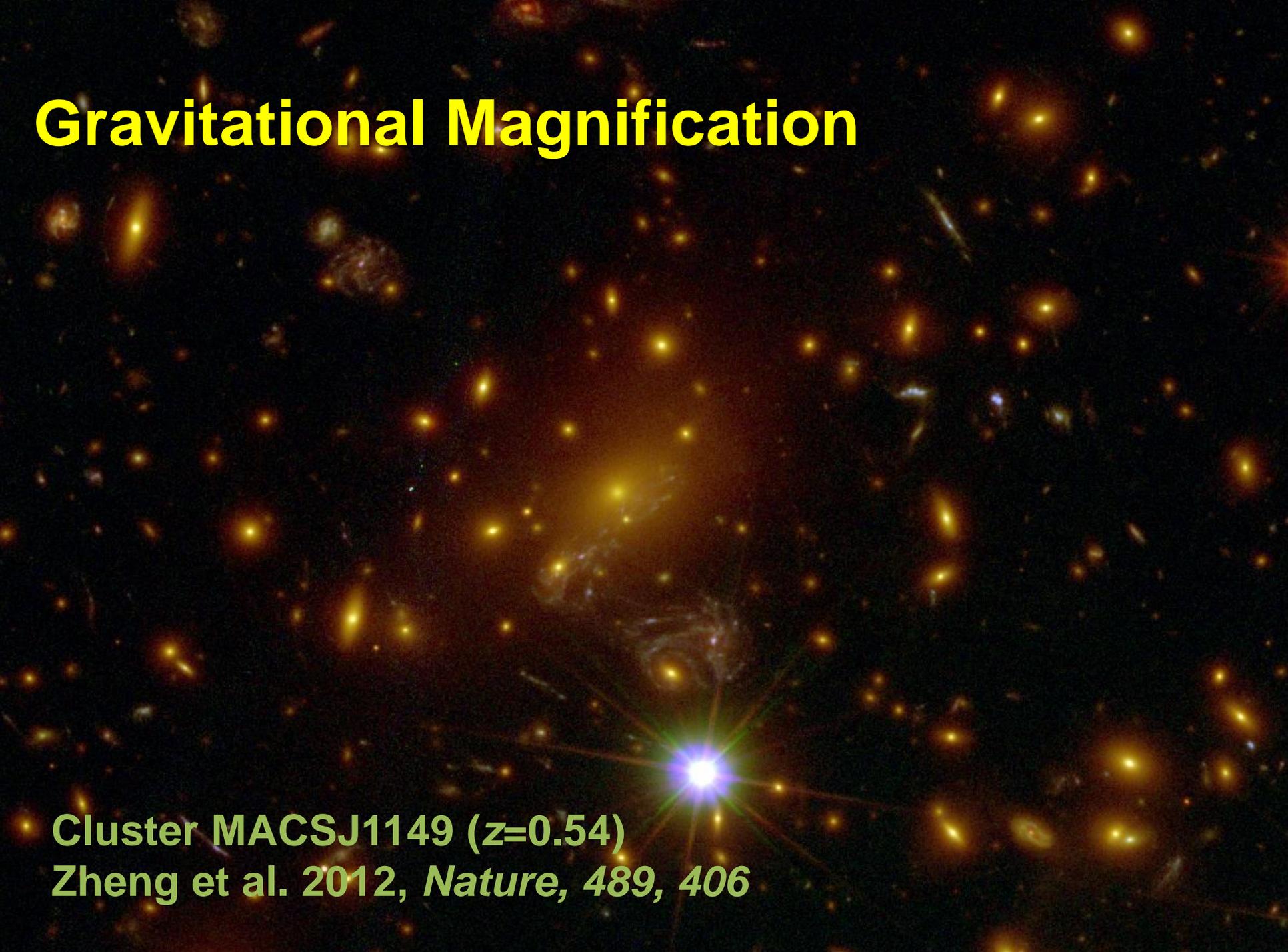
Broadhurst et al. 2005  
Coe et al. 2010  
Diego et al. 2015  
Umetsu et al. 2015

# Gravitational Shear



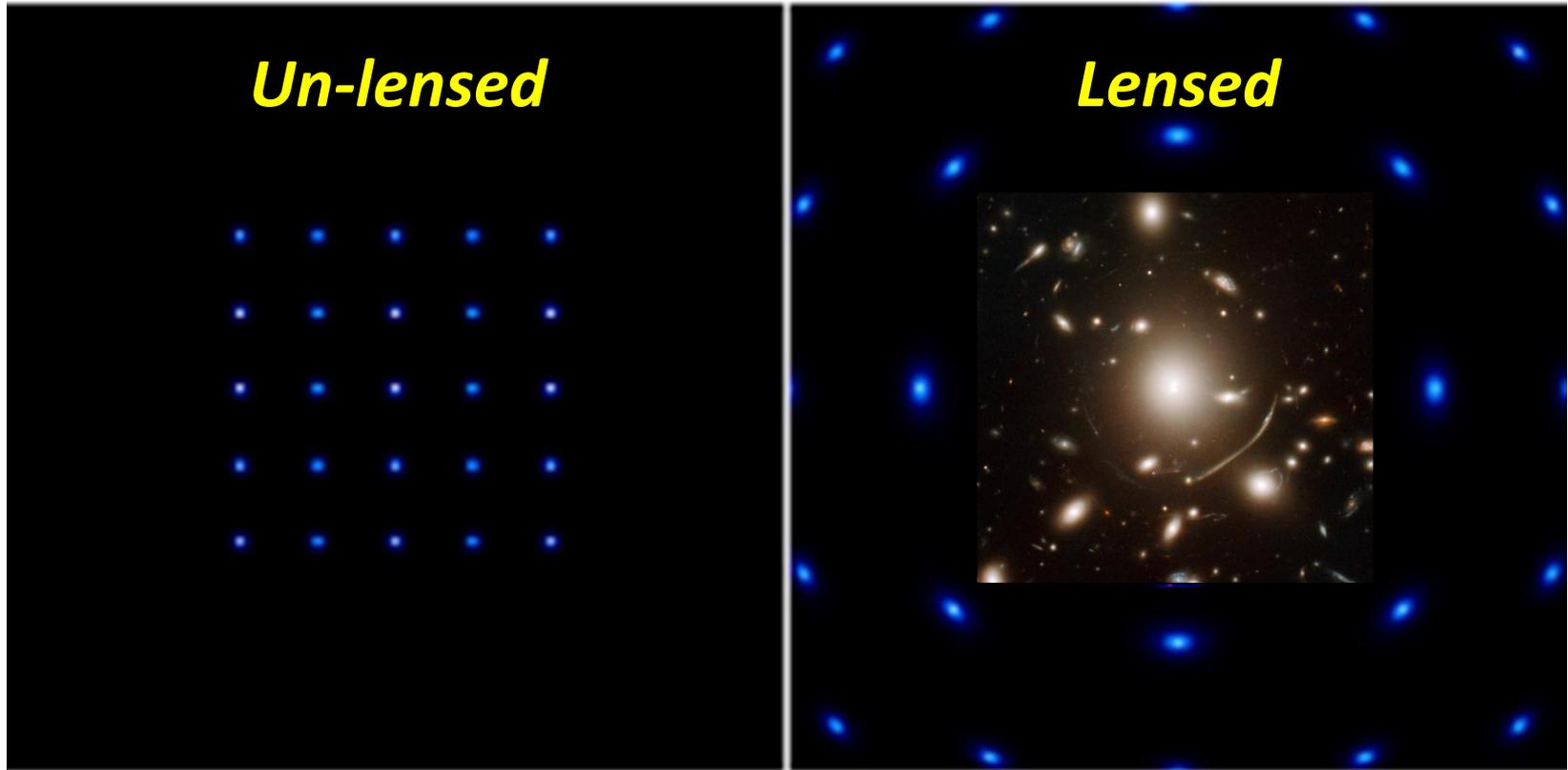
Cluster A2218 (NASA/ESA)

# Gravitational Magnification



Cluster MACSJ1149 ( $z=0.54$ )  
Zheng et al. 2012, *Nature*, 489, 406

# Weak lensing: shear & magnification



- **Shear** (Kaiser 92)
  - ✓ Shape distortion:  $\delta e \sim \gamma$
- **Magnification** (Broadhurst+95)
  - ✓ Flux amplification:  $\mu F$
  - ✓ Area distortion:  $\mu \Delta \Omega$

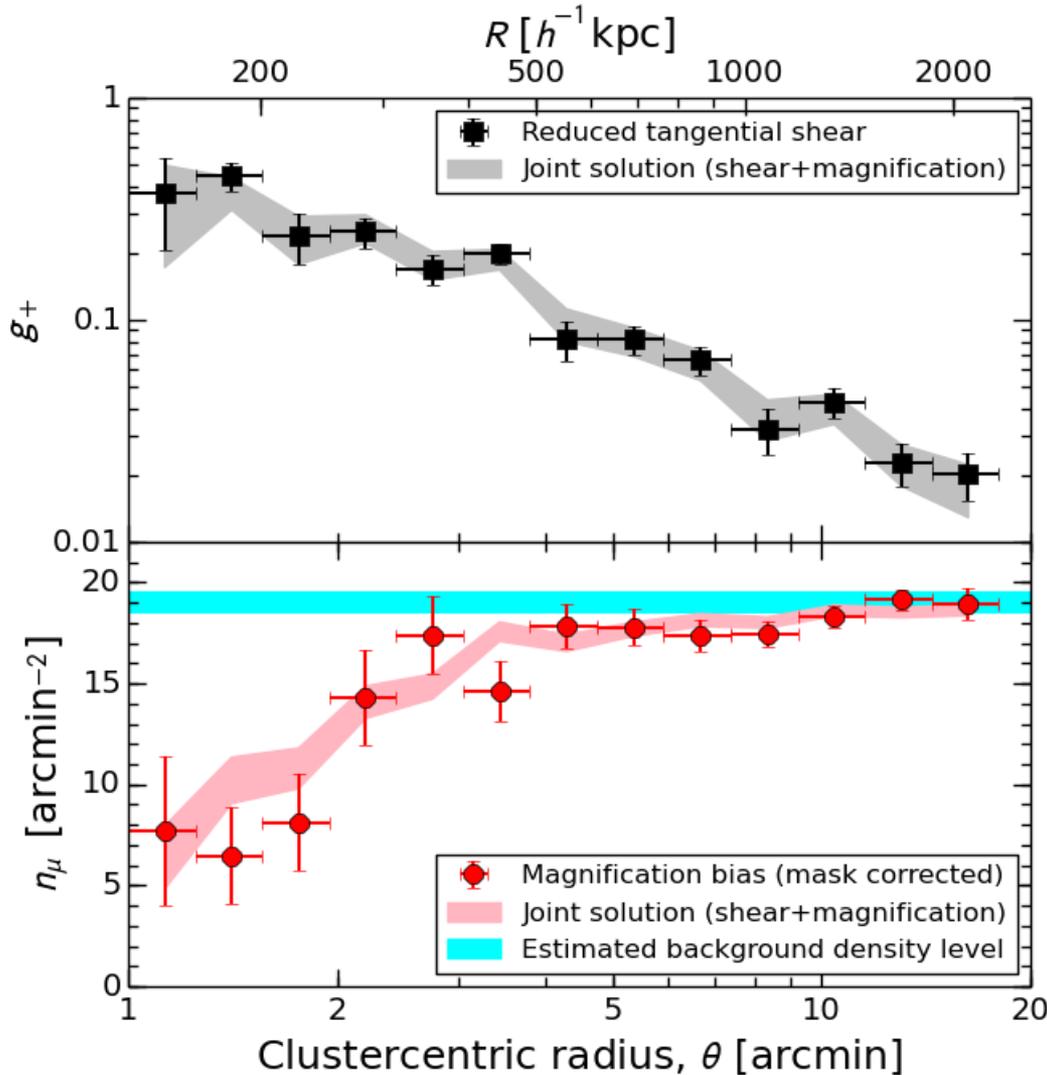
*Sensitive to “modulated” matter density*

$$\Sigma_c \gamma_+ = \Delta \Sigma(R) \equiv \Sigma(< R) - \Sigma(R)$$

*Sensitive to “total” matter density*

$$\mu \approx 1 + 2\kappa; \quad \Sigma_c \kappa = \Sigma(R) = \int (\rho - \bar{\rho}_m) dl$$

# Shear vs. Magnification



## Reduced tangential shear

$$g_+ \approx \gamma_+ = \Delta\Sigma / \Sigma_c$$

## Number count depletion due to magnification

$$n(< m_{\text{lim}}) = \bar{n}(< m_{\text{lim}}) \mu^{-1+2.5s}$$

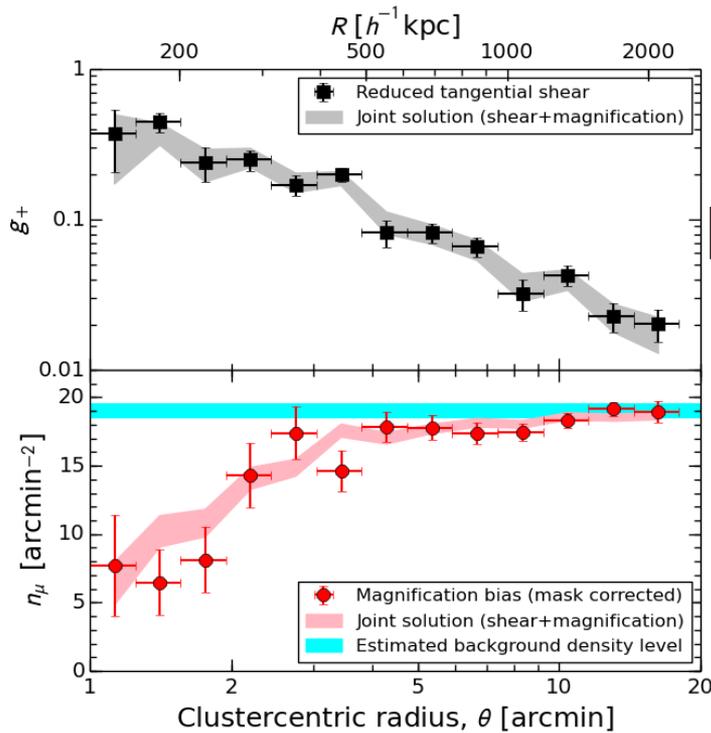
$$\text{with } s = \left[ d \log_{10} \bar{n}(< m) / dm \right]_{m=m_{\text{lim}}} < 0.4$$

Subaru *BVRiz* data, A1689  
(Umetsu+15, *ApJ*, 806, 207)

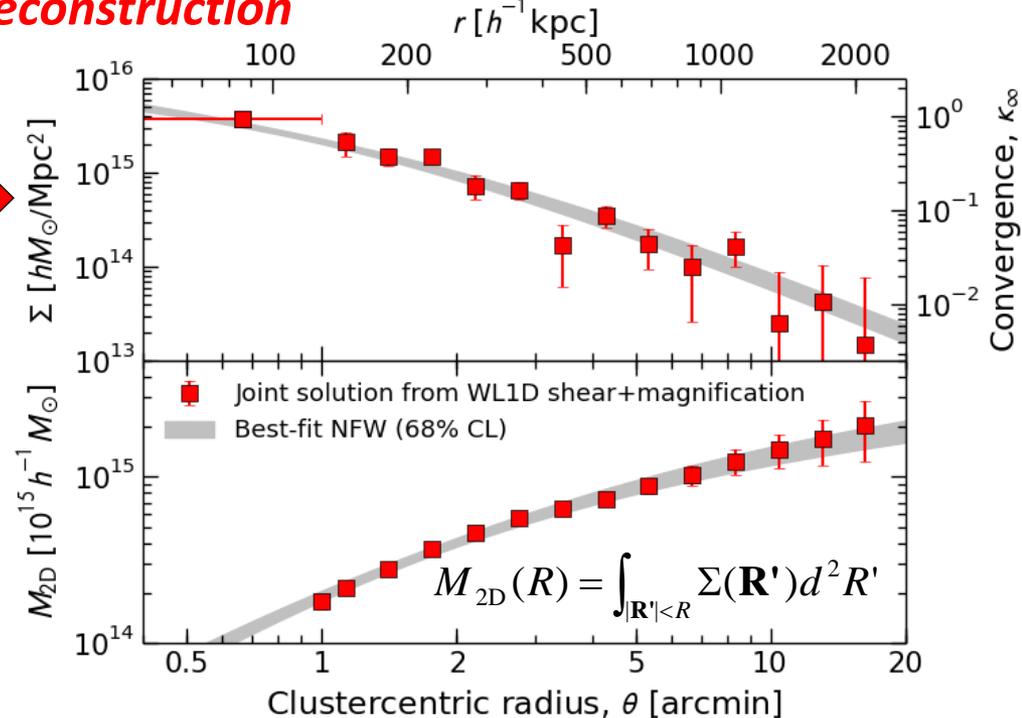
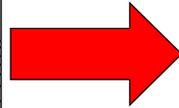
# Cluster Lensing Mass Inversion (CLUMI) code

Umetsu+11a, *ApJ*, 729, 127

$$P(\Sigma|WL) \propto P(WL|\Sigma)P(\Sigma) = P(n_{\mu}|\Sigma)P(g_{+}|\Sigma)P(\Sigma)$$



**Joint reconstruction**



- Mass-sheet degeneracy broken
- Total statistical precision improved by  $\sim 20\text{-}30\%$
- Calibration uncertainties marginalized over:  $c = \{\langle W \rangle_s, f_{W,s}, \langle W \rangle_{\mu}, \bar{n}_{\mu}, s_{\text{eff}}\}$ .